

## Estimation of the angular transmission of projectile residues in RUN89

### 1 Summary

This note shows the calculation of the transmission  $T$ , which describes the relative yield of products of a given mass, which pass through the FRS for the reaction  $^{56}\text{Fe}$  on protons at different beam energies. The calculation includes three steps, which consist of the calculation of the momentum width of the projectile residue in the rest frame, determining the corresponding opening angle of the velocity cone of the projectile residues in the laboratory frame and calculating the transmission  $T$  as a function of the angle determined in the previous step.

### 2 The momentum distribution width

#### Goldhaber model

The first case follows the result of the Goldhaber approach for the estimation of the width of the momentum distribution of the projectile residues [1]. It is assumed, that the distribution is isotropic in rest frame of reference (see formula (1)). For the constant  $\sigma_0$  the value of 103 MeV/c was used, which is consistent with the previously estimated results for reactions with similar energies, in which medium-mass nuclei are involved [1,3]. In this case, no other correction corresponding to the momentum transfer during the emission of particles or particle groups during the different reaction steps has been made, due to the fact, that in the statistical Goldhaber approach the processes which occur in the reaction are not described explicitly.

#### Morrissey systematics

The entire mass loss on which the transferred momentum depends is the result of two separate steps, namely the abrasion of nucleons and the following deexcitation of the prefragment by emission of nucleons or nucleon groups (ablation step). The Goldhaber formula describes only the momentum transfer caused by the abrasion, therefore a description of the transferred momentum, based on the entire mass loss requires a separate treatment of both steps, which is effectively included in the Morrissey systematics. The next two cases consist the empirical result of the momentum spread of projectile residues in which the width of the momentum distribution depends linearly on the square root of the projectile mass loss [3]. The constant of proportionality estimated by Morrissey [3] amounts to 150 MeV/c per unit of  $\sqrt{A}$ . In the present case this value is divided in addition by a factor of  $\sqrt{3}$ , because the calculations of the deflection angle refers to one cartesian component of the momentum in the rest frame of reference. Due to possible uncertainties of the estimated constant, the doubled value of  $300 / \sqrt{3}$  MeV/c is used to describe the kinematics in the third case. The third case should not be considered to be realistic, it just gives an extreme upper estimate for the width of the momentum spread, here it is used as a measure of the confidence range of our predictions.

### 3 The transmission estimation

The yield of the reaction products transmitted through the FRS without losses is calculated only by taking into account the opening angle of the velocity cone in the laboratory frame of reference, where the cone has a point source of origin. The broadening of the angular distribution due to angular straggling phenomena in the target or other layers of matter passed by the products are not included. Following the determination of the angular transmission proposed recently by Benlliure et al [3] an effective acceptance angle of 15mrad for the FRS spectrometer has been used. While a Gaussian shape of the distribution of the products with respect to the deflection angle in the laboratory frame of reference is assumed, the yield  $T$  is calculated by the use of equation (7), as quoted in [3].

### References

- [1] A. S. Goldhaber, Phys. Lett. B 53 (1974) 306-8
- [2] D.J. Morrissey, Phys. Rev. C 39 (1989) 460

[3] J. Benlliure, J. Pereira-Conca, K.-H. Schmidt, Nucl. Instr. and Meth A(2001), accepted; preprint GSI ,<http://www-wnt.gsi.de/kschmidt/bep00.htm>

