

Nuclear structure

Why ?

To identify the different phenomena at the origin of the nuclear properties

To develop models able to describe these phenomena

Test the models at their limits

High spin nuclei: to explore the nuclei at the limits of the angular momentum.

Heavy and super heavy nuclei: to explore the nuclei at the limits in charge.

Exotic nuclei: to explore the nuclei at the limits in isospin.

How ?

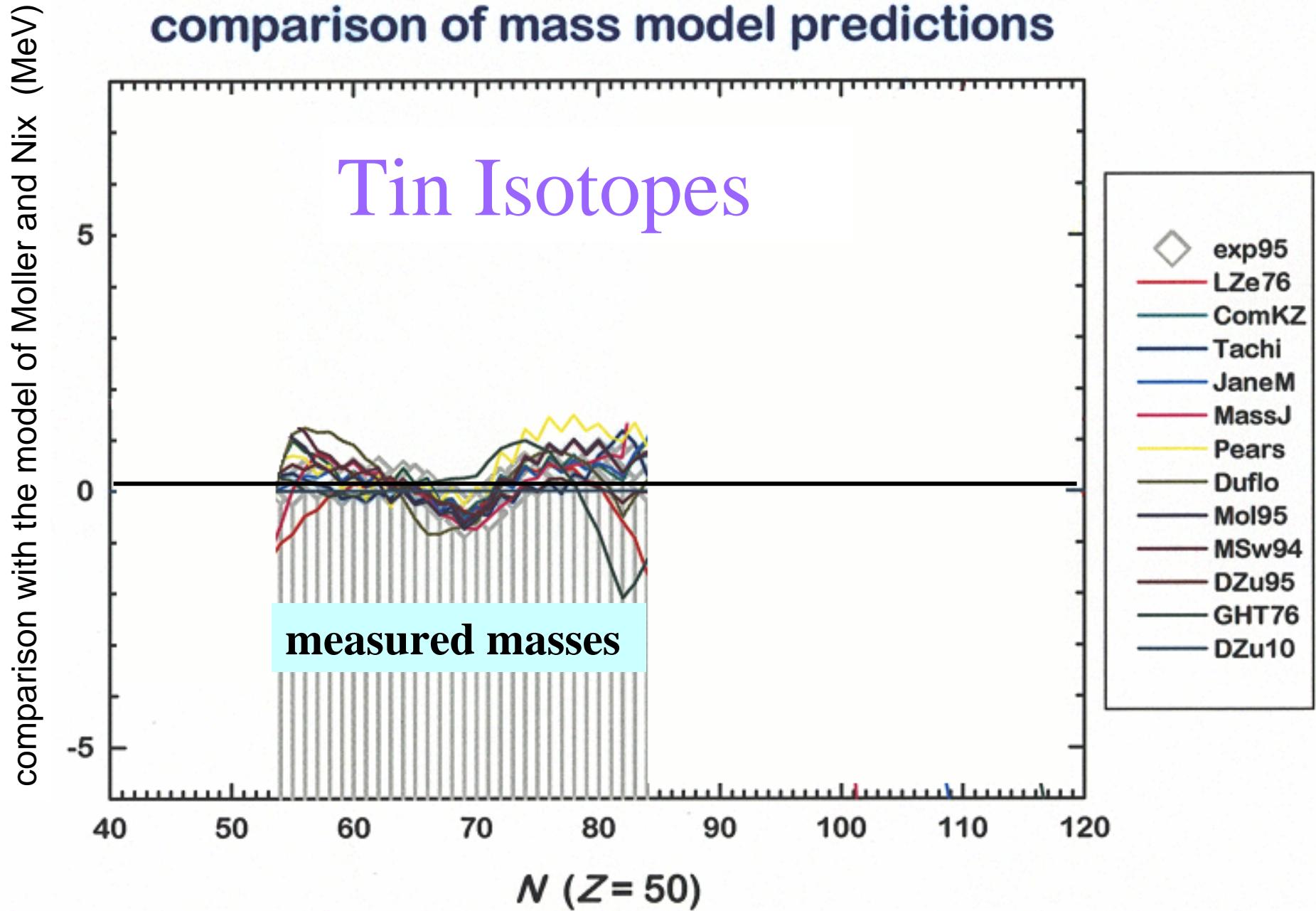
Development of exotic beams since 25 years

+

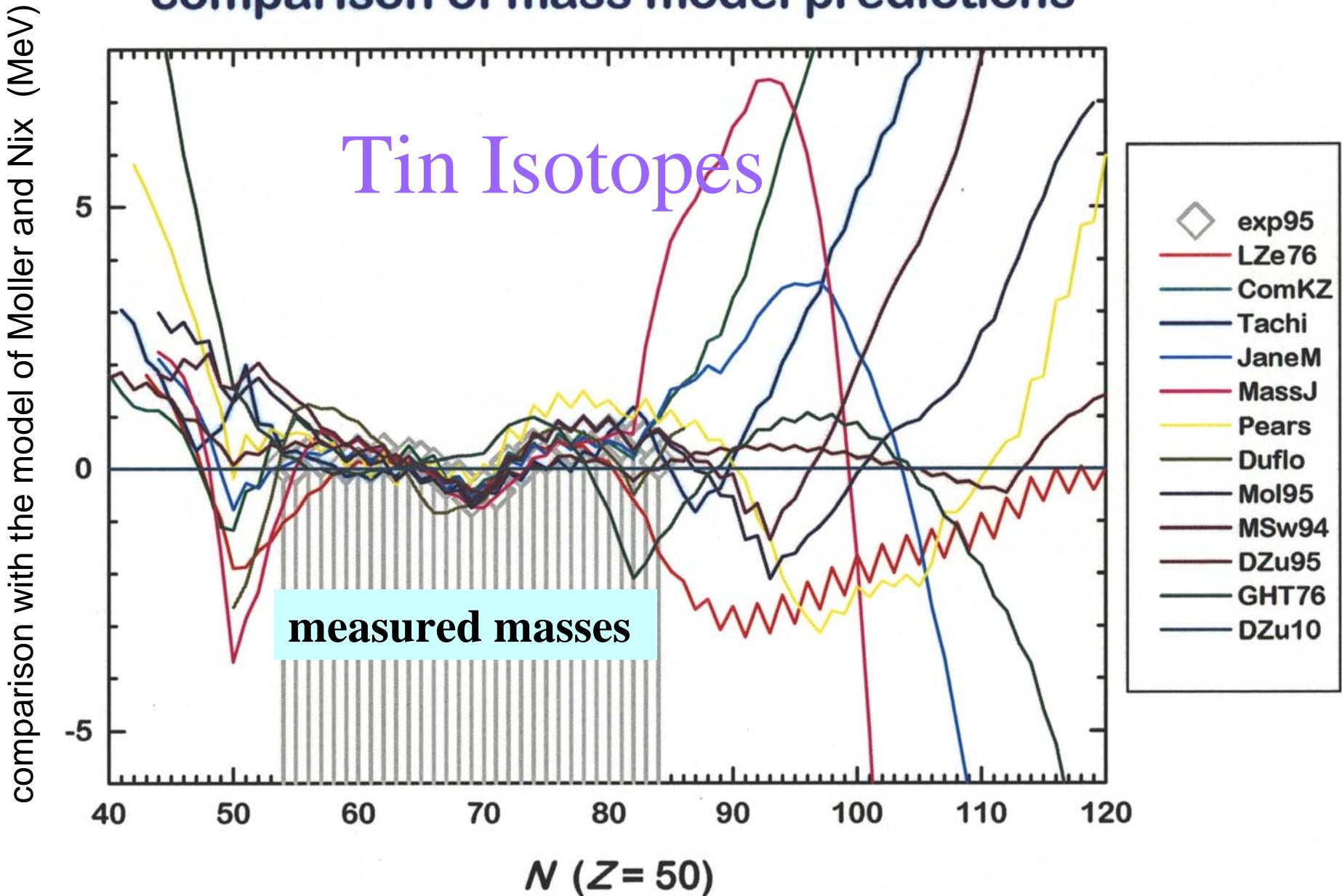
Development of new experimental devices

comparison of mass model predictions

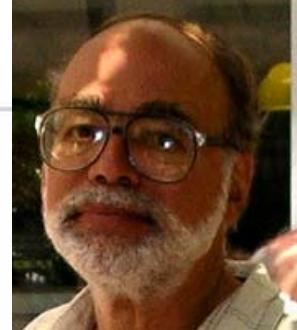
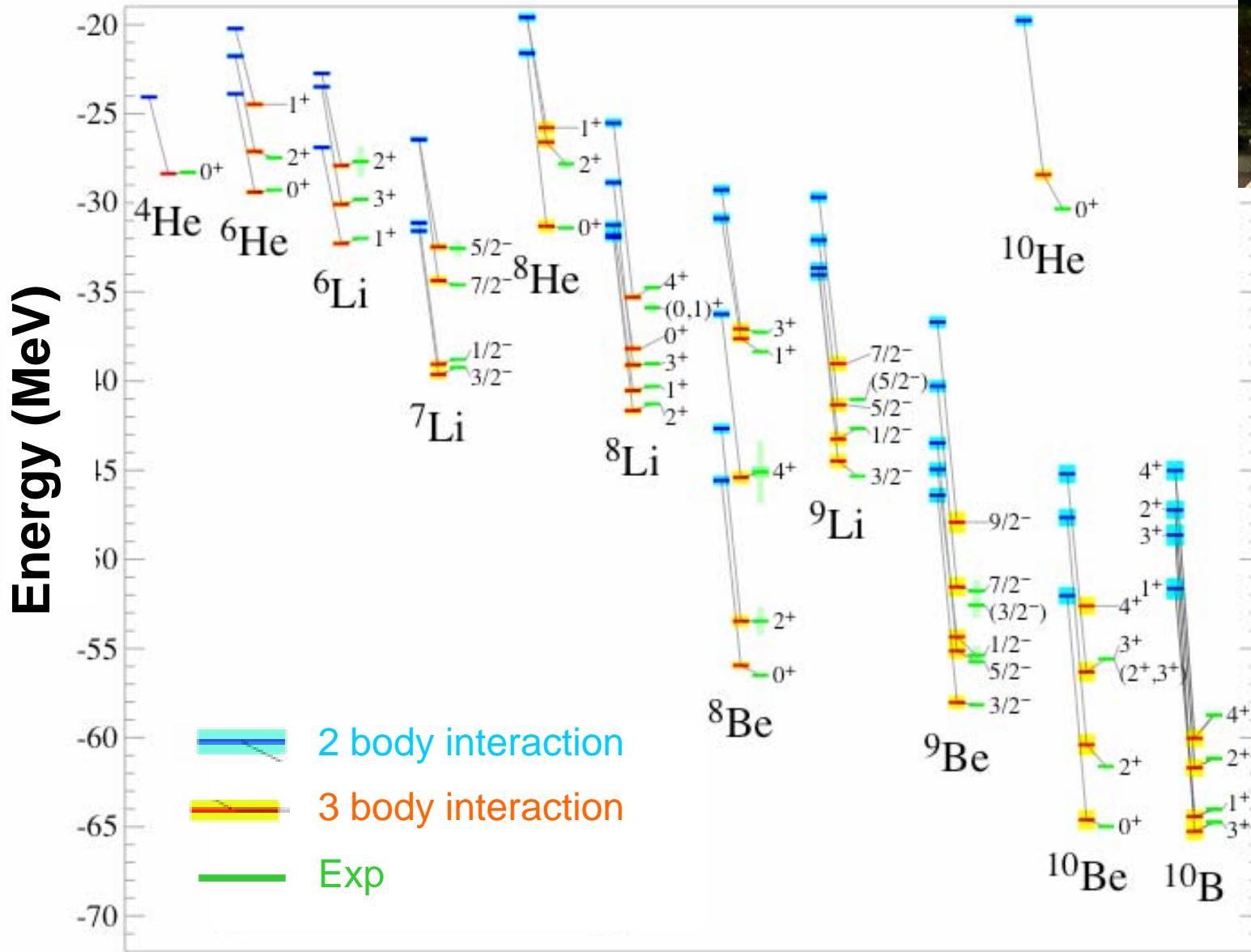
Tin Isotopes



comparison of mass model predictions

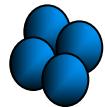


Binding energies of ground states and of the first excited states



S. Pieper

4n ?



Predictions for a 4-neutron system

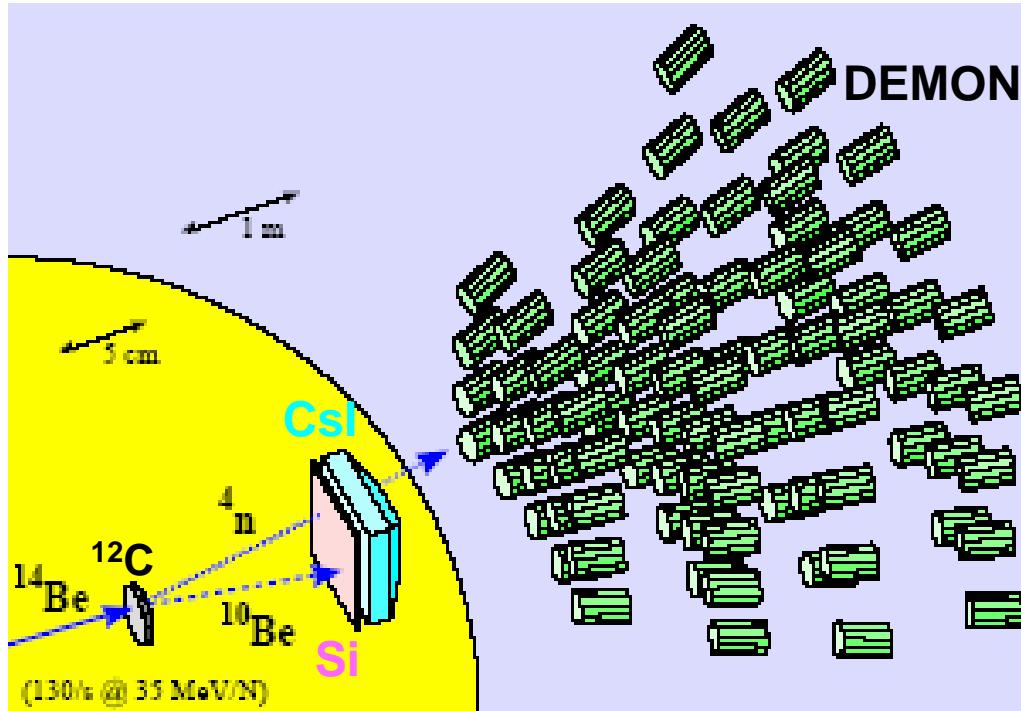
a lot of experiments since the 60's try to probe or not
the existence of a tetraneutron .

" I show that it does not seem possible to change modern nuclear Hamiltonians to bind tetraneutron without destroying many other successful predictions of those Hamiltonians.

This means that, should a recent experimental claim of a bound tetraneutron be confirmed, our understanding of nuclear forces will have to be significantly changed. "

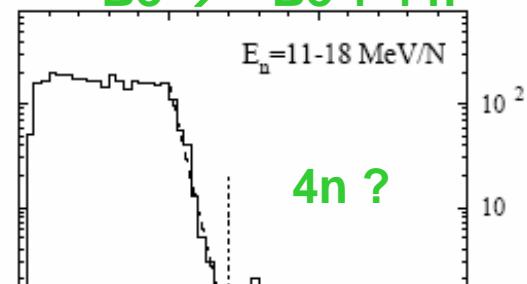
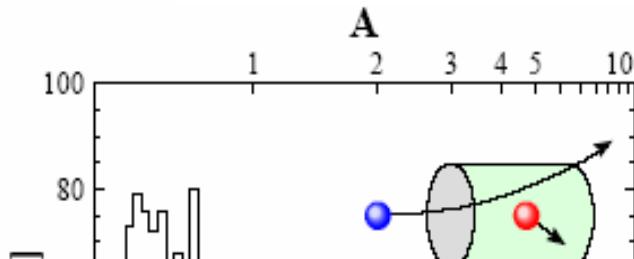
“Extract” neutron clusters

$$\blacktriangleright |^{14}\text{Be}\rangle \equiv a|^{10}\text{Be} + ^4\text{n}\rangle + \dots$$



- ▷ effective + clean + sensitive !!!
- ▷ technique similar to Chadwick's (1932) !
- ▷ saturation (sensitive to low E_p) ...

The ^{14}Be break-up experiment



4n = The quest of the holy Graal for physicists
in structure !

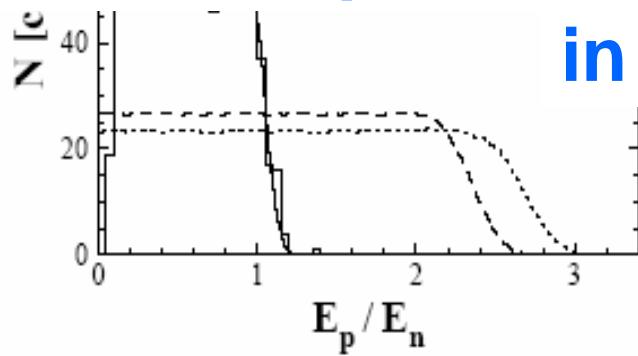


FIG. 2: Distribution of the ratio of proton energy, E_p (MeV), to the energy derived from the flight time, E_n (MeV/N), for data from the reaction $\text{C}(^{14}\text{Be}, ^{12}\text{Be} + \text{n})$ (histogram) and for simulations of elastic scattering of $^{1,3,4}\text{n}$ (solid, dashed and dotted lines, respectively) on protons. The experimental resolution has been included in the simulations.

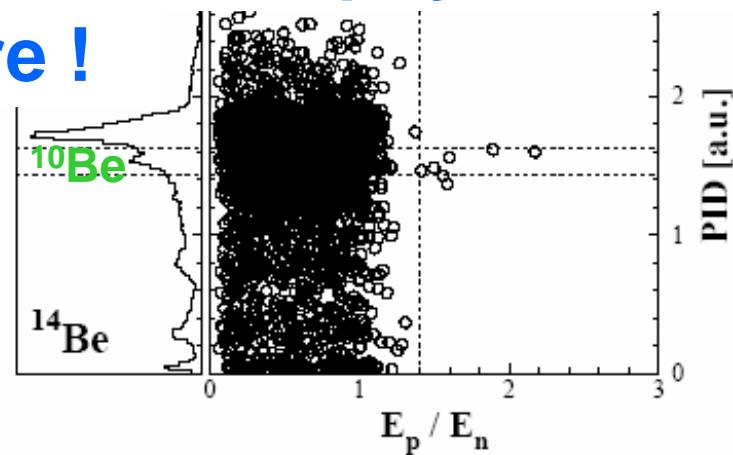


FIG. 5: Scatter plot and the projections onto both axes of the particle identification parameter PID defined in Eq. (1) vs E_p/E_n for the data from the reaction $\text{C}(^{14}\text{Be}, \text{X} + \text{n})$. The PID projection is displayed for all neutron energies. The dotted lines correspond to $E_p/E_n = 1.4$ and to the region centred on the ^{10}Be peak.