**Table 1: Formulas and constants**

|  |  |
|--|--|
| Width of the momentum distribution in the rest frame in MeV/c,<br>Eq.(1): Goldhaber theory[1]<br>Eq.(2): Morrissey systematics [2] | $\sigma^2 = \sigma_0^2 \frac{K(A-K)}{A-1} \quad (1)$ <p style="text-align: center;"><i>K</i>: Fragment mass<br/> <i>A</i>: Projectile mass</p> $\sigma = \frac{150}{\sqrt{3}} \cdot \sqrt{\Delta A} \quad (2)$ <p style="text-align: center;"><math>\Delta A</math>: Mass loss</p> |
| Momentum to velocity Transformation  | $\Delta\beta_{cm} = \frac{\frac{pc}{A \cdot 931.5}}{\sqrt{1 + \left(\frac{pc}{A \cdot 931.5}\right)^2}} \quad (3)$   |
| Time transform from rest to lab. frame of reference.   | $\frac{dt'}{dt} = \frac{1 + \frac{u \cdot v}{c^2}}{\sqrt{1 - \frac{v^2}{c^2}}} \quad (4)$  |
| Transformation laws of the velocity components from the rest to lab. frame of reference.   | $u_{\parallel}' = \frac{u_{\parallel} + v}{1 + \frac{u_{\parallel}' v}{c^2}}, \quad u_{\perp}' = \frac{u_{\perp} \sqrt{1 - \frac{v^2}{c^2}}}{1 + \frac{u_{\parallel}' v}{c^2}} \quad (5)$  |
| Deflection angle in the lab. frame of reference in [rad].  | $\theta = \frac{u'}{v} \sqrt{1 - \frac{v^2}{c^2}} \mapsto \frac{\Delta\beta_{cm}}{\beta} \sqrt{1 - \beta^2} \text{ if } u' \ll v \quad (6)$  |
| Transmission estimate of the FRS according to Benlliure et all [3].  | $T = 1 - \exp\left(-\frac{\alpha_{eff}^2}{2\sigma_{\theta}^2}\right) \quad (7)$  |

The denoted constants in the following table are listed below:

$\sigma_G, \sigma_M$ : Calculated widths of the momentum distribution in one direction in the rest frame of reference according to the Goldhaber formula (G) and Morrissey systematics (M);

$\theta_G, \theta_M$ : Maximum deflection angle in the laboratory frame of reference induced by a transferred momentum with the values  $\sigma_G$  and  $\sigma_M$  in the rest frame of reference;

$\theta_{DM}$ : Maximum deflection angle in the laboratory frame of reference induced by a transferred momentum with the value  $2.\sigma_M$ ;

$T_G, T_M, T_{DM}$ : Transmission coefficients for cone shaped velocity distributions of the projectile residues in the laboratory frame of reference, with the corresponding opening angles  $\theta_G, \theta_M, \theta_{DM}$ .

**Table 2: Results**

| A  | 300 A.MeV          |                    |                   |                   |                      |       |       |          |
|----|--------------------|--------------------|-------------------|-------------------|----------------------|-------|-------|----------|
|    | $\sigma_G$ [MeV/c] | $\sigma_M$ [MeV/c] | $\theta_G$ [mrad] | $\theta_M$ [mrad] | $\theta_{DM}$ [mrad] | $T_G$ | $T_M$ | $T_{DM}$ |
| 10 | 274.7              | 587.4              | 34.09             | 72.77             | 144.69               | 0.079 | 0.021 | 0.005    |
| 11 | 285.0              | 580.9              | 32.15             | 65.46             | 130.29               | 0.088 | 0.026 | 0.007    |
| 12 | 294.3              | 574.5              | 30.44             | 59.35             | 118.23               | 0.098 | 0.031 | 0.008    |
| 13 | 302.9              | 567.9              | 28.91             | 54.17             | 107.98               | 0.108 | 0.038 | 0.010    |
| 14 | 310.6              | 561.2              | 27.54             | 49.72             | 99.17                | 0.119 | 0.044 | 0.011    |
| 15 | 317.7              | 554.5              | 26.28             | 45.86             | 91.50                | 0.129 | 0.052 | 0.013    |
| 16 | 324.1              | 547.7              | 25.14             | 42.47             | 84.76                | 0.141 | 0.060 | 0.016    |
| 17 | 329.8              | 540.8              | 24.08             | 39.47             | 78.80                | 0.152 | 0.070 | 0.018    |
| 18 | 335.0              | 533.9              | 23.10             | 36.80             | 73.49                | 0.164 | 0.080 | 0.021    |
| 19 | 339.6              | 526.8              | 22.19             | 34.40             | 68.71                | 0.177 | 0.091 | 0.024    |
| 20 | 343.7              | 519.6              | 21.33             | 32.24             | 64.40                | 0.190 | 0.103 | 0.027    |
| 21 | 347.3              | 512.3              | 20.53             | 30.28             | 60.49                | 0.203 | 0.115 | 0.030    |
| 22 | 350.3              | 505.0              | 19.77             | 28.49             | 56.92                | 0.217 | 0.129 | 0.034    |
| 23 | 352.9              | 497.5              | 19.05             | 26.84             | 53.65                | 0.232 | 0.145 | 0.038    |
| 24 | 355.0              | 489.9              | 18.36             | 25.33             | 50.63                | 0.247 | 0.161 | 0.043    |
| 25 | 356.6              | 482.2              | 17.71             | 23.94             | 47.85                | 0.263 | 0.178 | 0.048    |
| 26 | 357.8              | 474.3              | 17.08             | 22.64             | 45.26                | 0.280 | 0.197 | 0.053    |
| 27 | 358.4              | 466.4              | 16.48             | 21.44             | 42.86                | 0.297 | 0.217 | 0.059    |
| 28 | 358.7              | 458.3              | 15.90             | 20.31             | 40.61                | 0.315 | 0.239 | 0.066    |
| 29 | 358.4              | 450.0              | 15.34             | 19.26             | 38.50                | 0.334 | 0.262 | 0.073    |
| 30 | 357.8              | 441.6              | 14.80             | 18.27             | 36.53                | 0.354 | 0.286 | 0.081    |
| 31 | 356.6              | 433.0              | 14.28             | 17.34             | 34.66                | 0.375 | 0.312 | 0.089    |
| 32 | 355.0              | 424.3              | 13.77             | 16.46             | 32.90                | 0.396 | 0.340 | 0.099    |
| 33 | 352.9              | 415.3              | 13.27             | 15.62             | 31.24                | 0.419 | 0.369 | 0.109    |
| 34 | 350.3              | 406.2              | 12.79             | 14.83             | 29.65                | 0.443 | 0.400 | 0.120    |
| 35 | 347.3              | 396.9              | 12.32             | 14.08             | 28.14                | 0.468 | 0.433 | 0.132    |
| 36 | 343.7              | 387.3              | 11.85             | 13.35             | 26.70                | 0.494 | 0.468 | 0.146    |
| 37 | 339.6              | 377.5              | 11.39             | 12.66             | 25.32                | 0.521 | 0.504 | 0.161    |
| 38 | 335.0              | 367.4              | 10.94             | 12.00             | 24.00                | 0.550 | 0.542 | 0.177    |
| 39 | 329.8              | 357.1              | 10.50             | 11.37             | 22.73                | 0.580 | 0.581 | 0.196    |
| 40 | 324.1              | 346.4              | 10.06             | 10.75             | 21.50                | 0.612 | 0.622 | 0.216    |
| 41 | 317.7              | 335.4              | 9.62              | 10.16             | 20.31                | 0.645 | 0.664 | 0.239    |
| 42 | 310.6              | 324.0              | 9.18              | 9.58              | 19.15                | 0.679 | 0.707 | 0.264    |
| 43 | 302.9              | 312.2              | 8.74              | 9.01              | 18.03                | 0.714 | 0.750 | 0.293    |
| 44 | 294.3              | 300.0              | 8.30              | 8.46              | 16.93                | 0.750 | 0.792 | 0.325    |
| 45 | 285.0              | 287.2              | 7.86              | 7.92              | 15.85                | 0.787 | 0.833 | 0.361    |
| 46 | 274.7              | 273.9              | 7.41              | 7.39              | 14.78                | 0.825 | 0.873 | 0.402    |
| 47 | 263.5              | 259.8              | 6.96              | 6.86              | 13.72                | 0.861 | 0.908 | 0.450    |
| 48 | 251.0              | 244.9              | 6.49              | 6.33              | 12.67                | 0.897 | 0.939 | 0.504    |
| 49 | 237.2              | 229.1              | 6.01              | 5.80              | 11.61                | 0.929 | 0.965 | 0.566    |
| 50 | 221.9              | 212.1              | 5.51              | 5.27              | 10.53                | 0.957 | 0.983 | 0.637    |
| 51 | 204.6              | 193.6              | 4.98              | 4.71              | 9.43                 | 0.979 | 0.994 | 0.718    |
| 52 | 184.7              | 173.2              | 4.41              | 4.13              | 8.27                 | 0.993 | 0.999 | 0.807    |
| 53 | 161.5              | 150.0              | 3.78              | 3.51              | 7.03                 | 0.999 | 1.000 | 0.898    |
| 54 | 133.1              | 122.5              | 3.06              | 2.82              | 5.63                 | 1.000 | 1.000 | 0.971    |
| 55 | 95.0               | 86.6               | 2.14              | 1.95              | 3.91                 | 1.000 | 1.000 | 0.999    |