Tools for structure studies

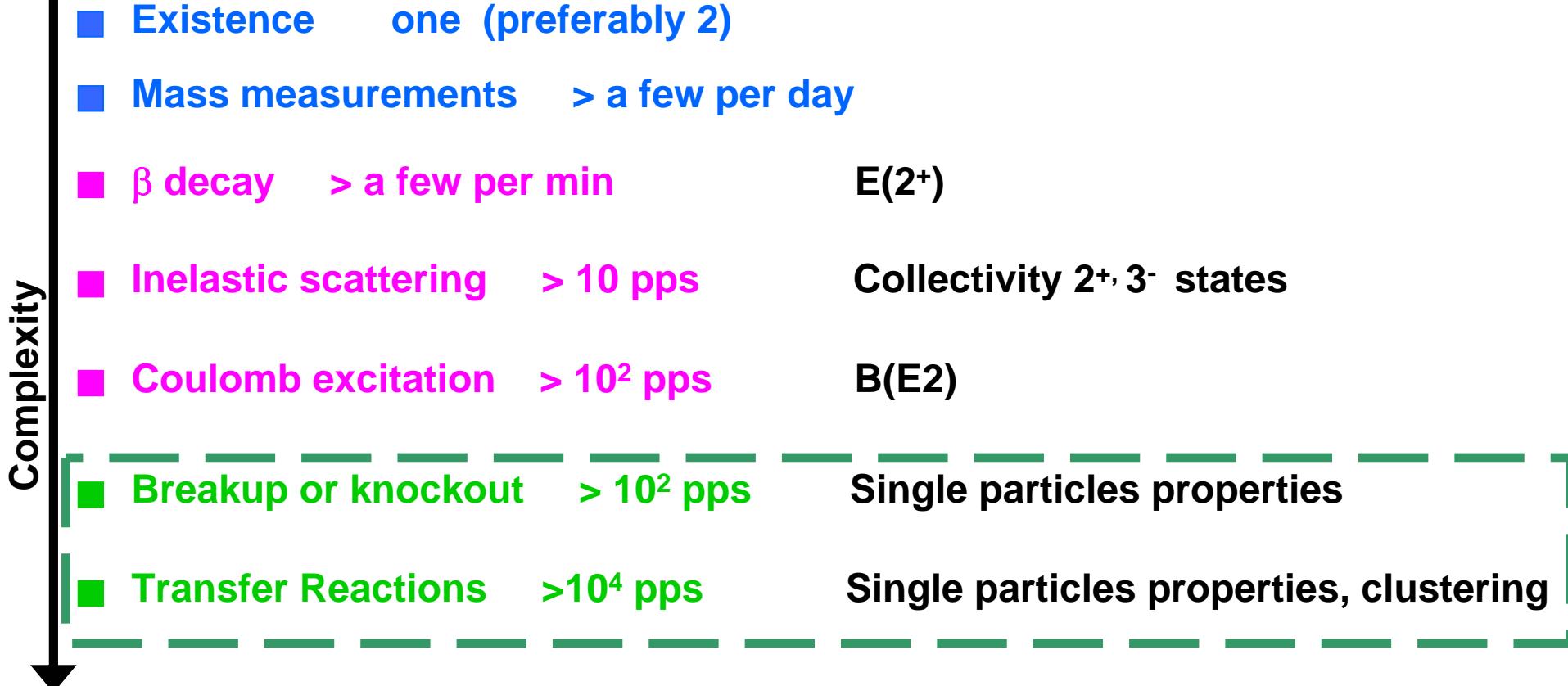
- Different ways to study the same problem !
ex: shell closures with mass measurements, inelastic scattering, coulex, transfer reactions etc....

BUT

- Different ways to confirm a new feature !
one information --> one piece of the puzzle in structure
+ complementary informations

- Tools depends on the beam energy and intensity

Tools for structure studies



Energy regimes

< 5 MeV/nucleon

REX-ISOLDE

5-70 MeV/nucleon

GANIL SISSI-SPIRAL

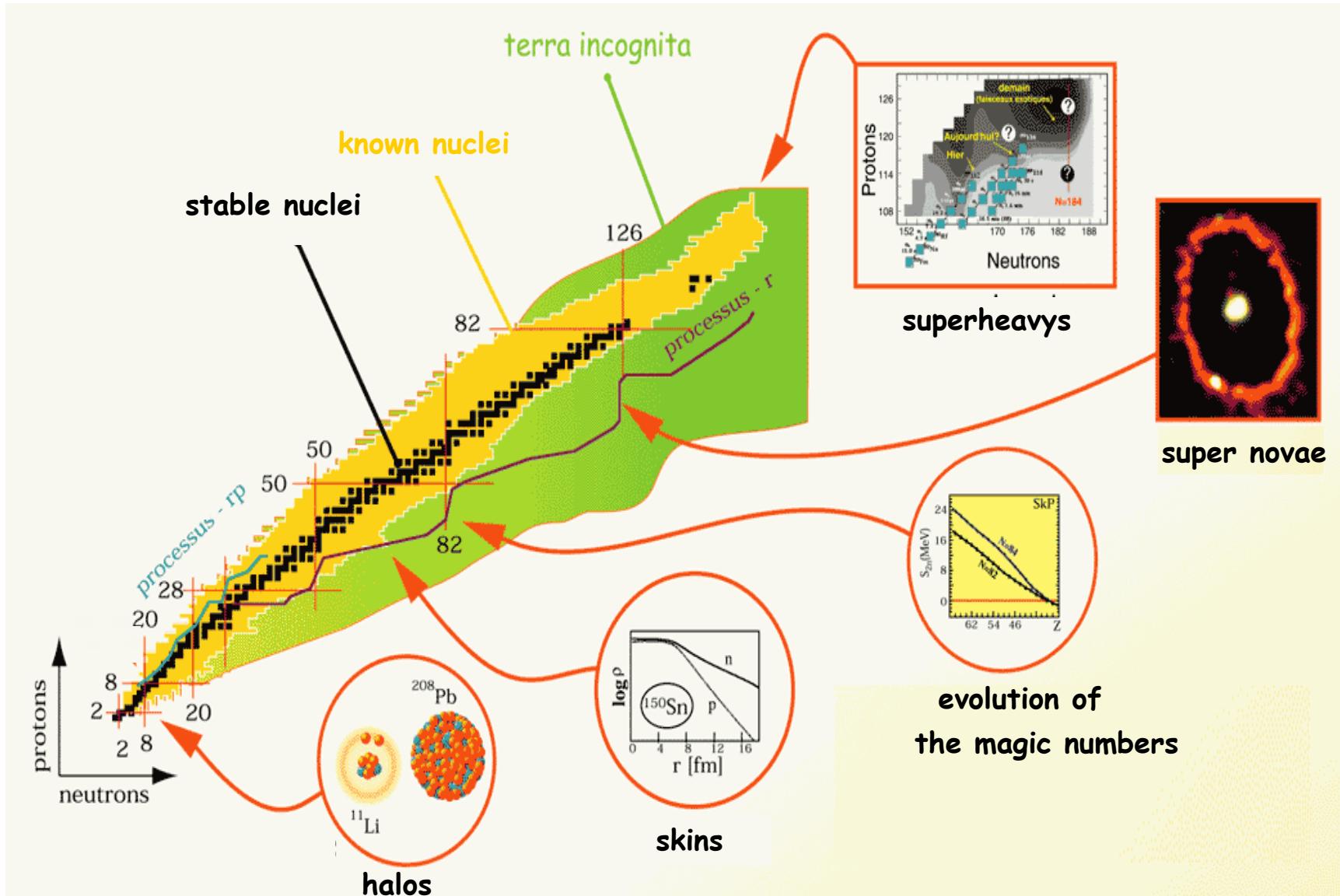
100-1000 MeV/nucleon

GSI-FRS

Transfer

knockout

Nuclear structure at the driplines



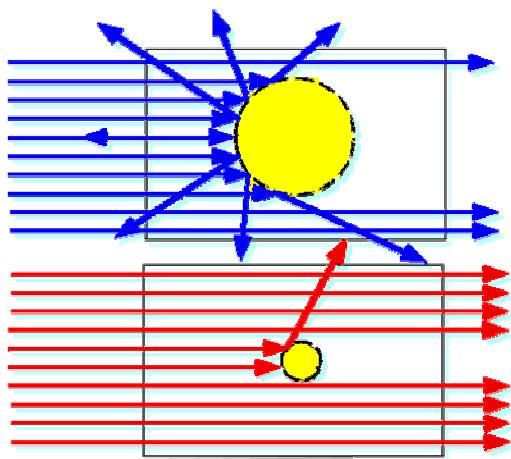
Halo nuclei

Halo nuclei

Exotic nuclei anormally big

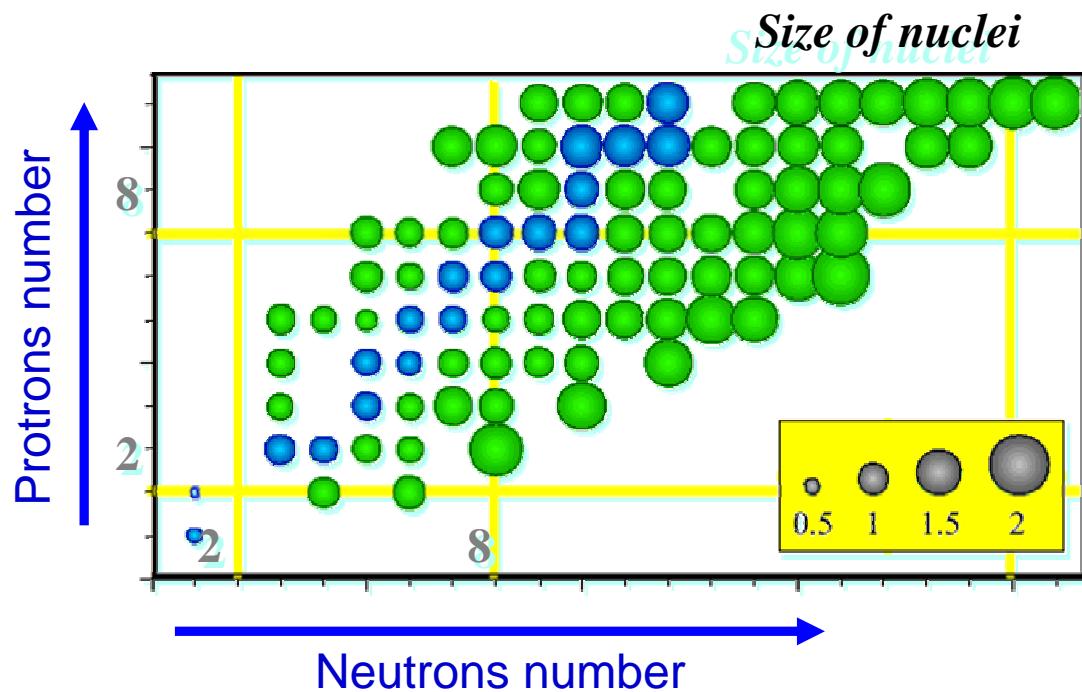
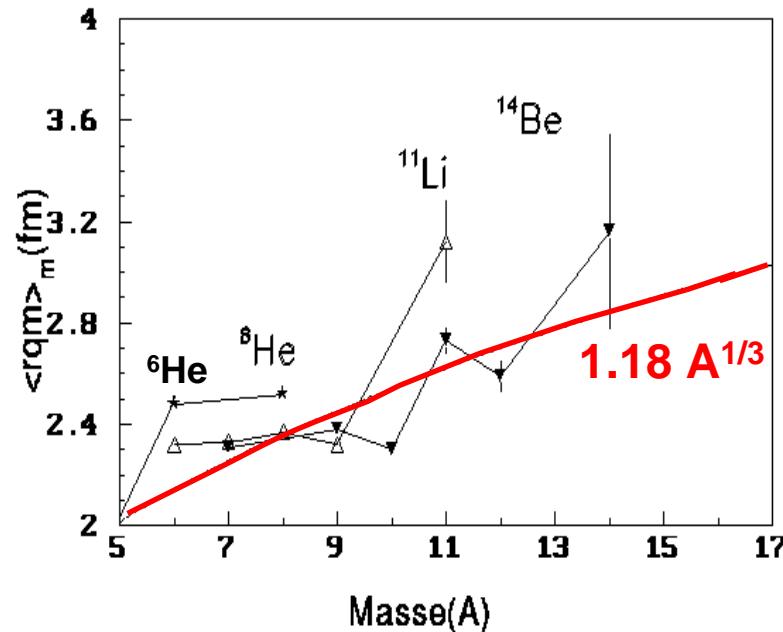
Measurement of reaction cross sections

I. Tanihata et al., Phys. Rev. Lett. 55 (1985) 2676

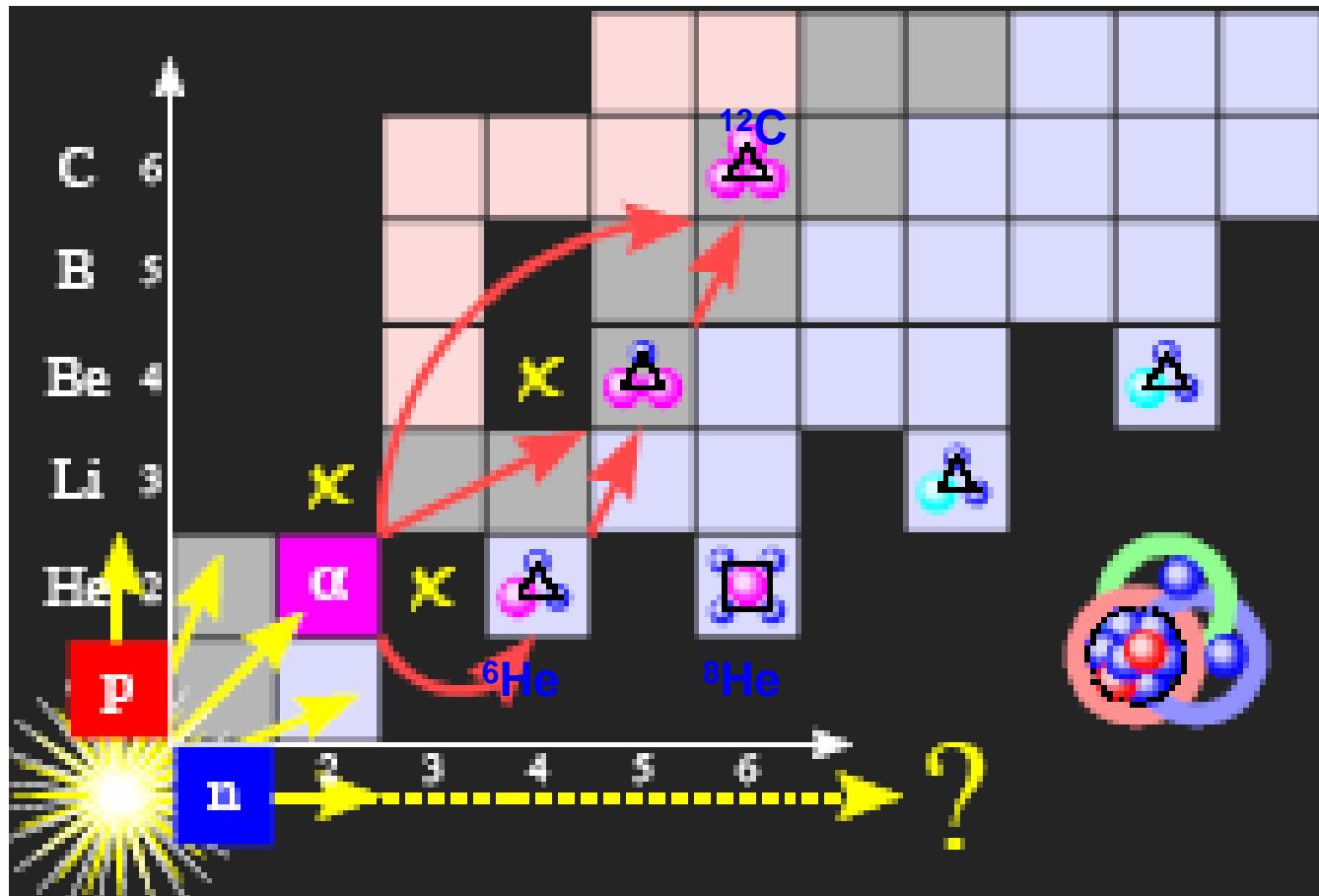


Rutherford's experiment

$$\sigma_R = \pi (R_{\text{proj}} + R_{\text{target}})^2$$



Halo nuclei



Heisenberg's principle

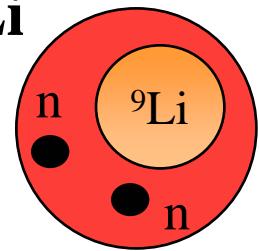
$$\Delta x \Delta p \geq \hbar$$

^{22}C , ^{17}Ne borromean

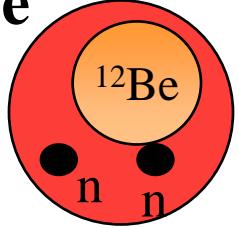
^{17}B , ^{19}C , ^8B one neutron, one proton halo

Borromean

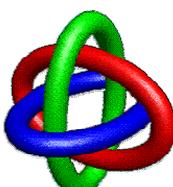
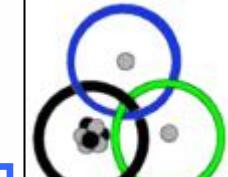
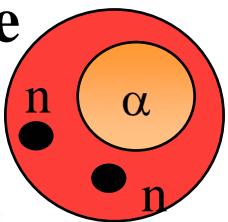
^{11}Li



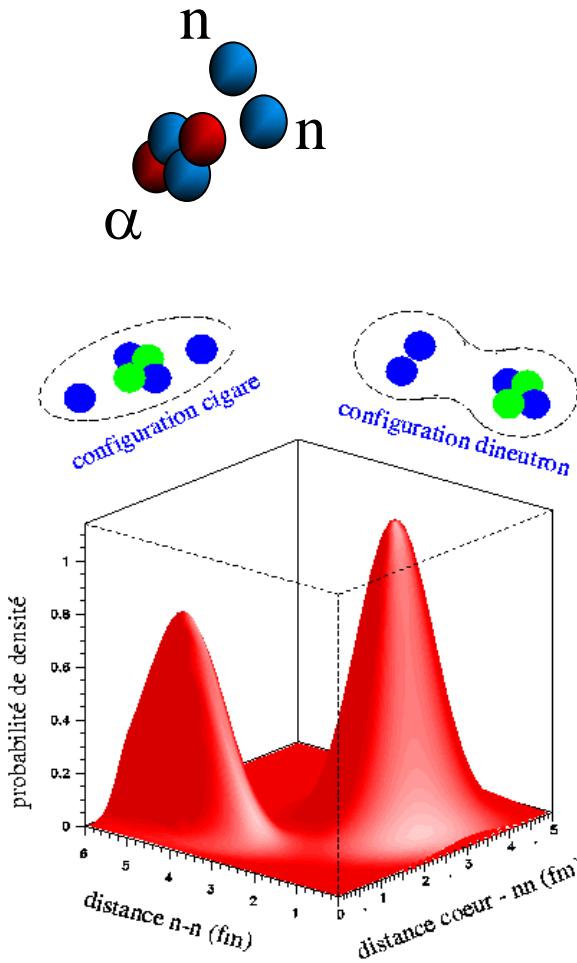
^{14}Be



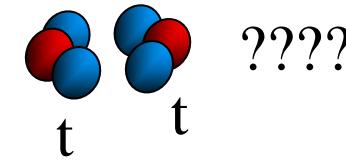
^6He



Ground state wave function of ${}^6\text{He}$



M. Zhukov et al. Phys. Rep. 231 (1993) 151



- ⬇ ${}^6\text{He}$ binding energy well reproduced with a $t+t$ configuration

A. Csoto, PRC 48 (1993) 165

- ⬇ Microscopic calculations

$\langle {}^6\text{He}|{}^4\text{He} + \text{n} + \text{n} \rangle$ 1.10 to 1.56

$\langle {}^6\text{He}|t + t \rangle$ 0.44 to 1.77

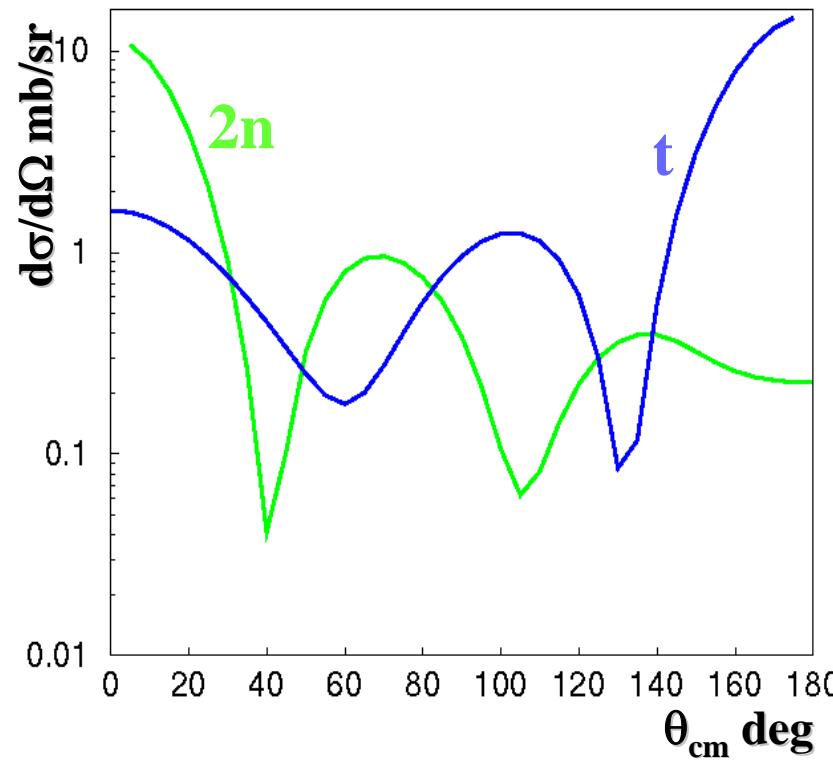
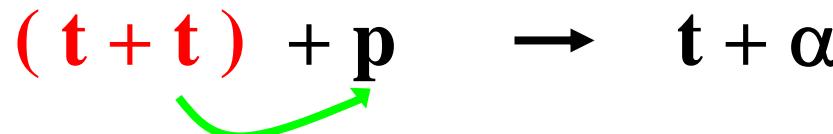
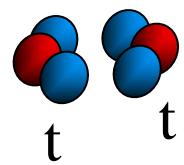
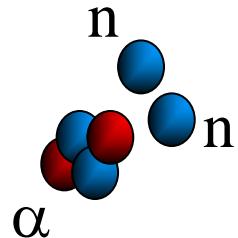
Yu. F. Smirnov, PRC 15 (1977) 84