Continuation of table 2

| A  | 500 A.MeV          |                    |                   |                   |                      |       |       |          |
|----|--------------------|--------------------|-------------------|-------------------|----------------------|-------|-------|----------|
|    | $\sigma_G$ [MeV/c] | $\sigma_M$ [MeV/c] | $\theta_G$ [mrad] | $\theta_M$ [mrad] | $\theta_{DM}$ [mrad] | $T_G$ | $T_M$ | $T_{DM}$ |
| 10 | 274.7              | 587.4              | 25.26             | 53.93             | 107.23               | 0.139 | 0.038 | 0.010    |
| 11 | 285.0              | 580.9              | 23.83             | 48.51             | 96.56                | 0.155 | 0.047 | 0.012    |
| 12 | 294.3              | 574.5              | 22.56             | 43.98             | 87.62                | 0.171 | 0.056 | 0.015    |
| 13 | 302.9              | 567.9              | 21.43             | 40.14             | 80.03                | 0.188 | 0.067 | 0.017    |
| 14 | 310.6              | 561.2              | 20.41             | 36.85             | 73.49                | 0.205 | 0.080 | 0.021    |
| 15 | 317.7              | 554.5              | 19.48             | 33.98             | 67.81                | 0.223 | 0.093 | 0.024    |
| 16 | 324.1              | 547.7              | 18.63             | 31.47             | 62.82                | 0.241 | 0.107 | 0.028    |
| 17 | 329.8              | 540.8              | 17.85             | 29.25             | 58.40                | 0.260 | 0.123 | 0.032    |
| 18 | 335.0              | 533.9              | 17.12             | 27.27             | 54.46                | 0.279 | 0.140 | 0.037    |
| 19 | 339.6              | 526.8              | 16.44             | 25.50             | 50.92                | 0.298 | 0.159 | 0.042    |
| 20 | 343.7              | 519.6              | 15.81             | 23.89             | 47.73                | 0.318 | 0.179 | 0.048    |
| 21 | 347.3              | 512.3              | 15.21             | 22.44             | 44.83                | 0.339 | 0.200 | 0.054    |
| 22 | 350.3              | 505.0              | 14.65             | 21.11             | 42.18                | 0.360 | 0.223 | 0.061    |
| 23 | 352.9              | 497.5              | 14.11             | 19.89             | 39.76                | 0.381 | 0.247 | 0.069    |
| 24 | 355.0              | 489.9              | 13.61             | 18.77             | 37.52                | 0.404 | 0.273 | 0.077    |
| 25 | 356.6              | 482.2              | 13.12             | 17.74             | 35.46                | 0.426 | 0.301 | 0.086    |
| 26 | 357.8              | 474.3              | 12.66             | 16.78             | 33.54                | 0.450 | 0.329 | 0.095    |
| 27 | 358.4              | 466.4              | 12.21             | 15.89             | 31.76                | 0.474 | 0.360 | 0.106    |
| 28 | 358.7              | 458.3              | 11.78             | 15.05             | 30.10                | 0.498 | 0.391 | 0.117    |
| 29 | 358.4              | 450.0              | 11.37             | 14.27             | 28.54                | 0.523 | 0.424 | 0.129    |
| 30 | 357.8              | 441.6              | 10.97             | 13.54             | 27.07                | 0.549 | 0.459 | 0.142    |
| 31 | 356.6              | 433.0              | 10.58             | 12.85             | 25.69                | 0.575 | 0.494 | 0.157    |
| 32 | 355.0              | 424.3              | 10.21             | 12.20             | 24.39                | 0.601 | 0.531 | 0.172    |
| 33 | 352.9              | 415.3              | 9.84              | 11.58             | 23.15                | 0.628 | 0.568 | 0.189    |
| 34 | 350.3              | 406.2              | 9.48              | 10.99             | 21.98                | 0.655 | 0.606 | 0.208    |
| 35 | 347.3              | 396.9              | 9.13              | 10.43             | 20.86                | 0.683 | 0.644 | 0.228    |
| 36 | 343.7              | 387.3              | 8.78              | 9.90              | 19.79                | 0.711 | 0.683 | 0.250    |
| 37 | 339.6              | 377.5              | 8.44              | 9.39              | 18.77                | 0.739 | 0.721 | 0.273    |
| 38 | 335.0              | 367.4              | 8.11              | 8.89              | 17.79                | 0.767 | 0.759 | 0.299    |
| 39 | 329.8              | 357.1              | 7.78              | 8.42              | 16.84                | 0.794 | 0.795 | 0.327    |
| 40 | 324.1              | 346.4              | 7.45              | 7.97              | 15.93                | 0.821 | 0.830 | 0.358    |
| 41 | 317.7              | 335.4              | 7.13              | 7.53              | 15.05                | 0.848 | 0.863 | 0.391    |
| 42 | 310.6              | 324.0              | 6.80              | 7.10              | 14.19                | 0.873 | 0.893 | 0.428    |
| 43 | 302.9              | 312.2              | 6.48              | 6.68              | 13.36                | 0.898 | 0.920 | 0.468    |
| 44 | 294.3              | 300.0              | 6.15              | 6.27              | 12.54                | 0.920 | 0.943 | 0.511    |
| 45 | 285.0              | 287.2              | 5.83              | 5.87              | 11.74                | 0.940 | 0.962 | 0.558    |
| 46 | 274.7              | 273.9              | 5.49              | 5.48              | 10.95                | 0.958 | 0.976 | 0.608    |
| 47 | 263.5              | 259.8              | 5.16              | 5.09              | 10.17                | 0.973 | 0.987 | 0.663    |
| 48 | 251.0              | 244.9              | 4.81              | 4.69              | 9.39                 | 0.984 | 0.994 | 0.721    |
| 49 | 237.2              | 229.1              | 4.45              | 4.30              | 8.60                 | 0.992 | 0.998 | 0.781    |
| 50 | 221.9              | 212.1              | 4.08              | 3.90              | 7.81                 | 0.997 | 0.999 | 0.842    |
| 51 | 204.6              | 193.6              | 3.69              | 3.49              | 6.99                 | 0.999 | 1.000 | 0.900    |
| 52 | 184.7              | 173.2              | 3.27              | 3.06              | 6.13                 | 1.000 | 1.000 | 0.950    |
| 53 | 161.5              | 150.0              | 2.80              | 2.60              | 5.21                 | 1.000 | 1.000 | 0.984    |
| 54 | 133.1              | 122.5              | 2.27              | 2.09              | 4.17                 | 1.000 | 1.000 | 0.998    |
| 55 | 95.0               | 86.6               | 1.59              | 1.45              | 2.90                 | 1.000 | 1.000 | 1.000    |

Continuation of table 2

| A  | 750 A.MeV          |                    |                   |                   |                      |       |       |          |
|----|--------------------|--------------------|-------------------|-------------------|----------------------|-------|-------|----------|
|    | $\sigma_G$ [MeV/c] | $\sigma_M$ [MeV/c] | $\theta_G$ [mrad] | $\theta_M$ [mrad] | $\theta_{DM}$ [mrad] | $T_G$ | $T_M$ | $T_{DM}$ |
| 10 | 274.7              | 587.4              | 19.62             | 41.87             | 83.26                | 0.220 | 0.062 | 0.016    |
| 11 | 285.0              | 580.9              | 18.50             | 37.67             | 74.97                | 0.244 | 0.076 | 0.020    |
| 12 | 294.3              | 574.5              | 17.52             | 34.15             | 68.03                | 0.268 | 0.092 | 0.024    |
| 13 | 302.9              | 567.9              | 16.64             | 31.17             | 62.14                | 0.292 | 0.109 | 0.029    |
| 14 | 310.6              | 561.2              | 15.84             | 28.61             | 57.06                | 0.317 | 0.128 | 0.034    |
| 15 | 317.7              | 554.5              | 15.12             | 26.39             | 52.65                | 0.342 | 0.149 | 0.040    |
| 16 | 324.1              | 547.7              | 14.46             | 24.44             | 48.78                | 0.367 | 0.172 | 0.046    |
| 17 | 329.8              | 540.8              | 13.86             | 22.71             | 45.35                | 0.393 | 0.196 | 0.053    |
| 18 | 335.0              | 533.9              | 13.29             | 21.18             | 42.29                | 0.418 | 0.222 | 0.061    |
| 19 | 339.6              | 526.8              | 12.77             | 19.80             | 39.54                | 0.444 | 0.250 | 0.069    |
| 20 | 343.7              | 519.6              | 12.27             | 18.55             | 37.06                | 0.470 | 0.279 | 0.079    |
| 21 | 347.3              | 512.3              | 11.81             | 17.42             | 34.81                | 0.496 | 0.310 | 0.089    |
| 22 | 350.3              | 505.0              | 11.37             | 16.39             | 32.75                | 0.523 | 0.342 | 0.100    |
| 23 | 352.9              | 497.5              | 10.96             | 15.45             | 30.87                | 0.549 | 0.376 | 0.111    |
| 24 | 355.0              | 489.9              | 10.56             | 14.58             | 29.13                | 0.576 | 0.411 | 0.124    |
| 25 | 356.6              | 482.2              | 10.19             | 13.77             | 27.53                | 0.602 | 0.447 | 0.138    |
| 26 | 357.8              | 474.3              | 9.83              | 13.03             | 26.04                | 0.629 | 0.485 | 0.153    |
| 27 | 358.4              | 466.4              | 9.48              | 12.34             | 24.66                | 0.655 | 0.523 | 0.169    |
| 28 | 358.7              | 458.3              | 9.15              | 11.69             | 23.37                | 0.681 | 0.561 | 0.186    |
| 29 | 358.4              | 450.0              | 8.83              | 11.08             | 22.16                | 0.707 | 0.600 | 0.205    |
| 30 | 357.8              | 441.6              | 8.52              | 10.51             | 21.02                | 0.733 | 0.639 | 0.225    |