K. Arai et al., PRC 59 (1999) 1432

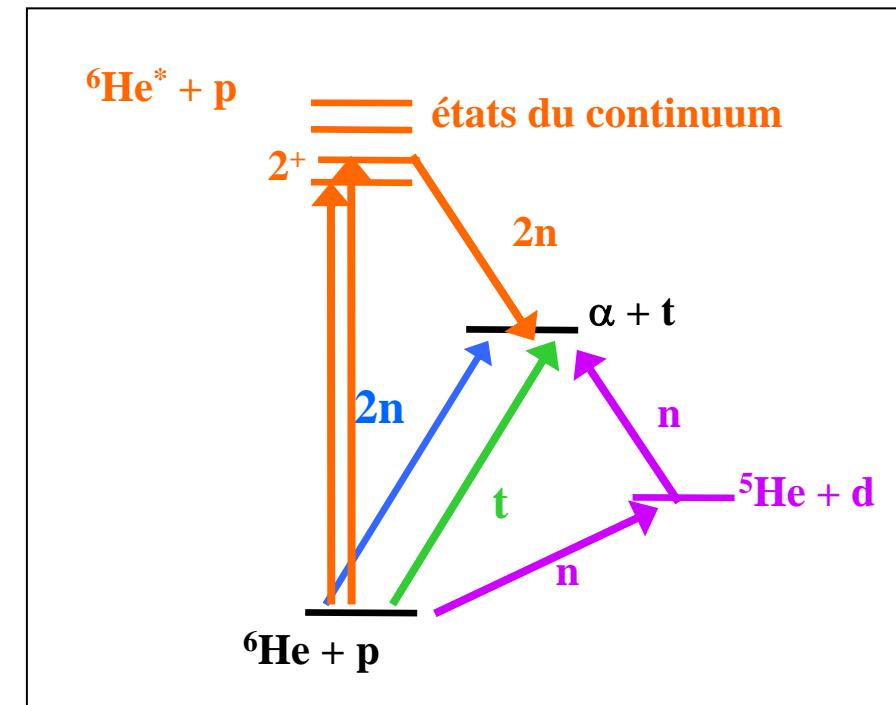
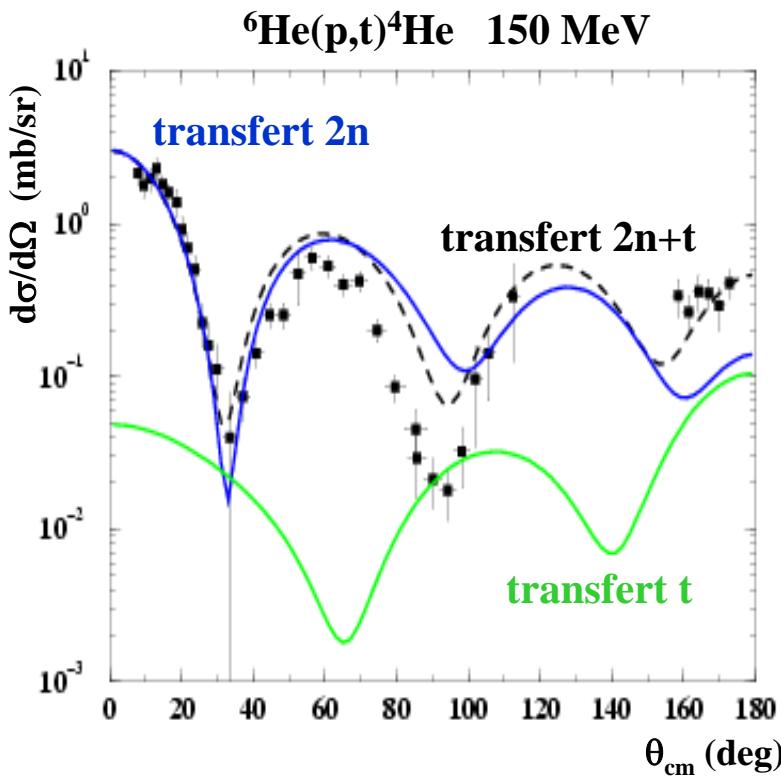
- ⬇ Analogy with ${}^6\text{Li}$

${}^6\text{Li}(p, {}^3\text{He})\alpha$

clusters $\alpha+d$ and ${}^3\text{He}+t$
same importance !!



Ground state wave function of ${}^6\text{He}$



Coupled channels calculations

Search for t+t clustering in ${}^6\text{He}$
L.G et al., NPA, 378 (2004) 426c

Investigation of ${}^6\text{He}$ cluster structures
L.G et al., accepted in PRC

t+t exist but very small !!

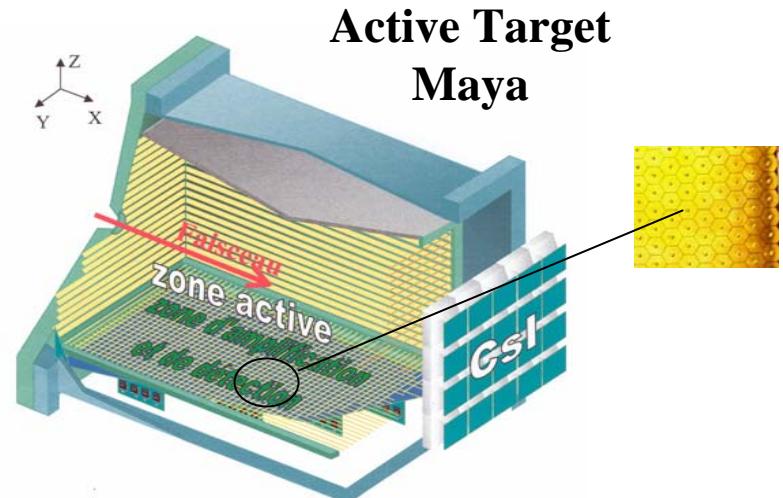
Ground state wave function of ${}^8\text{He}$

- ◆ ${}^6\text{He}(2^+)$ is predominant in the ${}^8\text{He}_{g.s}$ wave function

${}^6\text{He}(2^+)$:	66%
${}^6\text{He}_{g.s.}$:	33%

${}^8\text{He}(\text{p},\text{t}){}^6\text{He}_{g.s.}$, ${}^8\text{He}(\text{p},\text{t}){}^6\text{He}_{2+}$
@ 60 MeV, Riken

A. Korsheninnikov, PRL 90 (2003) 082501



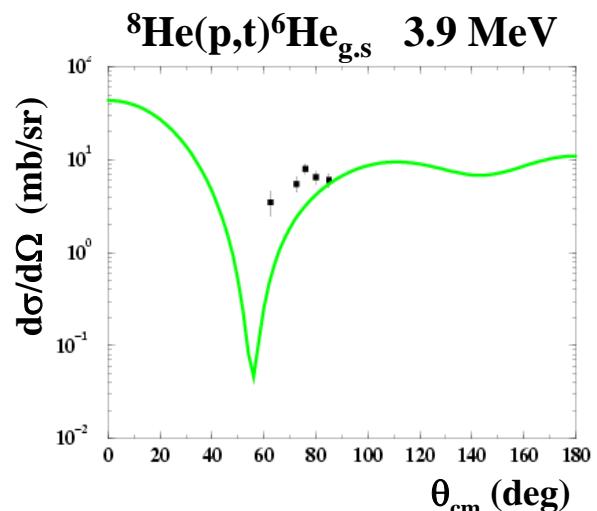
@ 3.9 MeV, GANIL/SPIRAL with MAYA

lower energy \longrightarrow higher cross sections

but optical potentials ?

compound nuclei ?

${}^6\text{He}(2^+)$, ${}^6\text{He}_{g.s.}$ same weight than Riken



W. Mittig, Ch. E Demonchy thesis

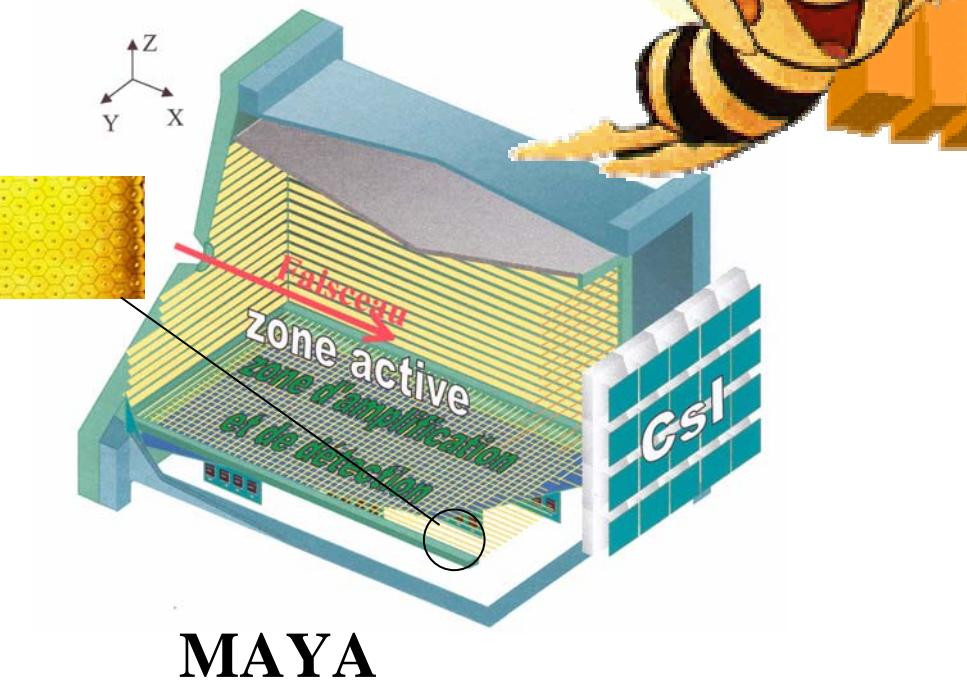
Actar Project: GSI involved

- detection gaz
also used as a target
- ✓ very efficient
- ✓ Low detection threshold for particles
- ✓ used as a thick target
- ✓ Large angular acceptance
- ✓ Important reaction energy range

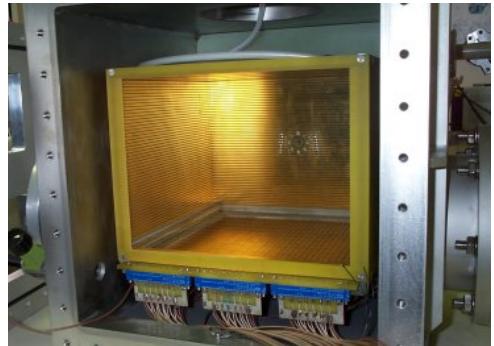
■ Experiment

- elastic resonance scattering
- $$^8\text{He} + \text{p} \longrightarrow \text{IAS of } ^9\text{He}$$
- $^{26}\text{F}(\text{d}, ^3\text{He})^{25}\text{O}$

Active Target



MAYA



W. Mittig, C.E. Demonchy et al., GANIL

Molecular states

Ne

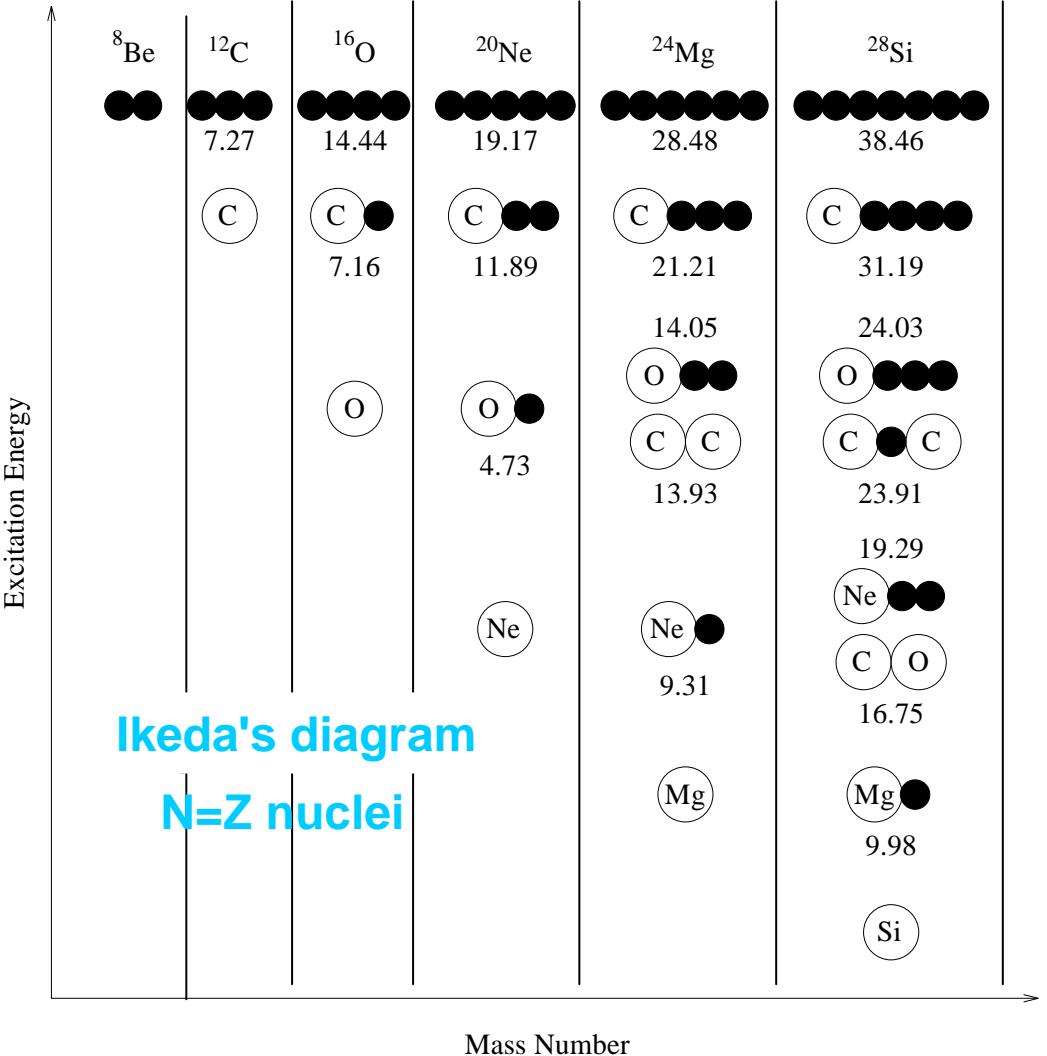
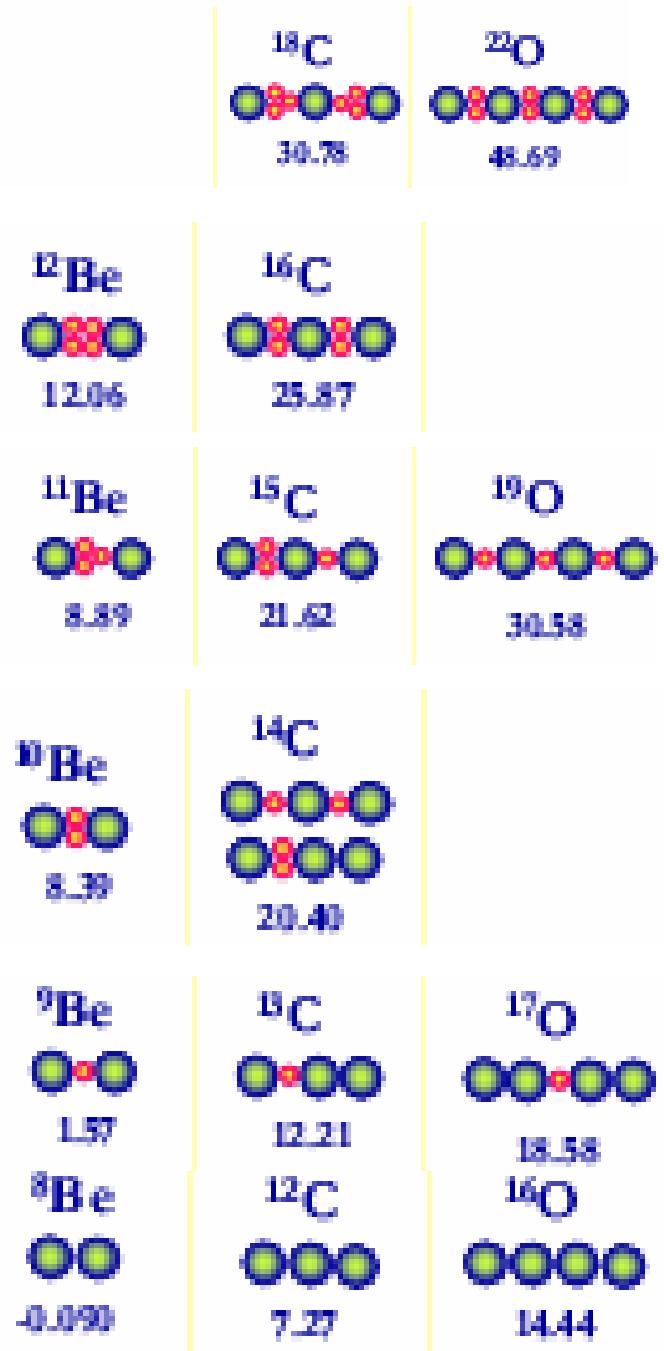
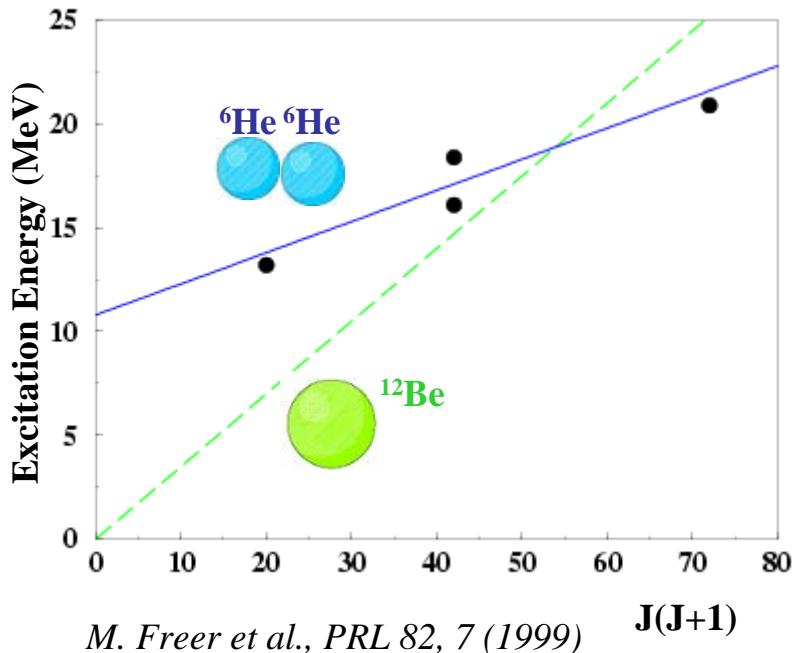


FIG. 1: The Ikeda threshold diagram for nuclei with α -clustering. Cluster structures are predicted to appear close to the associated decay thresholds. The energies needed for the decomposition of the normal nucleus into the structures are indicated in MeV (from [127]).