| 31 | 356.6              | 433.0              | 8.22              | 9.98              | 19.95                | 0.758 | 0.677 | 0.246    |
| 32 | 355.0              | 424.3              | 7.92              | 9.47              | 18.93                | 0.782 | 0.715 | 0.269    |
| 33 | 352.9              | 415.3              | 7.64              | 8.99              | 17.97                | 0.806 | 0.751 | 0.294    |
| 34 | 350.3              | 406.2              | 7.36              | 8.53              | 17.06                | 0.829 | 0.787 | 0.321    |
| 35 | 347.3              | 396.9              | 7.09              | 8.10              | 16.19                | 0.851 | 0.820 | 0.349    |
| 36 | 343.7              | 387.3              | 6.82              | 7.68              | 15.37                | 0.872 | 0.851 | 0.379    |
| 37 | 339.6              | 377.5              | 6.56              | 7.29              | 14.57                | 0.892 | 0.880 | 0.411    |
| 38 | 335.0              | 367.4              | 6.30              | 6.91              | 13.81                | 0.910 | 0.905 | 0.446    |
| 39 | 329.8              | 357.1              | 6.04              | 6.54              | 13.08                | 0.927 | 0.928 | 0.482    |
| 40 | 324.1              | 346.4              | 5.79              | 6.19              | 12.37                | 0.943 | 0.947 | 0.521    |
| 41 | 317.7              | 335.4              | 5.53              | 5.84              | 11.69                | 0.956 | 0.963 | 0.561    |
| 42 | 310.6              | 324.0              | 5.28              | 5.51              | 11.02                | 0.968 | 0.975 | 0.604    |
| 43 | 302.9              | 312.2              | 5.03              | 5.19              | 10.37                | 0.977 | 0.985 | 0.648    |
| 44 | 294.3              | 300.0              | 4.78              | 4.87              | 9.74                 | 0.985 | 0.991 | 0.695    |
| 45 | 285.0              | 287.2              | 4.52              | 4.56              | 9.12                 | 0.991 | 0.996 | 0.742    |
| 46 | 274.7              | 273.9              | 4.27              | 4.25              | 8.50                 | 0.995 | 0.998 | 0.789    |
| 47 | 263.5              | 259.8              | 4.00              | 3.95              | 7.90                 | 0.997 | 0.999 | 0.835    |
| 48 | 251.0              | 244.9              | 3.74              | 3.65              | 7.29                 | 0.999 | 1.000 | 0.880    |
| 49 | 237.2              | 229.1              | 3.46              | 3.34              | 6.68                 | 1.000 | 1.000 | 0.920    |
| 50 | 221.9              | 212.1              | 3.17              | 3.03              | 6.06                 | 1.000 | 1.000 | 0.953    |
| 51 | 204.6              | 193.6              | 2.87              | 2.71              | 5.42                 | 1.000 | 1.000 | 0.978    |
| 52 | 184.7              | 173.2              | 2.54              | 2.38              | 4.76                 | 1.000 | 1.000 | 0.993    |
| 53 | 161.5              | 150.0              | 2.18              | 2.02              | 4.04                 | 1.000 | 1.000 | 0.999    |
| 54 | 133.1              | 122.5              | 1.76              | 1.62              | 3.24                 | 1.000 | 1.000 | 1.000    |
| 55 | 95.0               | 86.6               | 1.23              | 1.12              | 2.25                 | 1.000 | 1.000 | 1.000    |