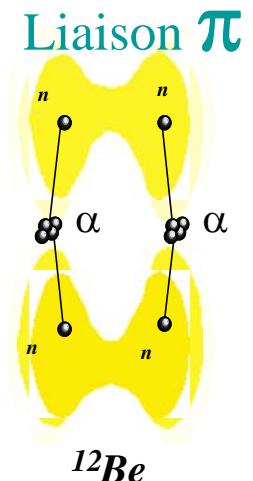
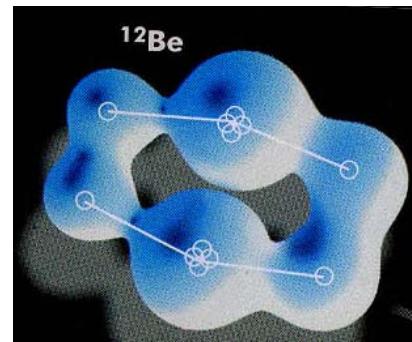
New Structures

- Inelastic Experiments

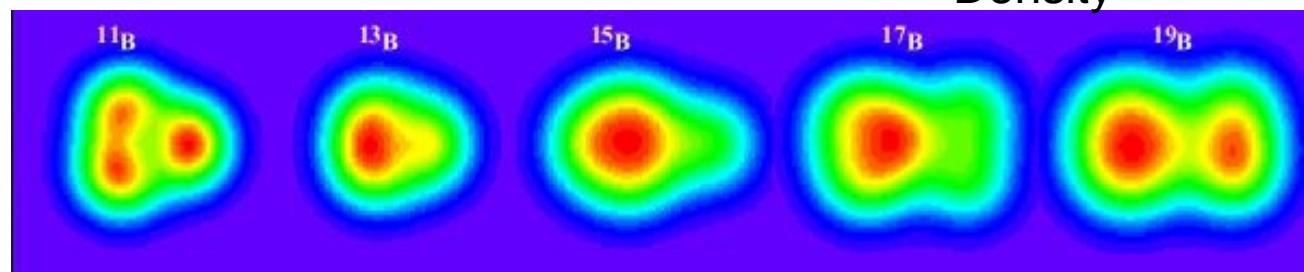


M. Freer et al., PRL 82, 7 (1999)

$J(J+1)$



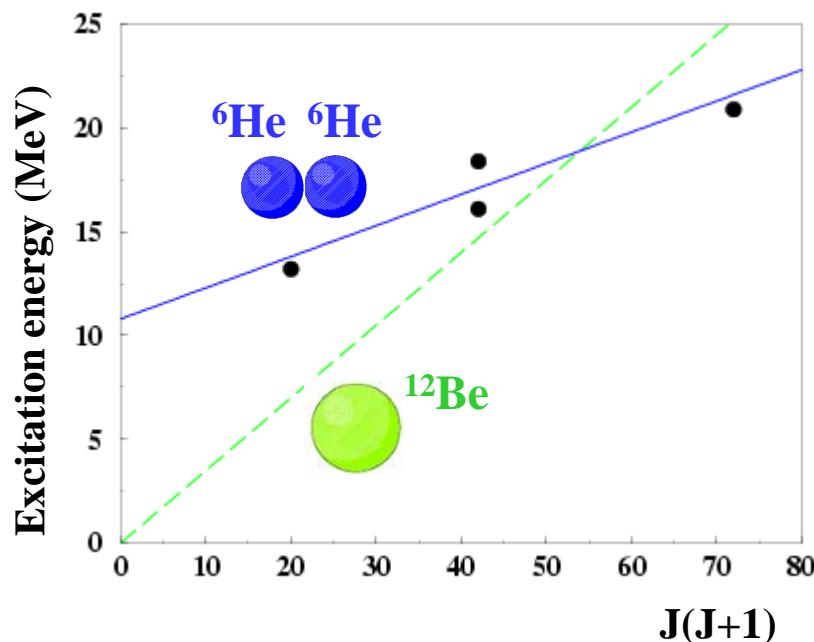
Density



AMD calculations Kanada-Enyo, Horiuchi et al.

Inelastic scattering

Clustering of excited states

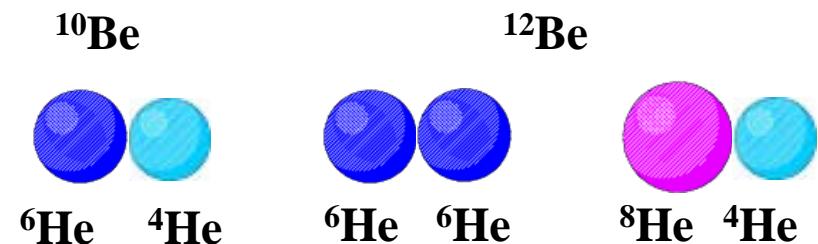


M. Freer et al., PRL 82, 1383 (1999)

Knockout

Test of a new method

Clustering in the ground state



Collaboration CHARISSA:

N. Orr, M. Marques, LPC Caen

F. Carstoiu, Univ. de Bucharest

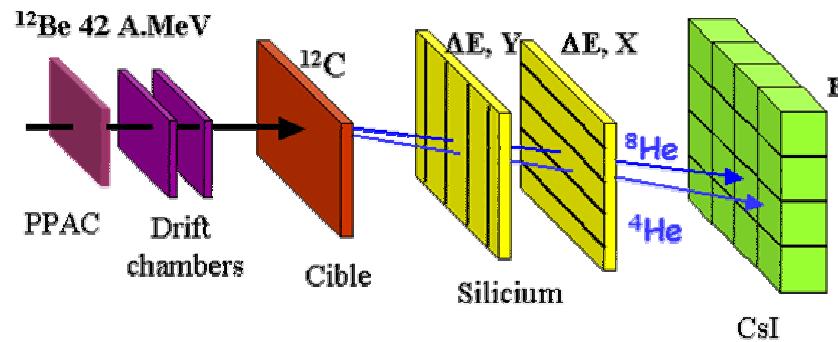
M. Freer, Univ. de Birmingham

Molecular states of $^{10,12}\text{Be}$

- Analogy with one nucleon knockout

Momentum distribution $p \rightarrow l$

$\sigma_{\alpha} \rightarrow \text{Spectroscopic factor}$



Molecular states of $^{10,12}\text{Be}$

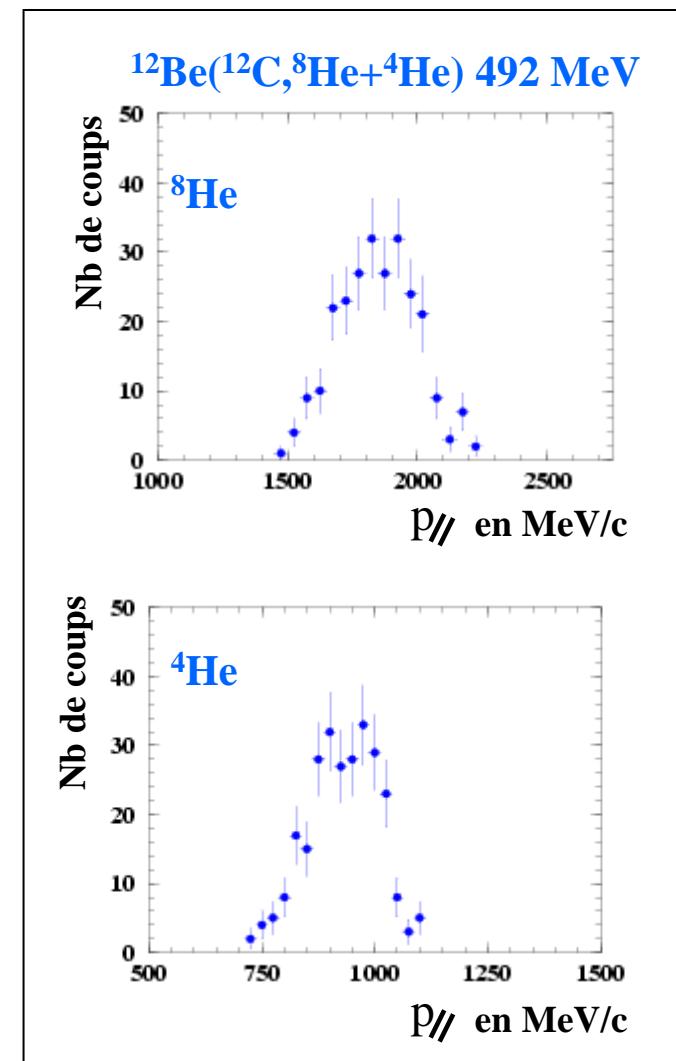
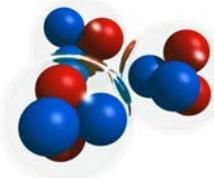
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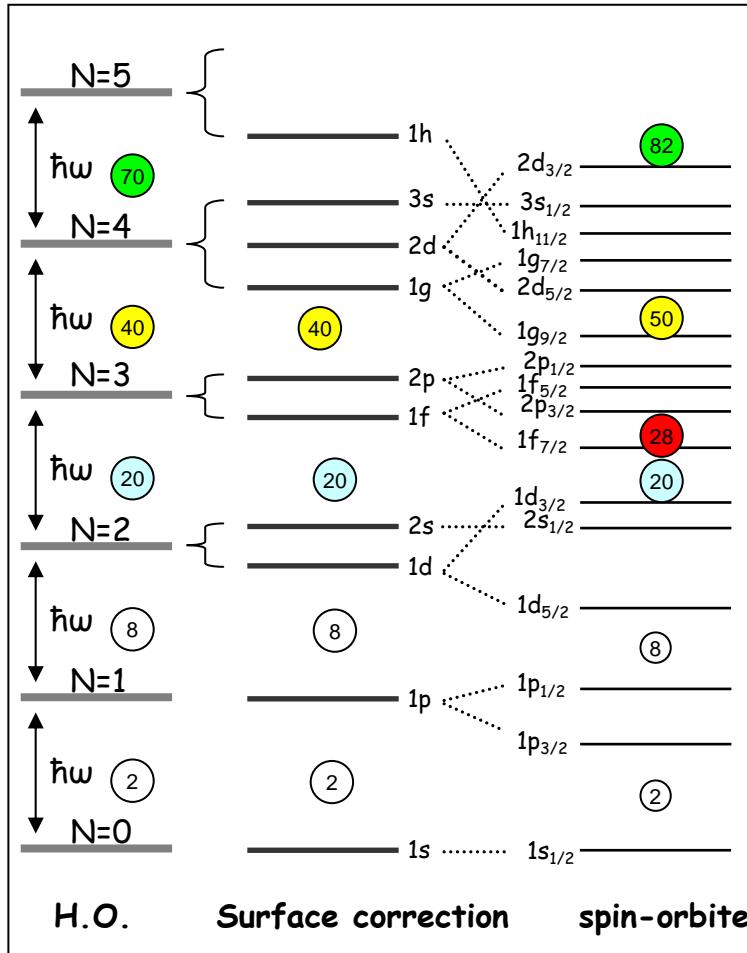
Theory under progress
Comparison with a Glauber's model

- Test october 2005



Shell evolution

Shell model



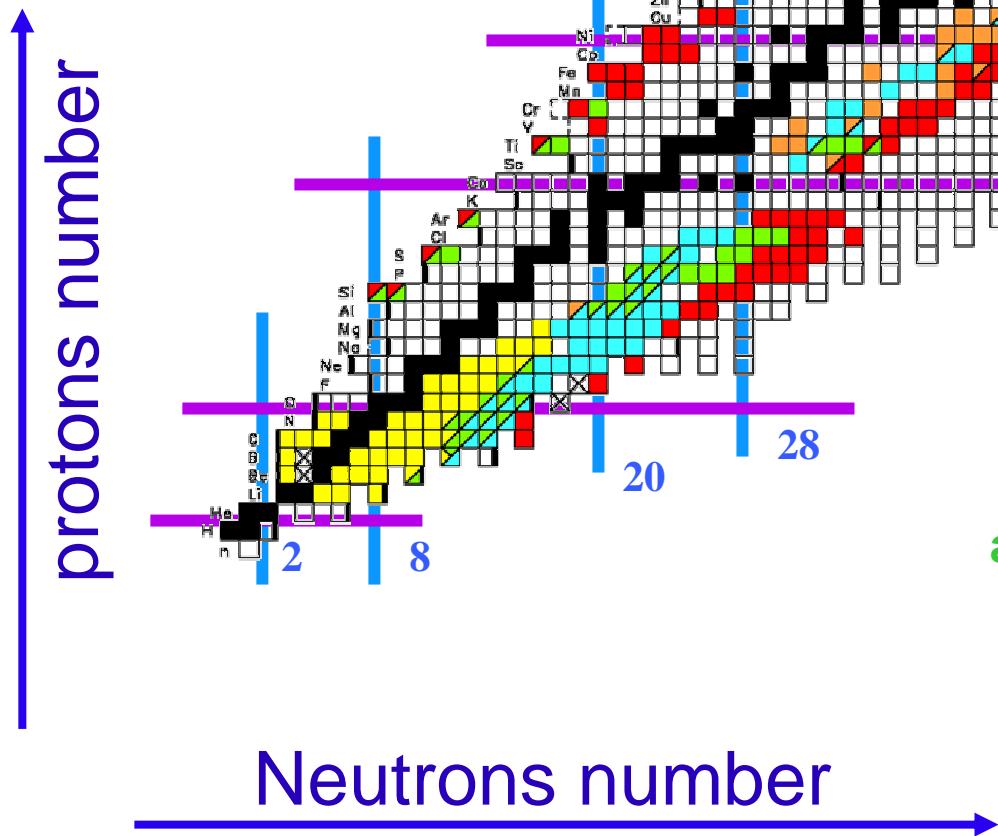
- Shell model (~1950):

- Nucléon = independant particle move in an average potential created by the ensemble of the other nucleons
- Reproduces many properties of the nuclei
- Magic numbers : (2,8,20,28,50,82,...)

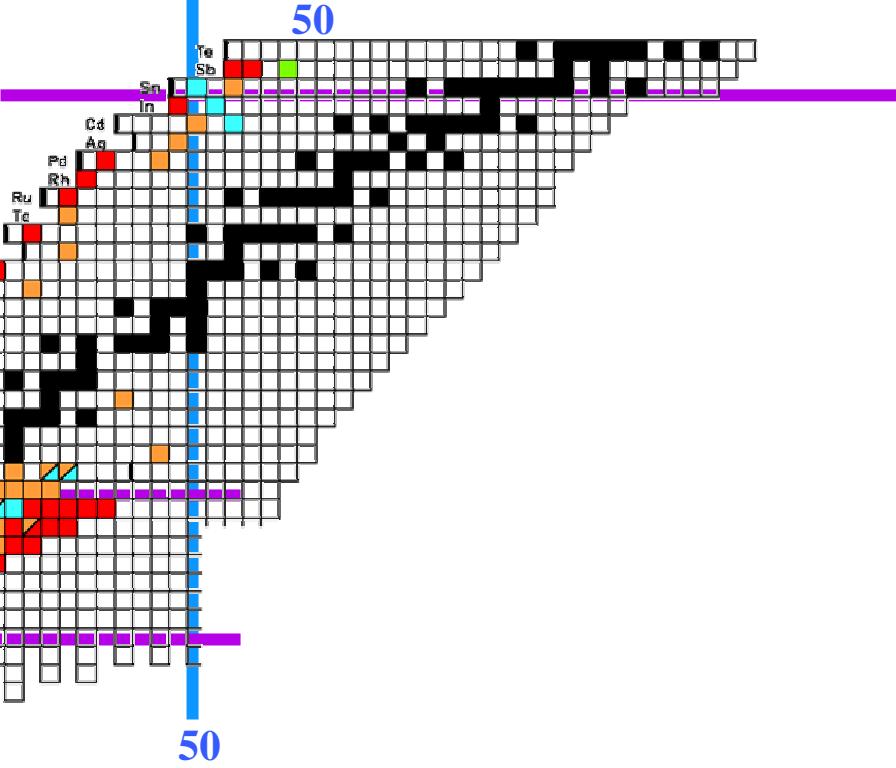


J. Hans D. Jensen Maria Goeppert Mayer
 Discovery of the magic numbers
 Nobel prize 1963

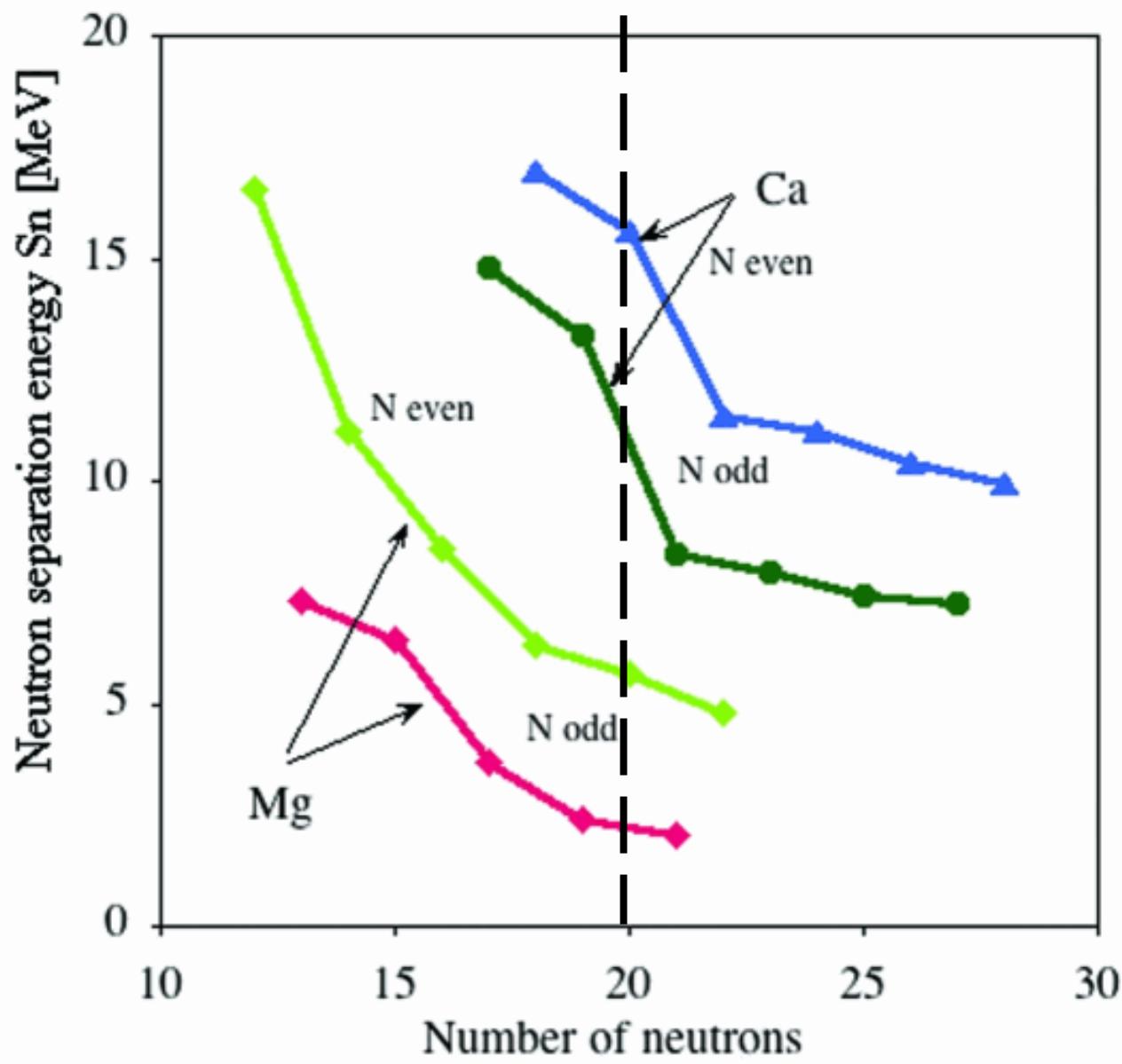
Magic Numbers



Weakening of shell $N=20, 28$
already observed far from stability



N = 20



New magic numbers

- $V_{\sigma\tau}$ monopole interaction:

coupling of proton-neutron spin-orbit partners

but missing in n-rich nuclei

the spin orbit partner of the valence neutrons are not occupied by protons

- **N = 16 neutron proton interaction $\pi d5/2 - \nu d3/2$**

Experimental Evidence from

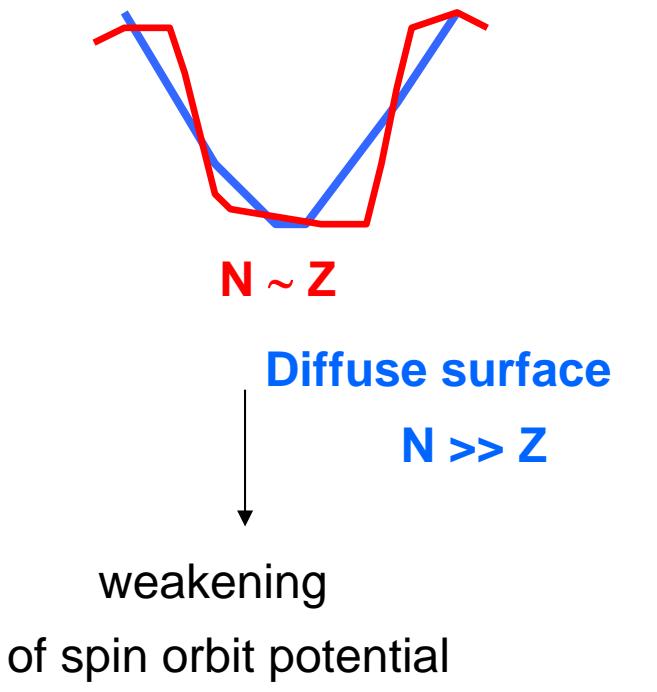
- in beam fragmentation, PRC 69 (2004) 034312
- longitudinum momentum distribution

^{28}O (N=20) ?

- **N = 34 neutron proton interaction $\pi f7/2 - \nu f5/2$**

Evolution of magicity with increasing N/Z

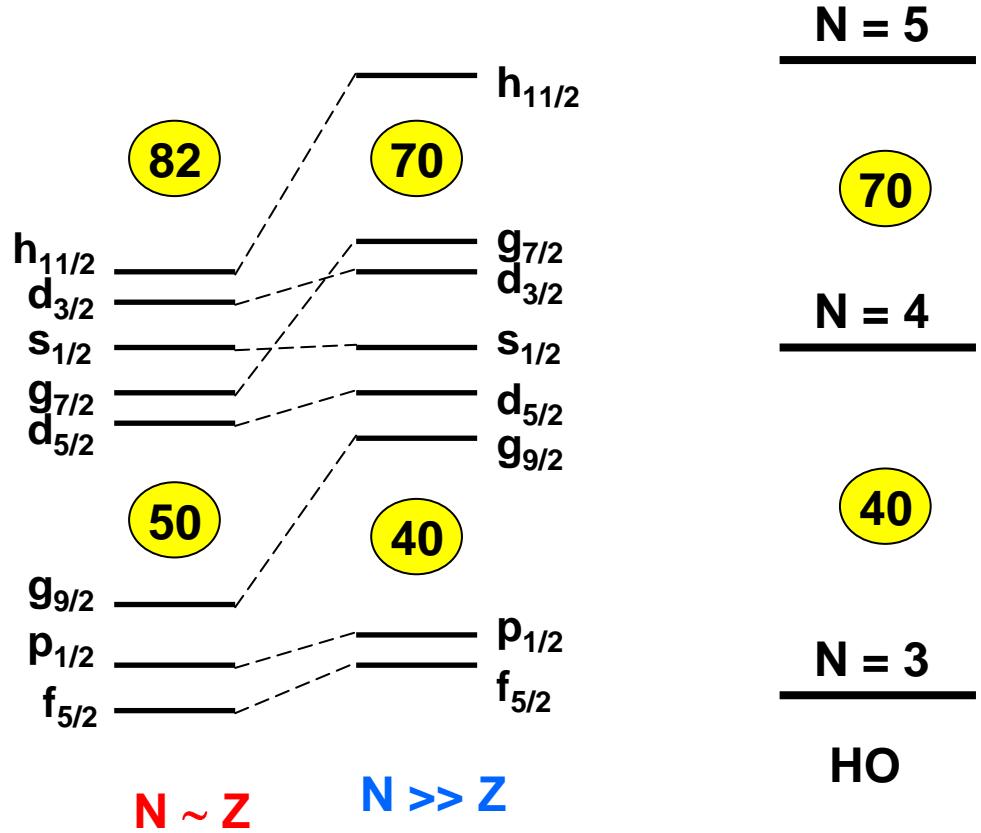
Study of Z magic nuclei: O, Ca, Ni, Sn isotopic chains



ex: ^{68}Ni (N=40)

B(E_2) small \rightarrow magic nuclei ?

O. Sorlin et al., PRL 88, 092501 (1994)



Dobaczewski et al., PRL 72, 981 (1994)

Shopping List of Nuclei

SPIRAL II, FAIR —————> **EURISOL**

$N = 16$ ^{24}O , ^{25}O , ^{25}F , ^{26}Ne

$N = 20$ all nuclei in the region of ^{32}Mg , called the magic inversion land

$N = 34$ $N = 40$

$Z = 20$ ^{48}Ca ^{54}Ca ^{60}Ca
 Calcium isotopes chain

$N = 40$ $N = 50$

$Z = 28$ ^{56}Ni ^{68}Ni ^{78}Ni
 Nickel isotopes chain

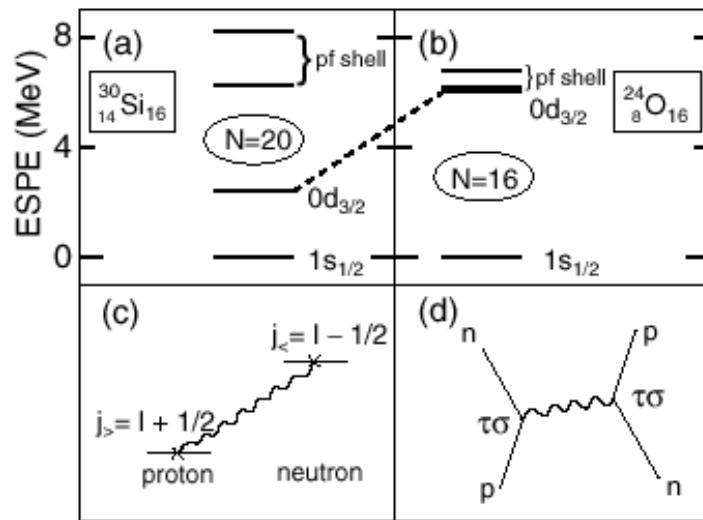
$N = Z = 50$ ^{100}Sn

Vladimir,

Is it so boring ?

Modification de la structure en couches loin de la stabilité

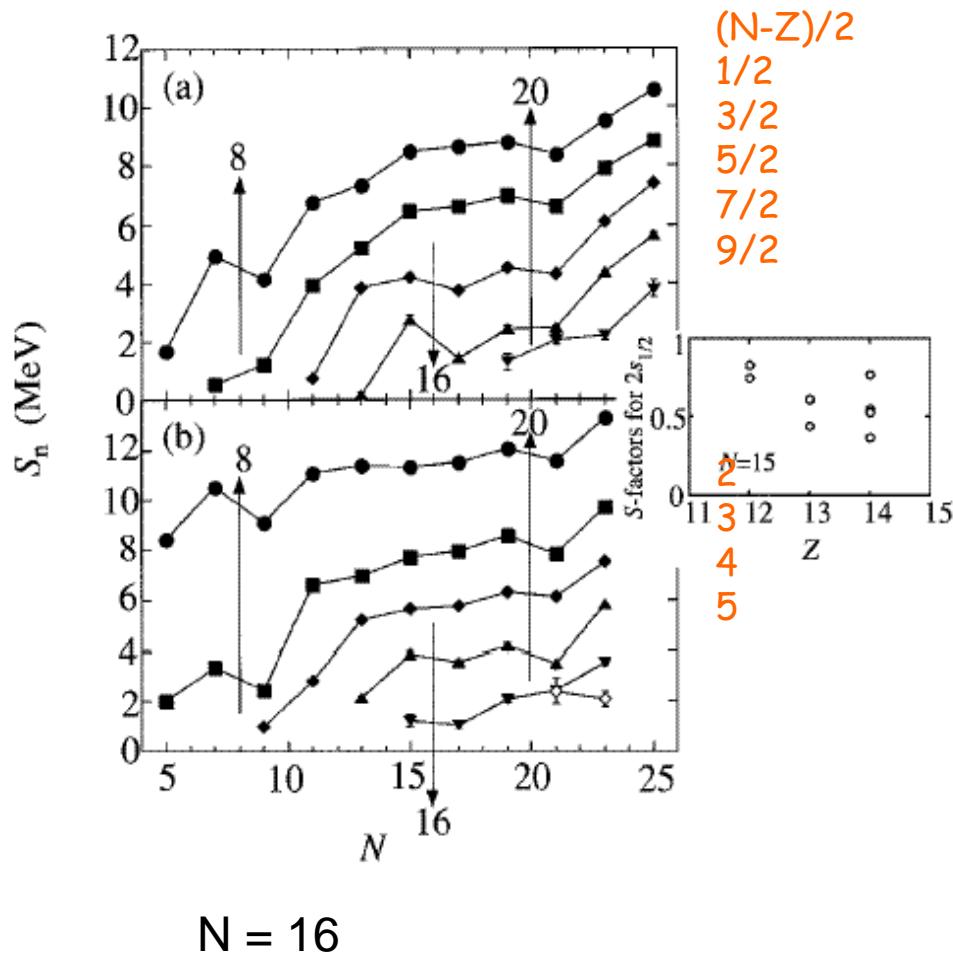
T. Otsuka et al., Phys. Rev. Lett. 87 (01) 082502



Observation complémentaire:
Augmentation des sections efficaces de réaction dans la même région de noyaux.

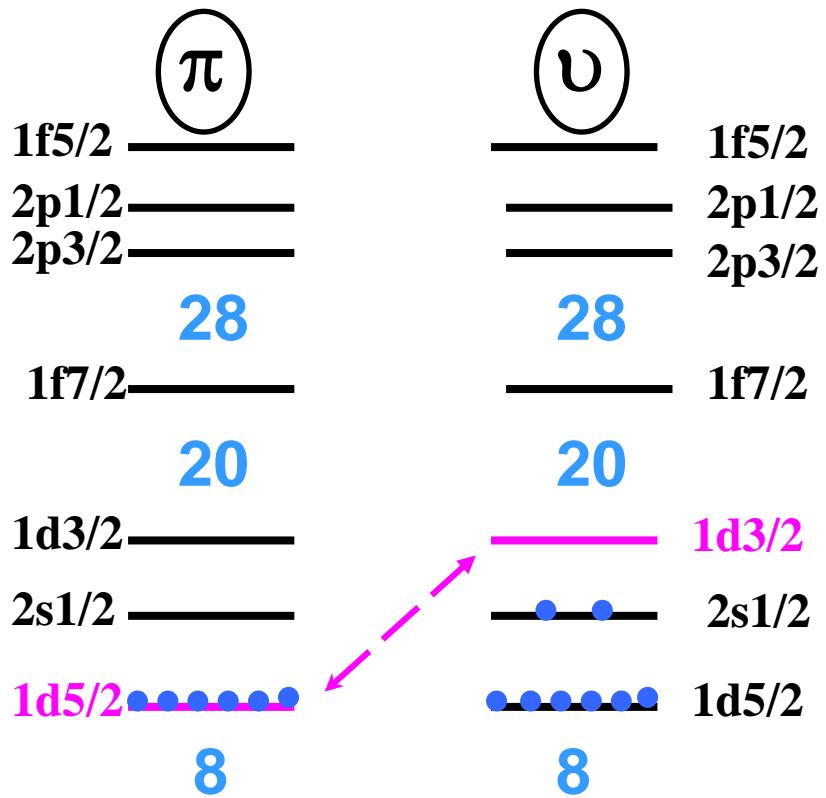
$$N = 34$$

A. Ozawa et al., Phys. Rev. Lett. 84 (00) 5493

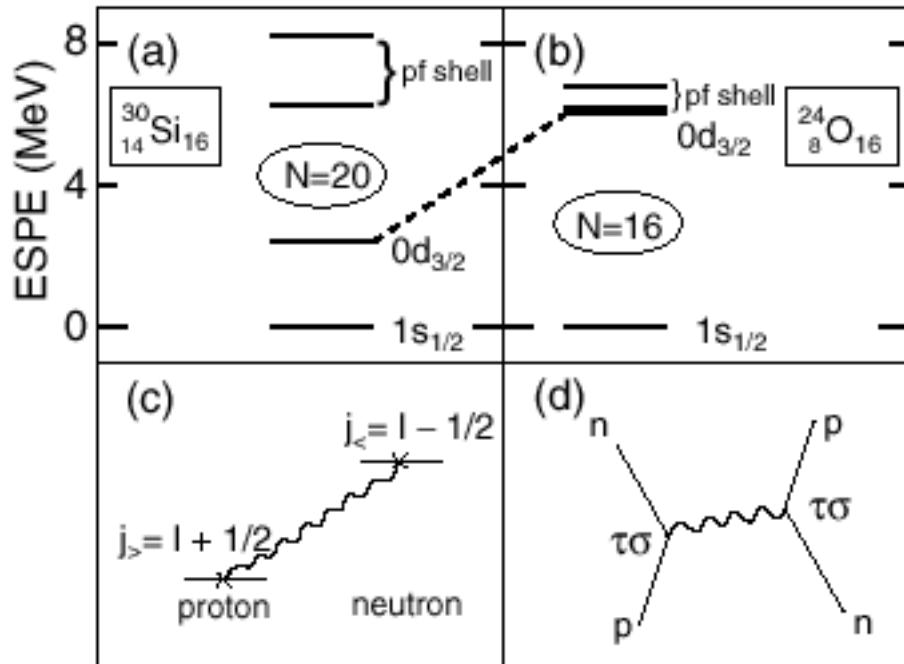
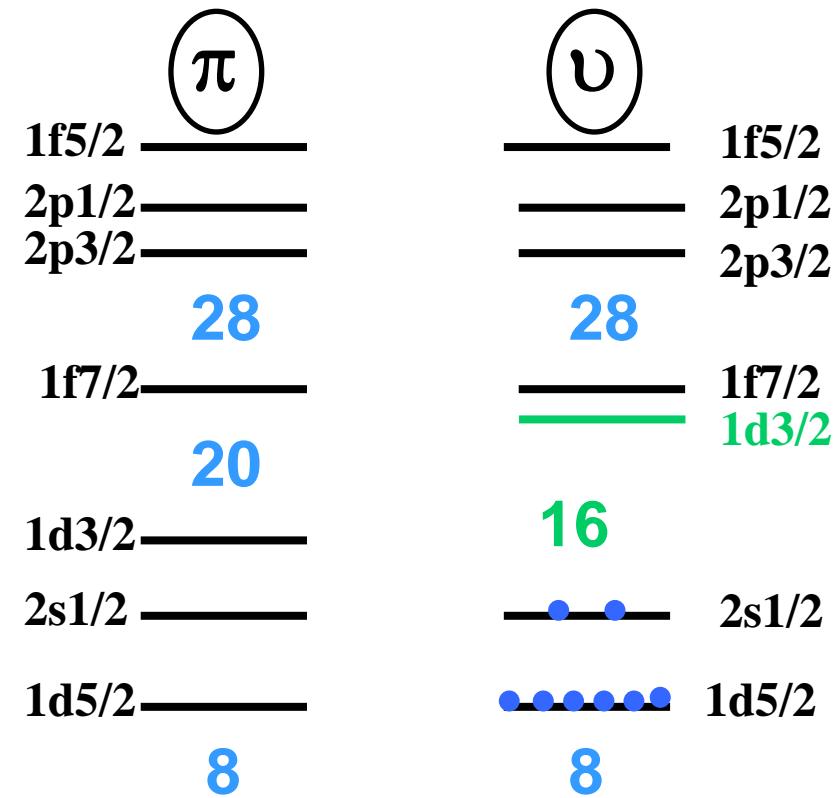


^{30}Si

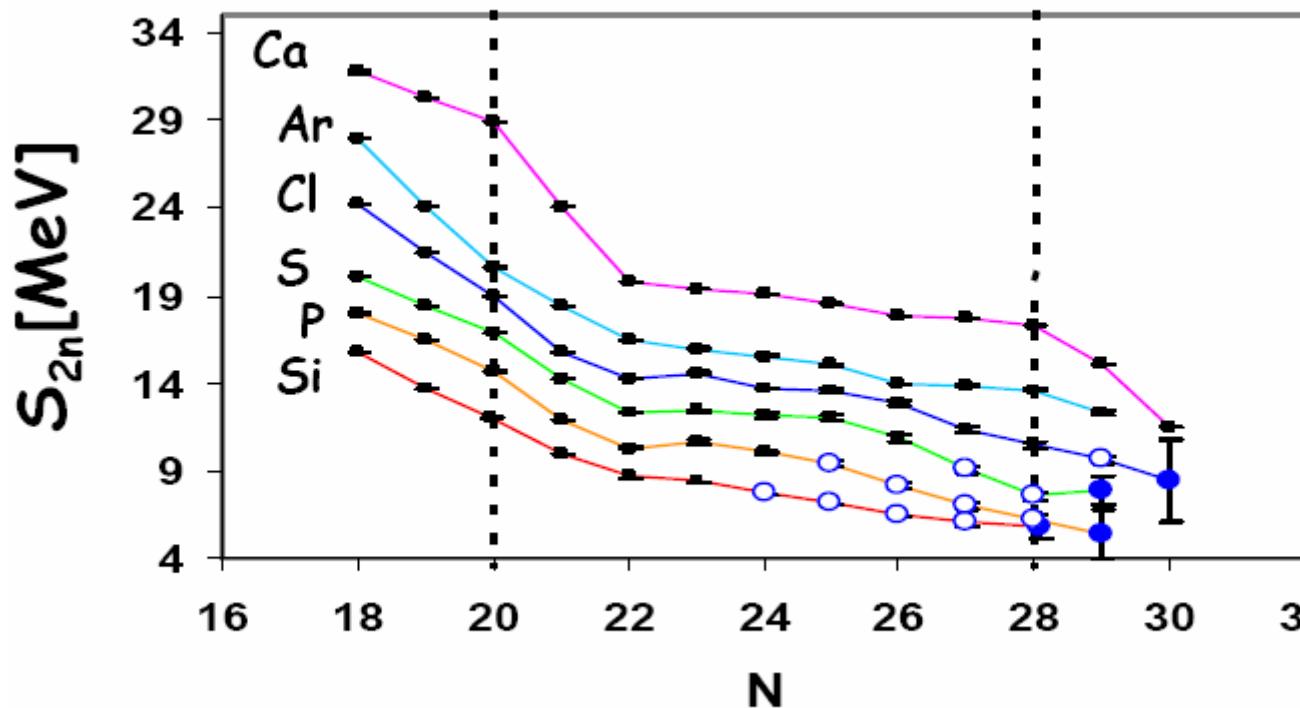
14 16



$^{24}_{\Lambda}O_{16}$



$N=28$



✓ New masses:

^{42}Si , ^{44}P , ^{45}S , ^{47}Cl

✓ Weakening of shell $N=28$

			Al27	Al28	Al29	Al30	Al31	Al32	Al33	Al34	Al35	Al36	Al37	Al38	Al39	Al40	Al41	
Mg24	Mg25	Mg26	Mg27	Mg28	Mg29	Mg30	Mg31	Mg32	Mg33	Mg34	Mg35	Mg36	Mg37	Mg38				
Na22	Na23	Na24	Na25	Na26	Na27	Na28	Na29	Na30	Na31	Na32								
Ne20	Ne21	Ne22	Ne23	Ne24	Ne25	Ne26	Ne27	Ne28	Ne29	Ne30	Ne31							
F19	F20	F21	F22	F23	F24	F25	F26	F27		F29								

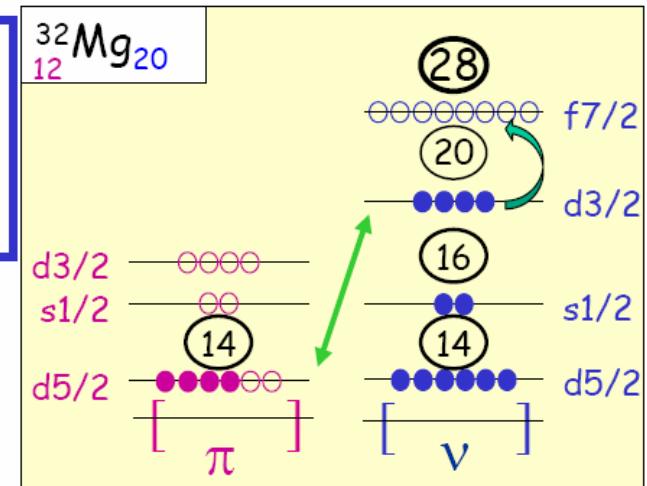
Weakening of shell closure N=28
 Deformation
 Decrease of the spin-orbit coupling

Reorganisation of shell structure around N=20

Deformation

Neutron-Proton Interaction

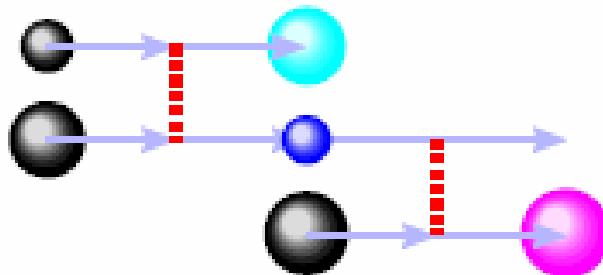
(Otsuka et al. Eur. Phys. J. A 13 (2002) 69)



1960s-2000s : a long (unsuccessful) quest

► two-step reactions :

- ▷ $p + W \xrightarrow{(A\bar{b})} A\bar{n} + {}^{70}\text{Zn} \rightarrow {}^{72}\text{Zn} [(t,p)]$
- ▷ ${}^{208}\text{Po} (\pi^-, \pi^+) {}^4n \xrightarrow{({}^{208}\text{Po})} {}^{212}\text{Po} + \gamma$

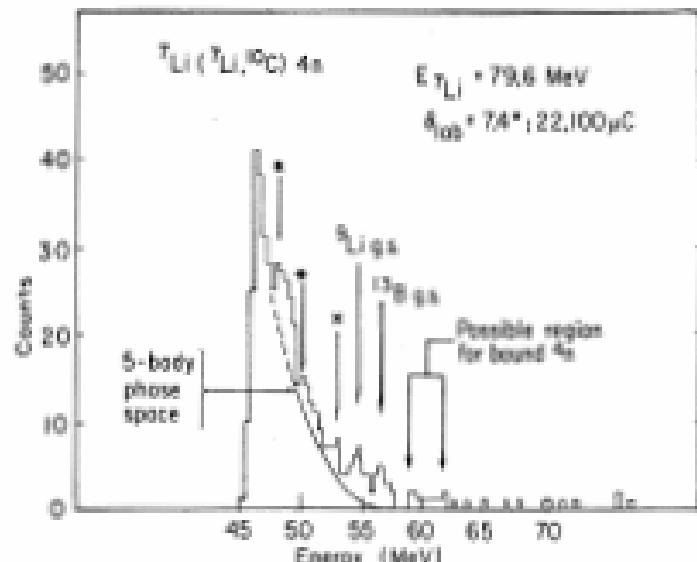


► π charge exchange :

- ▷ ${}^3\text{H} (\pi^-, \gamma) 3n$
- ▷ $\{{}^3, {}^4\}\text{He} (\pi^-, \pi^+) \{{}^3, {}^4\}n$

► multinucleon transfer :

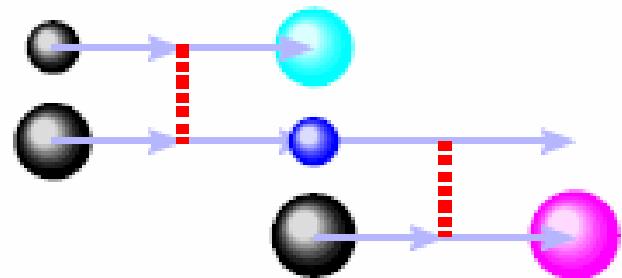
- ▷ ${}^7\text{Li} + {}^{11}\text{B} \rightarrow {}^{14}\text{O} + 4n$
- ▷ ${}^7\text{Li} + {}^7\text{Li} \rightarrow \{{}^{10,11}\}\text{C} + \{{}^4, {}^3\}n$



► backgrounds + cross-sections ...

1960s-2000s : a long (unsuccessful) quest

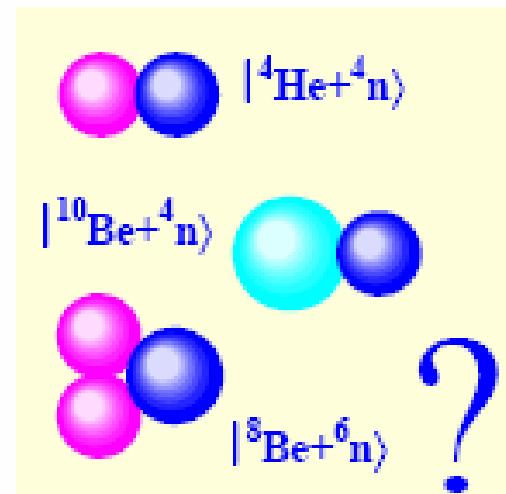
► two-step reactions :



► π charge exchange :



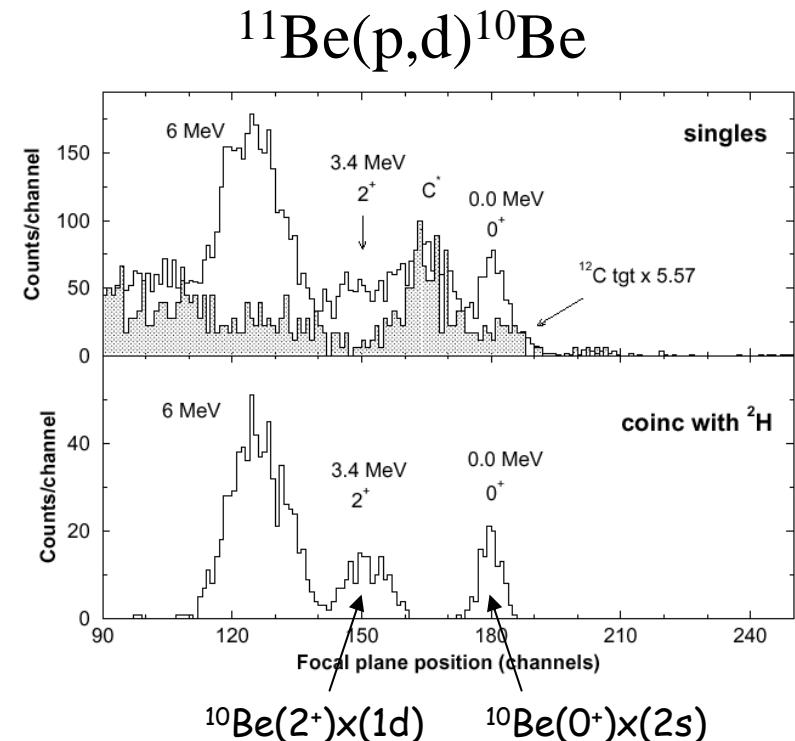
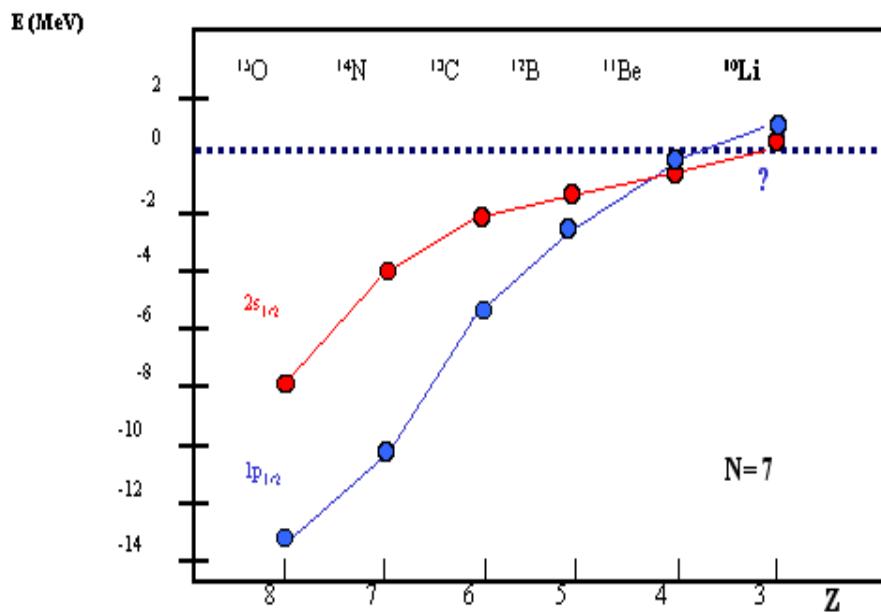
► multinucleon transfer :



► look *inside* very n -rich nuclei !!!

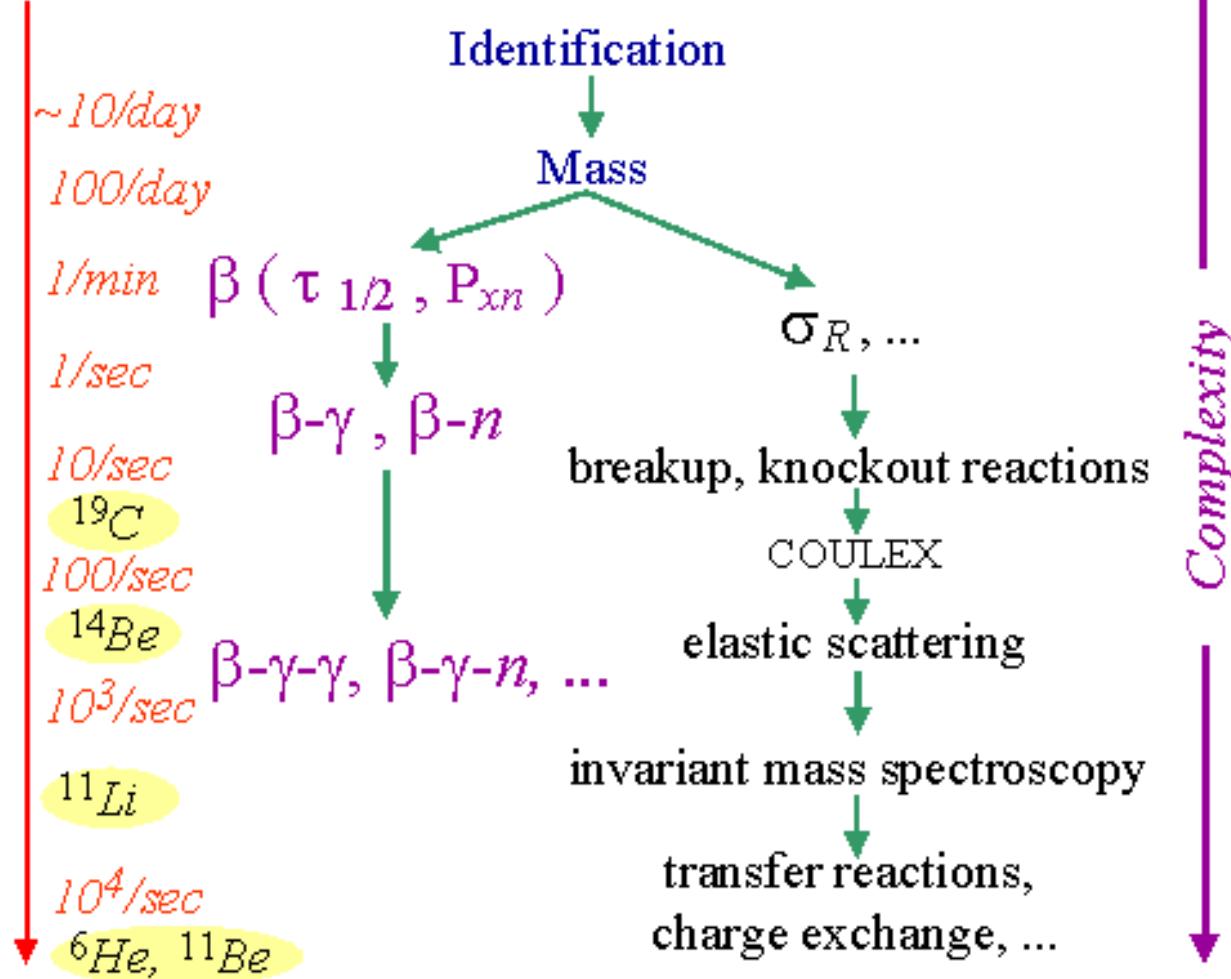
Modification de la structure en couches loin de la stabilité

—Inversion des couches $1p_{1/2}$ et $2s_{1/2}$ pour les noyaux riches en neutrons

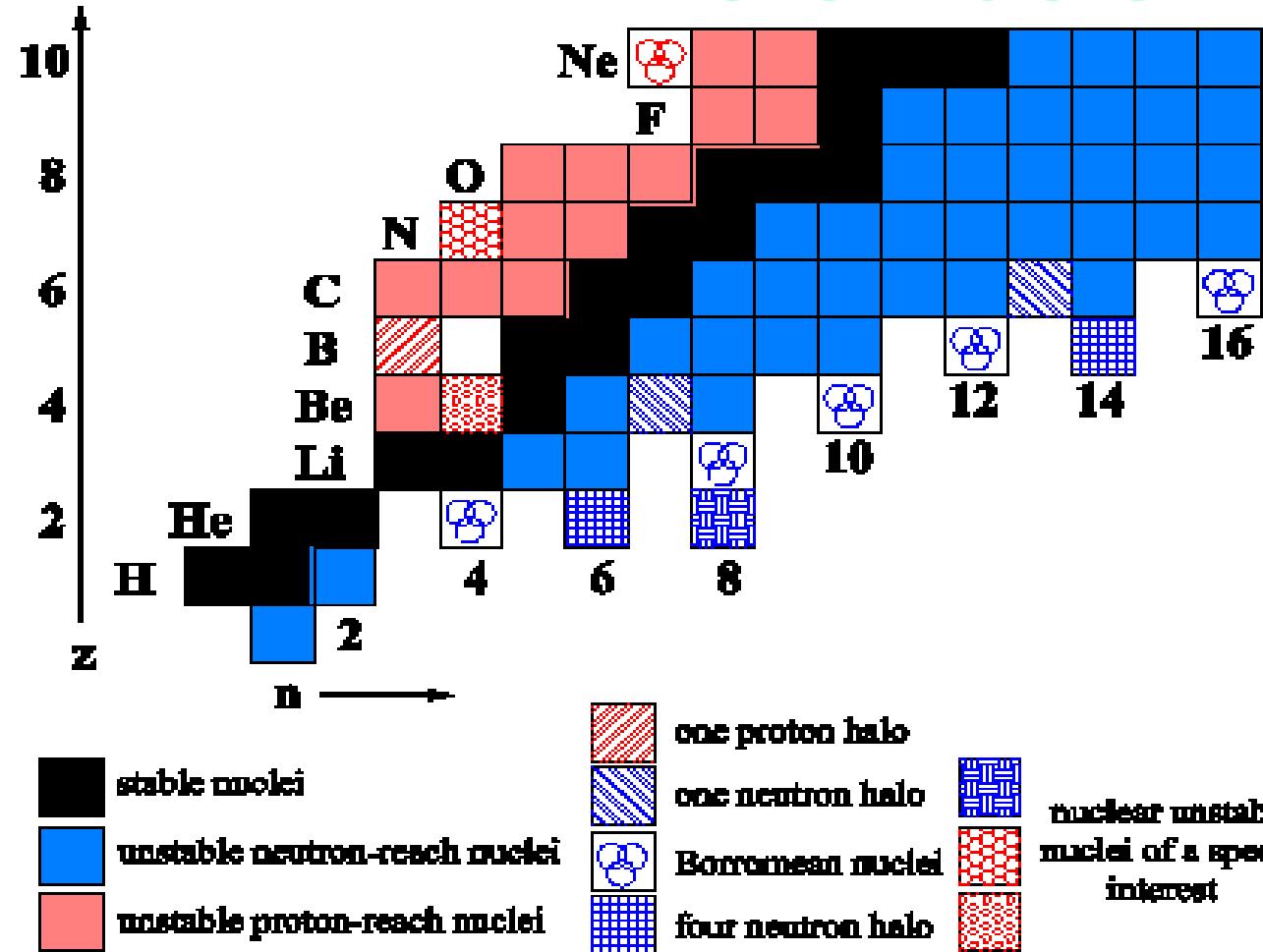


Tools for structure studies

The evolution in experimental complexity with beam intensity

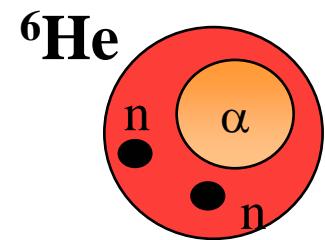
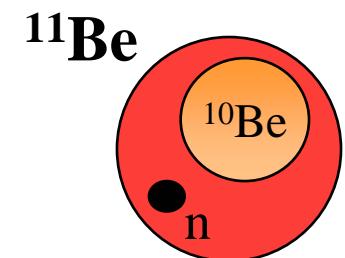
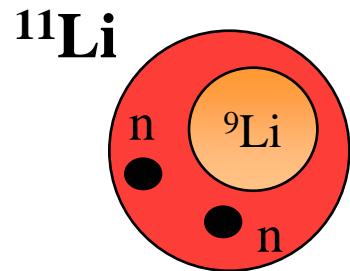


Halo nuclei

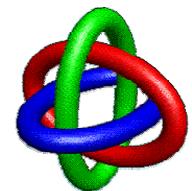


^{17}B , ^{19}C , ^8B one neutron, one proton halo

^{22}C , ^{17}Ne borromean



^6He , ^{11}Li , ^{14}Be
Borroméen



Faisceaux

GANIL - SISSI fragmentation : (déjà mesurés)

^{16}C 40 MeV/A : ^{18}O 63 MeV/A + ^9Be 800 mg/cm² ----> 10^4 pps

^{20}O 43 MeV/A : ^{40}Ar 77 MeV/A + ^{12}C 360 mg/cm² ----> $5 \cdot 10^3$ pps

^{22}O 46 MeV/A : ^{36}S 77 MeV/A + ^{12}C 540 mg/cm² ----> 1200 pps

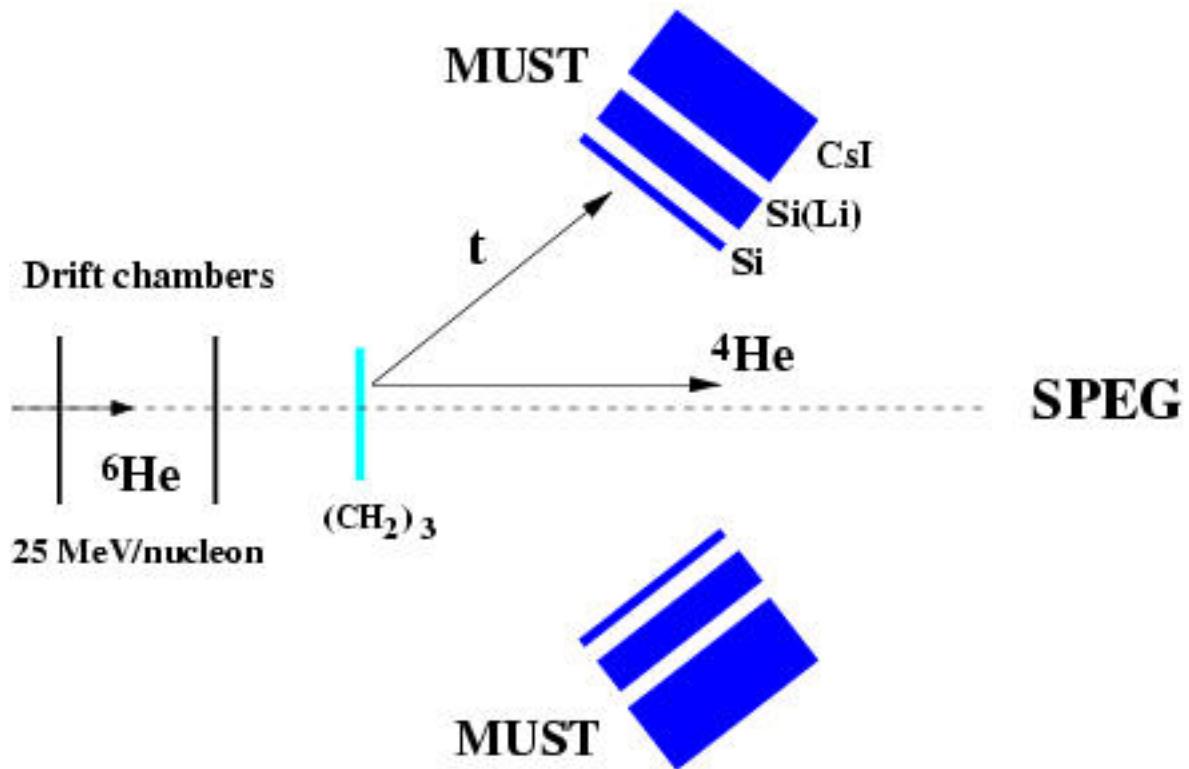
^{25}F 40 MeV/A : ^{36}S 77 MeV/A + ^{12}C 530 mg/cm² ----> 200 pps

GANIL - SISSI fragmentation : (estimation code LISE)

^{18}C 40 MeV/A : ^{40}Ar 77 MeV/A + ^{12}C 360 mg/cm² ----> $3 \cdot 10^3$ pps

GANIL - SPIRAL II :

^{68}Ni : 10^5 pps rapport spiral II, p7



Fonction d'onde de l' ${}^6\text{He}$: $t + t$?

- Energie de liaison de l' ${}^6\text{He}$
reproduite
avec une configuration triton-triton

A. Csoto, PRC 48 (1993) 165

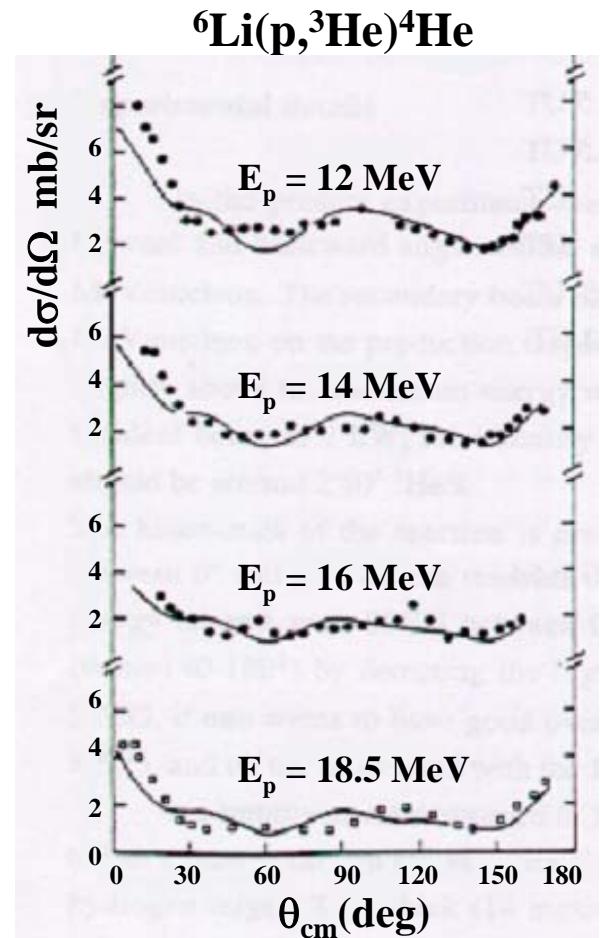
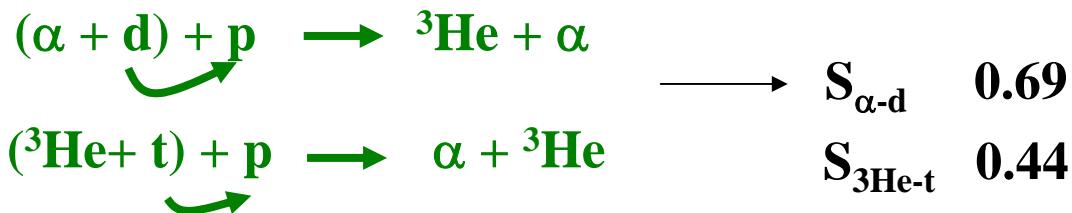
- Calculs microscopiques

TISM: $S_{t-t} = 1.77$ Yu. F. Smirnov, PRC 15 (1977) 84
 $S_{\alpha-2n} = 1.12$

RGM: $S_{t-t} = 0.49$ K. Arai et al., PRC 59 (1999) 1432

- Analogie avec ${}^6\text{Li}$

${}^6\text{Li}(p, {}^3\text{He})\alpha$: clusters $\alpha+d$ et ${}^3\text{He}+t$



M.F Werby et al., PRC 8 (1973) 106

- $$\begin{array}{ccc} \mathbf{A} + \mathbf{a} & \longrightarrow & \mathbf{B} + \mathbf{b} \\ \{\mathbf{B+x}\} + \mathbf{a} & \longrightarrow & \mathbf{B} + \{\mathbf{a+x}\} \end{array}$$

x: nucléon(s) transférés
ici: t, 2n
- $$\frac{d\sigma}{d\Omega} \text{ dépend de } \mathbf{T}_{AB}$$
 : élément de matrice de la réaction
- $$\mathbf{T}_{AB} = \langle \chi_{bB}^+ \Phi_b \Phi_B | W_{bB} | \Psi_{aA}^+ \rangle$$
 post

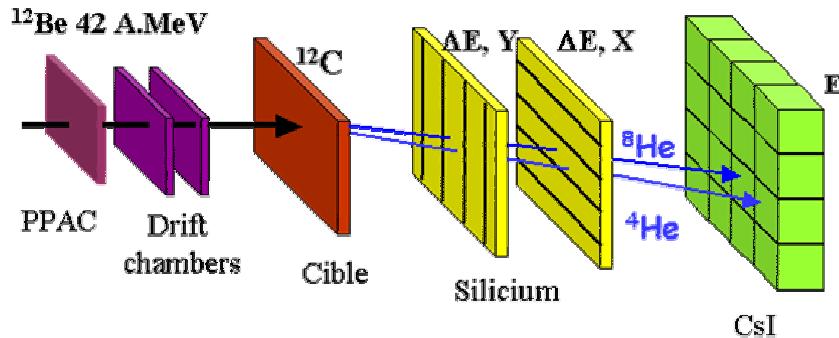
$\chi_{aA}^+ \Phi_a \Phi_A$ DWBA
- $$W_{bB} = V_{bB} - U_{bB}$$

$V_{aB} + V_{xB}$ décrit la diffusion élastique de b+B

Voies couplées

- $\Psi_{\text{CRC}} = \sum_i \Phi_i^t \Phi_i^p \chi_i^{t-p}$
 - cible
 - projectile
 - $i=a,b,c\dots$
 - partitions de masse
- $(H-E)\Psi_{\text{CRC}} = 0$
- **Projection**
 - sur les différents états d'une partition de masse
 - ↳ Système d'équations intégro-différentielles couplées reliant les inconnues χ_i^{t-p}
- **Résolution système + conditions asymptotiques**
 - ↳ Amplitudes de diffusion f_{ab}, f_{bc}
 - ↳ Section efficace différentielle de la réaction

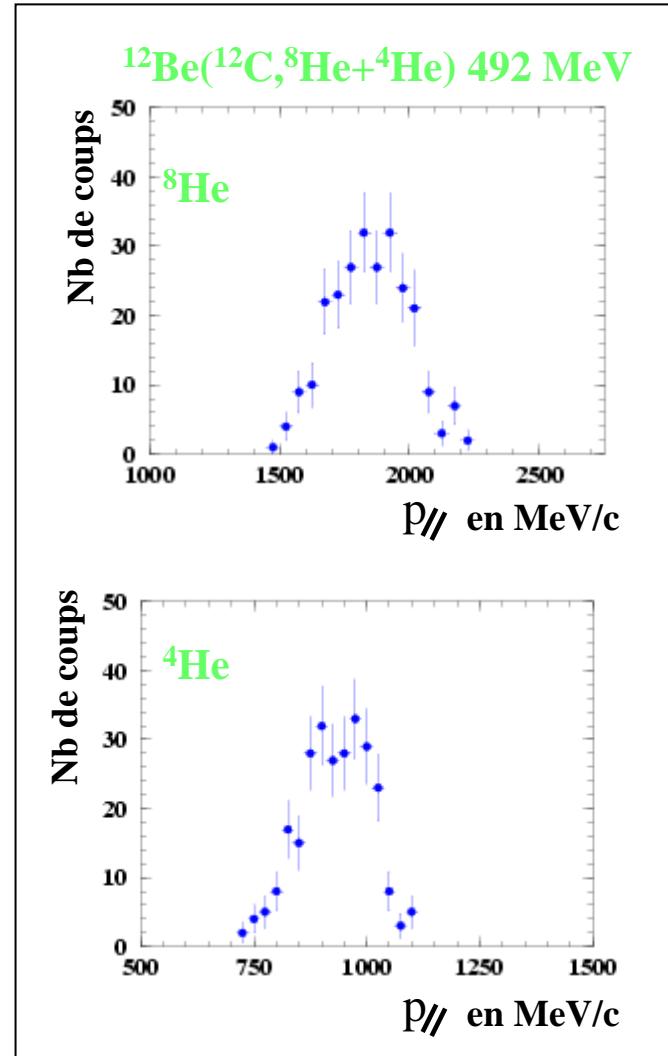
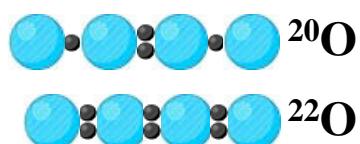
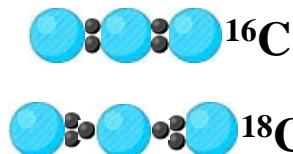
Etats moléculaires du $^{10,12}Be$



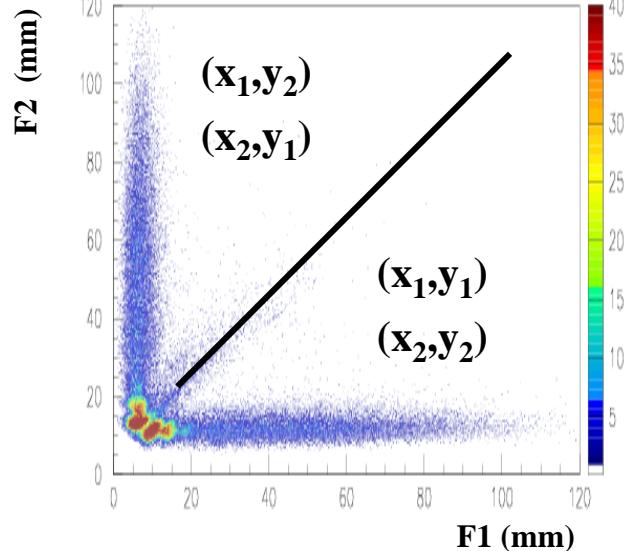
- ♦ Méthode

- distributions p_{\parallel} et p_{\perp} expérimentales des fragments chargés
- comparaison modèle de Glauber (F. Carstoiu)
- simulation Monte-Carlo:
convolution distributions moment théoriques avec effets expérimentaux

- ♦ Futur

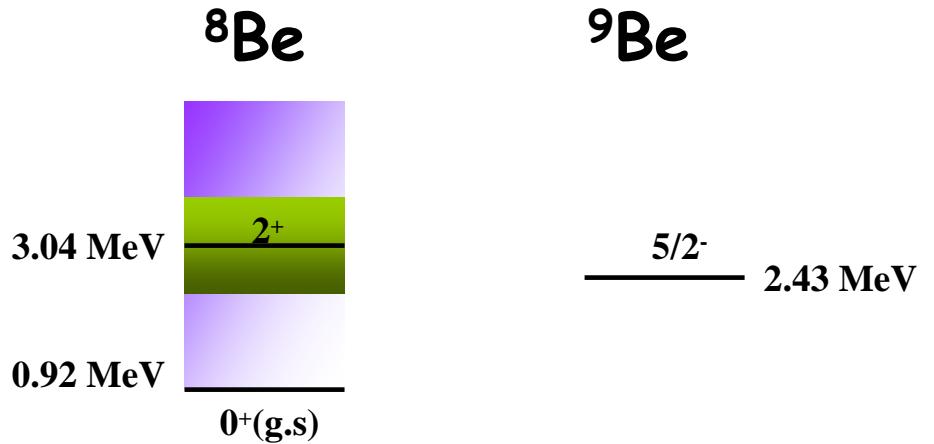
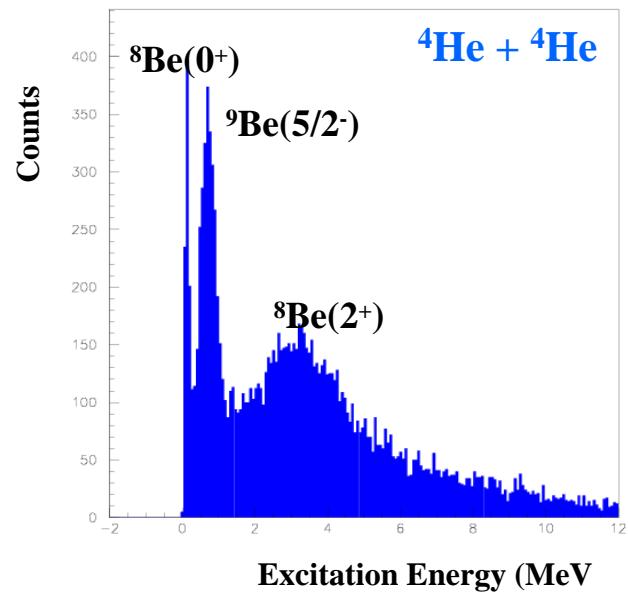
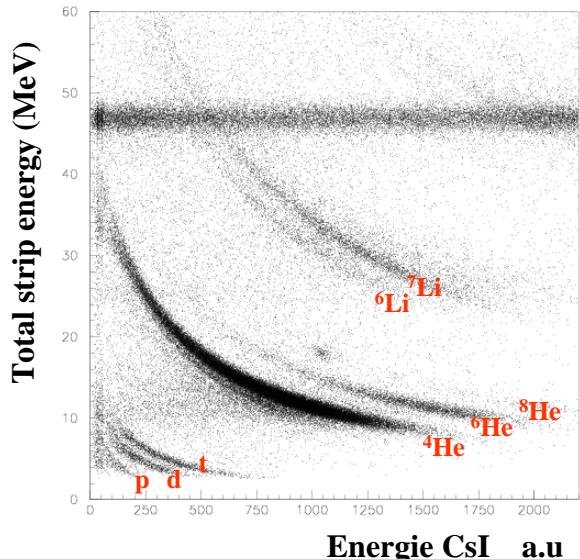


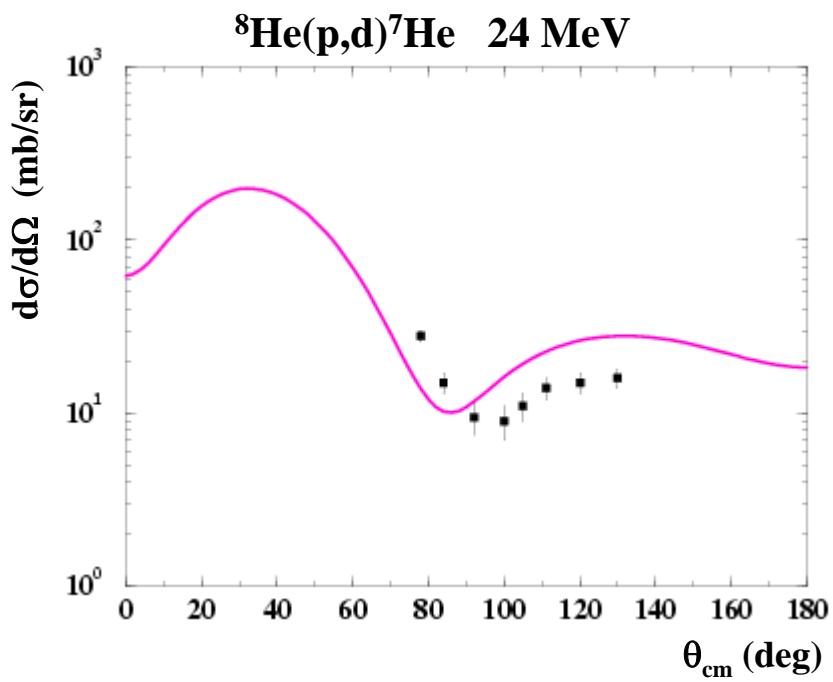
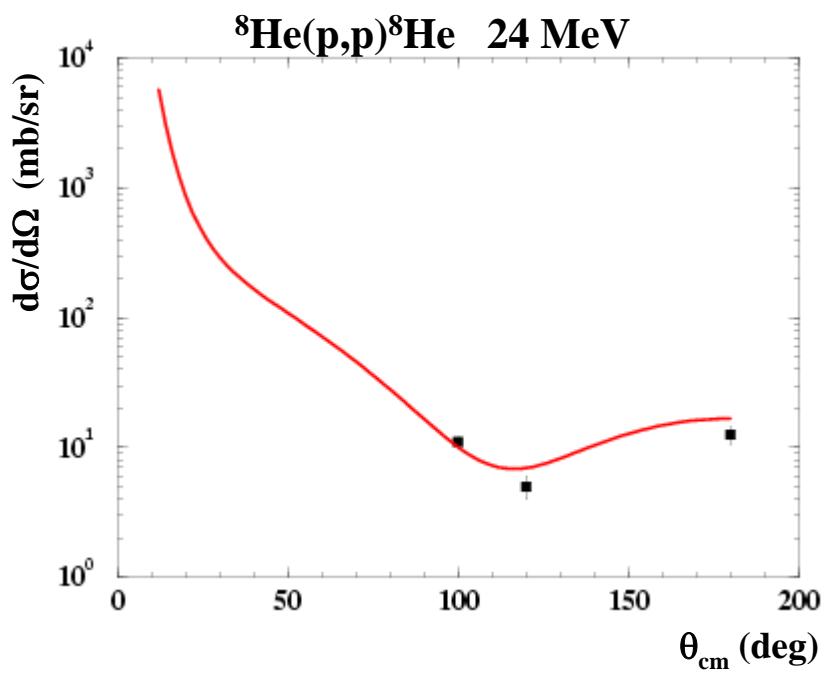
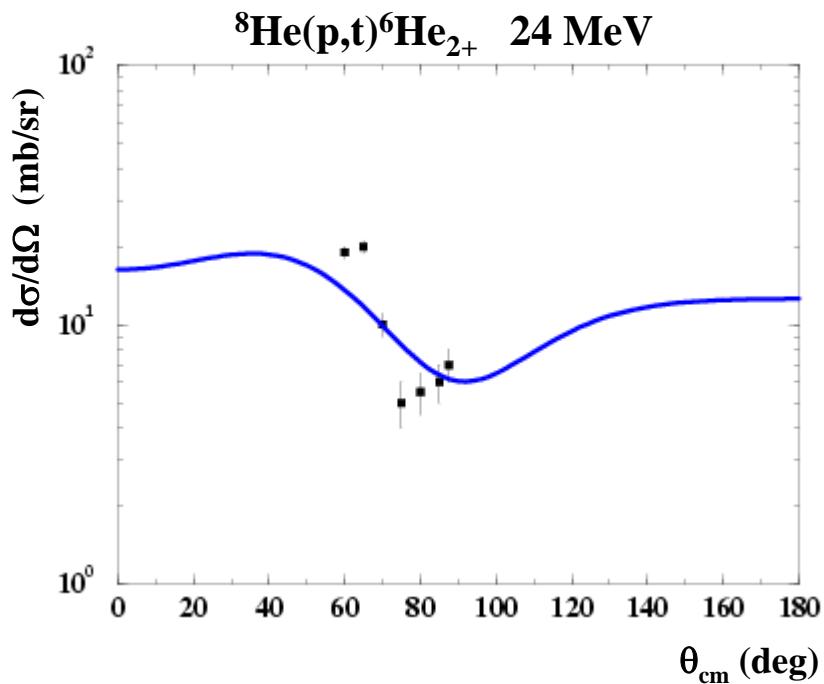
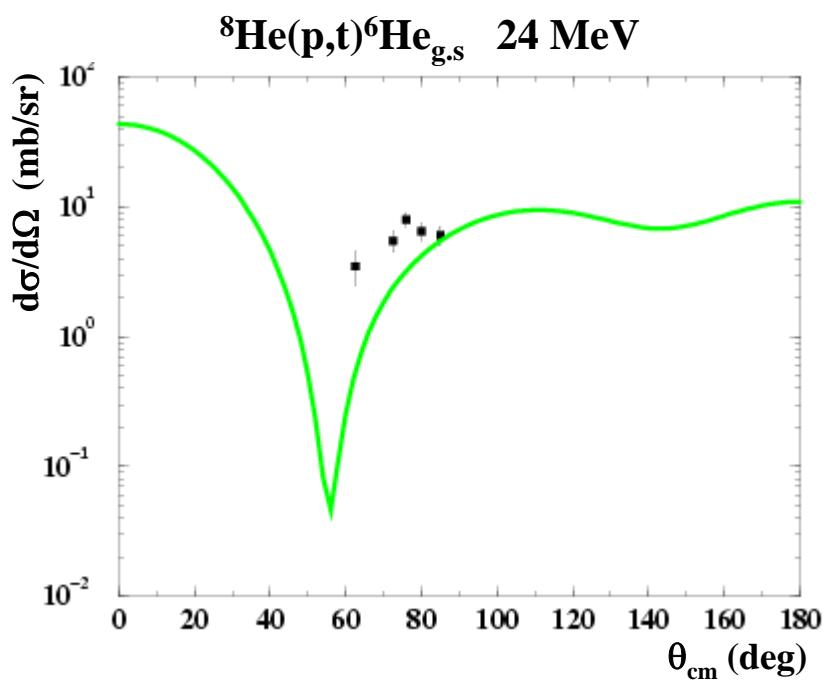
2 Events correlation

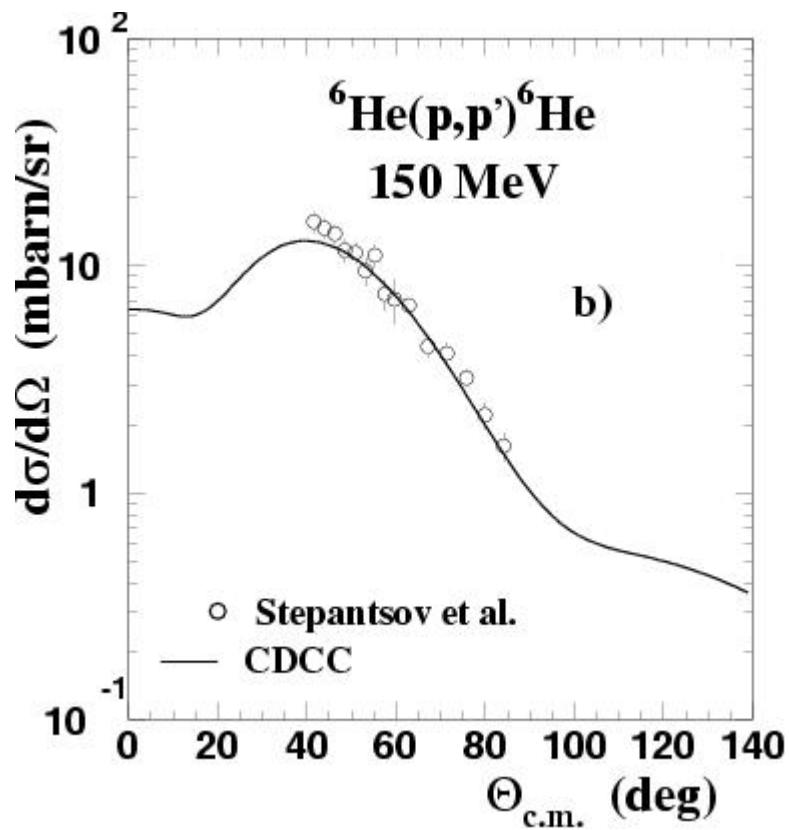
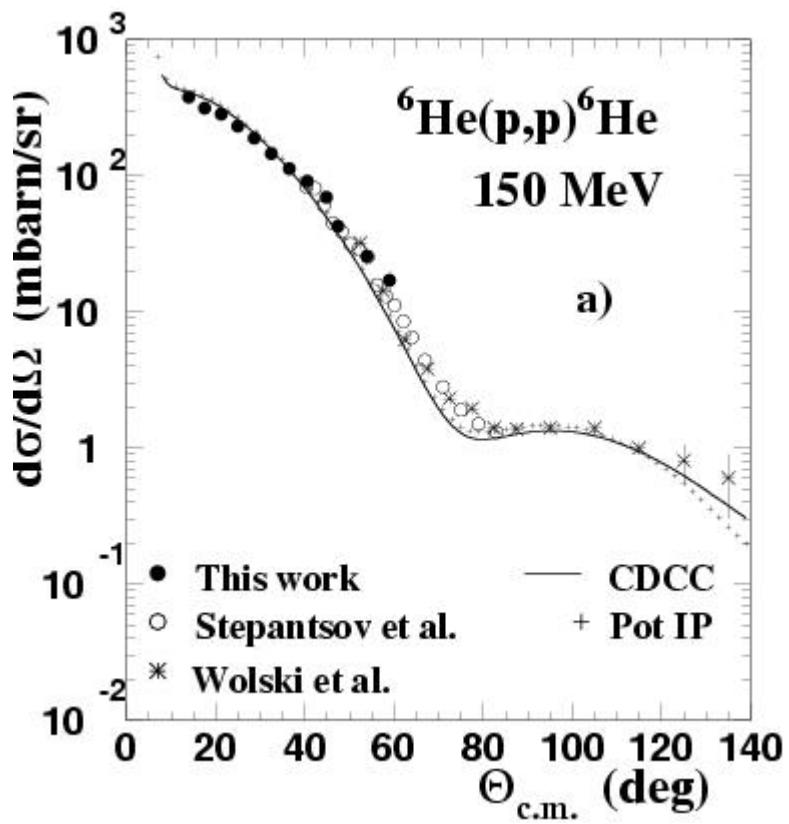


F1 and F2 Fonctions de corrélation

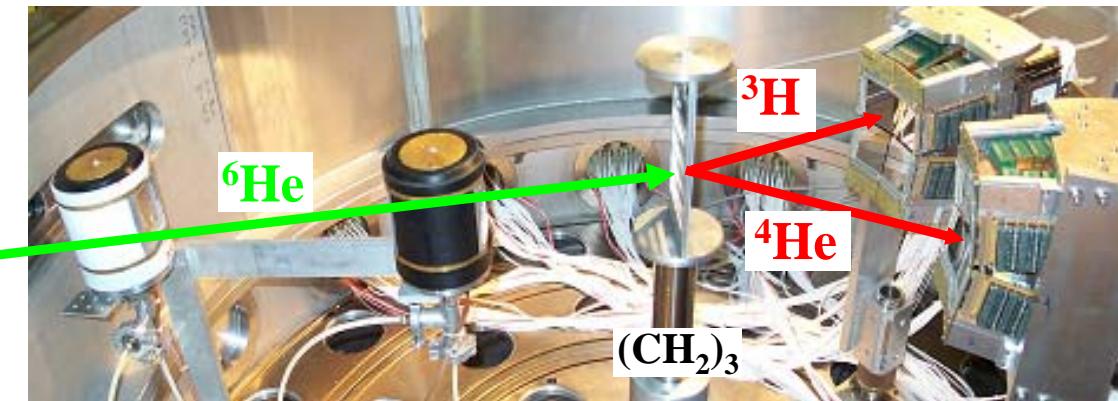
- x₁, x₂, y₁, y₂
precise position
(charge division)
- px₁, px₂, py₁, py₂
rough position
(strip number)







Dispositif expérimental

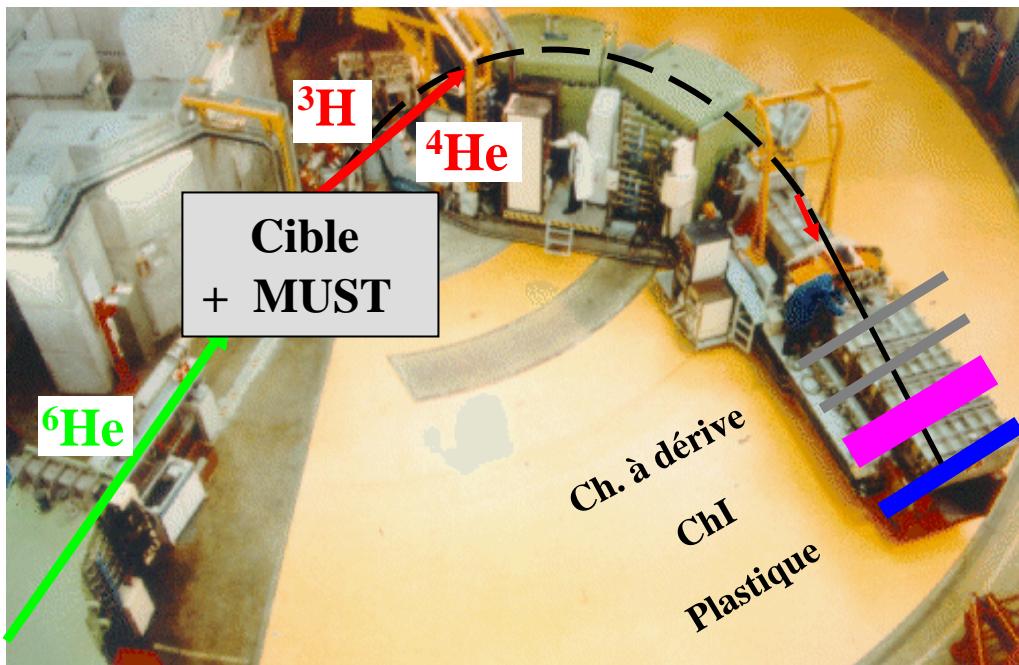


Détection: ${}^4\text{He}$ et ${}^3\text{H}$

MUST

ou

SPEG

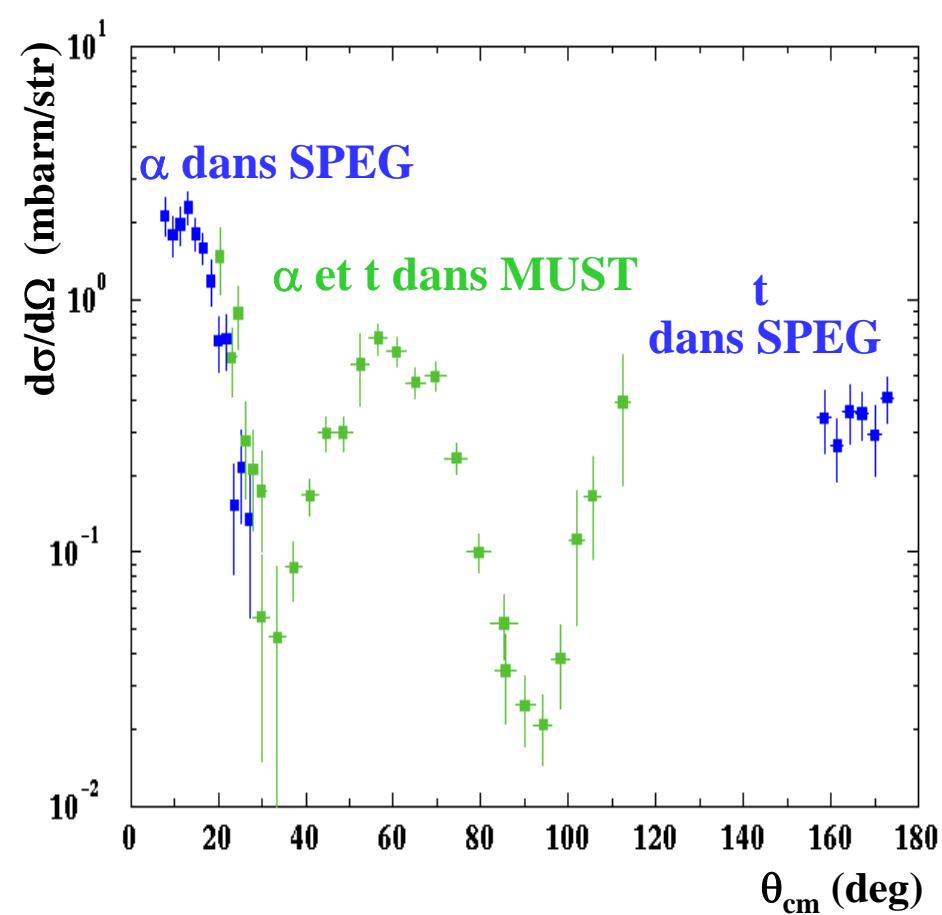


Collaboration:

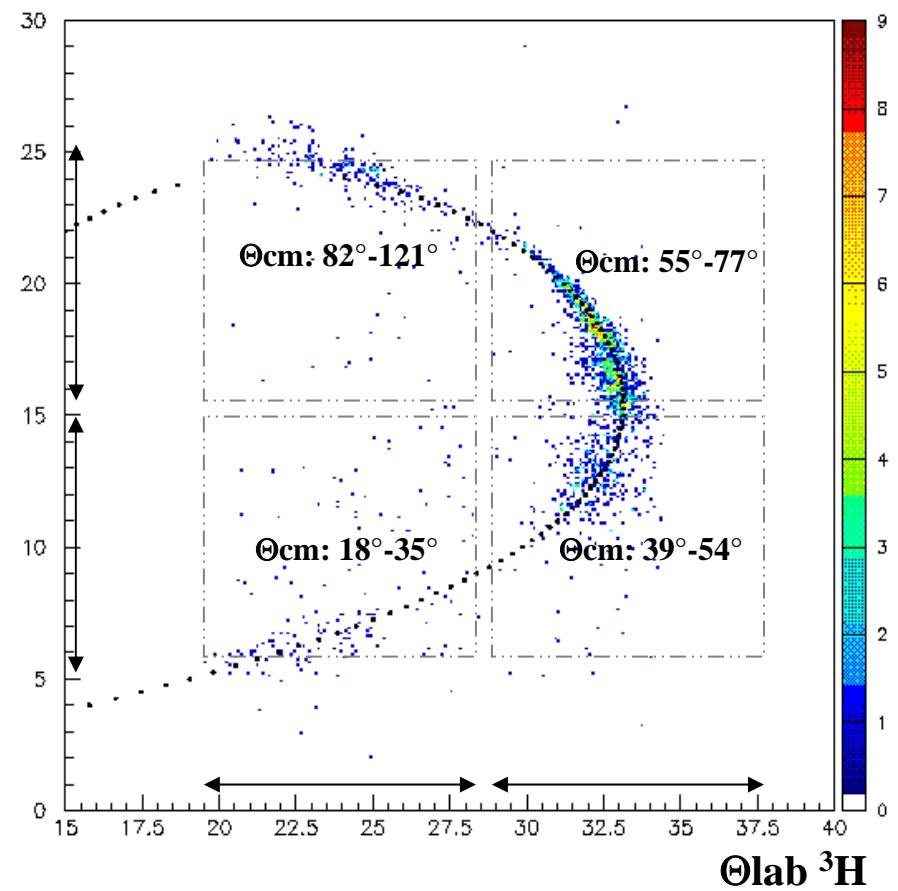
Ganil

Dapnia, IPNO,
Bruyères-le-Châtel

${}^6\text{He}(p,t){}^4\text{He}$ 150 MeV



MUST: α et t en coïncidence

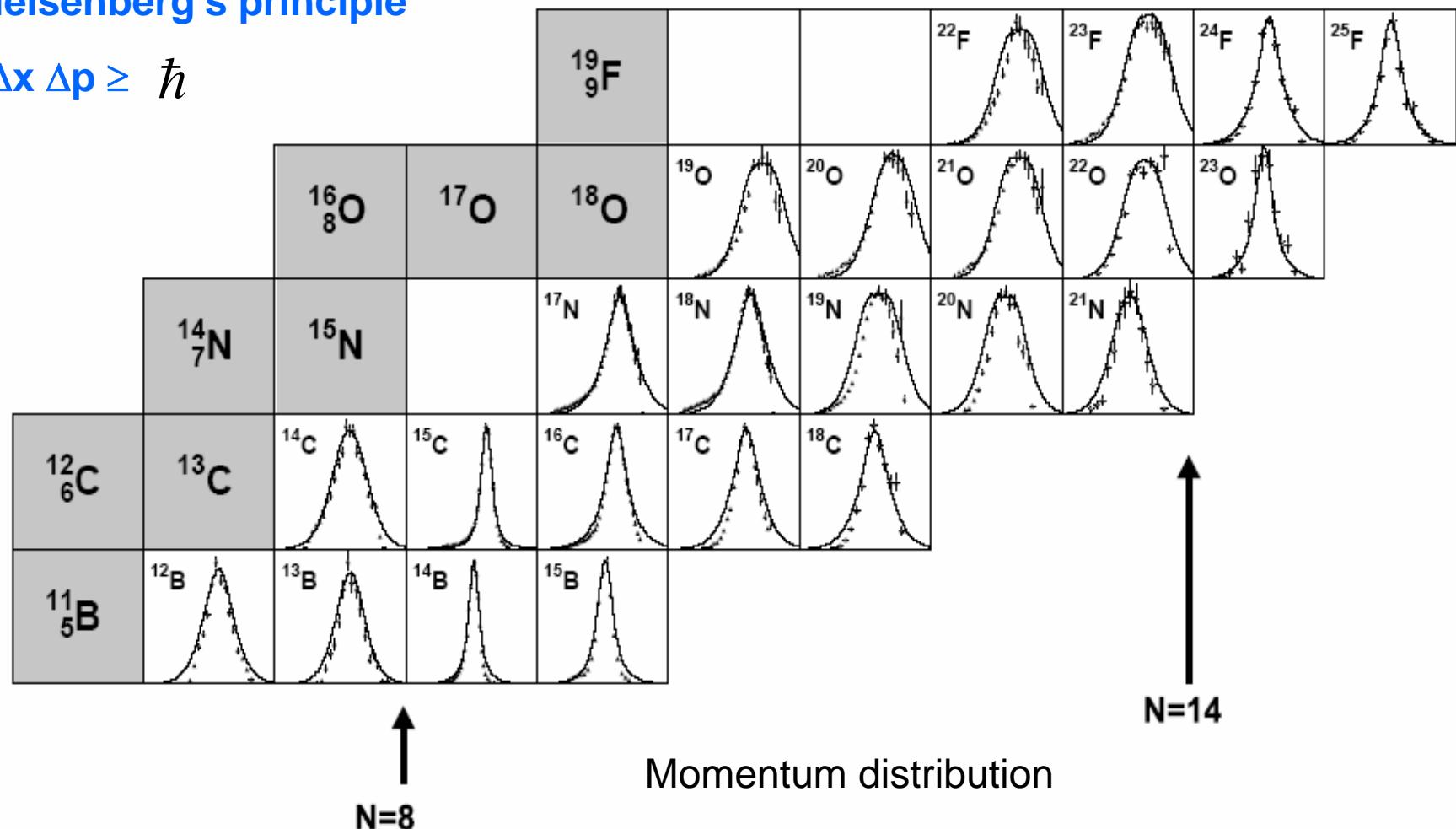


→ bon accord entre les données obtenues avec SPEG et MUST

Single-Neutron Removal: p-sd shell

Heisenberg's principle

$$\Delta x \Delta p \geq \hbar$$



Expt v 's Glauber Theory + Shell Model: Sauvan, et al., PRC (2004)