Continuation of table 2

| 1000 A.MeV |                    |                    |                   |                   |                      |       |       |          |
|------------|--------------------|--------------------|-------------------|-------------------|----------------------|-------|-------|----------|
| A          | $\sigma_G$ [MeV/c] | $\sigma_M$ [MeV/c] | $\theta_G$ [mrad] | $\theta_M$ [mrad] | $\theta_{DM}$ [mrad] | $T_G$ | $T_M$ | $T_{DM}$ |
| 10         | 274.7              | 587.4              | 16.23             | 34.64             | 68.88                | 0.305 | 0.089 | 0.023    |
| 11         | 285.0              | 580.9              | 15.31             | 31.16             | 62.03                | 0.335 | 0.109 | 0.029    |
| 12         | 294.3              | 574.5              | 14.49             | 28.25             | 56.29                | 0.366 | 0.131 | 0.035    |
| 13         | 302.9              | 567.9              | 13.76             | 25.79             | 51.41                | 0.397 | 0.156 | 0.042    |
| 14         | 310.6              | 561.2              | 13.11             | 23.67             | 47.21                | 0.427 | 0.182 | 0.049    |
| 15         | 317.7              | 554.5              | 12.51             | 21.83             | 43.56                | 0.457 | 0.210 | 0.058    |
| 16         | 324.1              | 547.7              | 11.97             | 20.22             | 40.35                | 0.487 | 0.241 | 0.067    |
| 17         | 329.8              | 540.8              | 11.46             | 18.79             | 37.52                | 0.517 | 0.273 | 0.077    |
| 18         | 335.0              | 533.9              | 11.00             | 17.52             | 34.99                | 0.547 | 0.307 | 0.088    |
| 19         | 339.6              | 526.8              | 10.56             | 16.38             | 32.71                | 0.576 | 0.343 | 0.100    |
| 20         | 343.7              | 519.6              | 10.16             | 15.35             | 30.66                | 0.605 | 0.380 | 0.113    |
| 21         | 347.3              | 512.3              | 9.77              | 14.41             | 28.80                | 0.633 | 0.418 | 0.127    |
| 22         | 350.3              | 505.0              | 9.41              | 13.56             | 27.10                | 0.661 | 0.458 | 0.142    |
| 23         | 352.9              | 497.5              | 9.07              | 12.78             | 25.54                | 0.688 | 0.498 | 0.158    |
| 24         | 355.0              | 489.9              | 8.74              | 12.06             | 24.10                | 0.714 | 0.539 | 0.176    |
| 25         | 356.6              | 482.2              | 8.43              | 11.40             | 22.78                | 0.740 | 0.579 | 0.195    |
| 26         | 357.8              | 474.3              | 8.13              | 10.78             | 21.55                | 0.765 | 0.620 | 0.215    |
| 27         | 358.4              | 466.4              | 7.85              | 10.21             | 20.40                | 0.789 | 0.660 | 0.237    |
| 28         | 358.7              | 458.3              | 7.57              | 9.67              | 19.33                | 0.812 | 0.700 | 0.260    |
| 29         | 358.4              | 450.0              | 7.30              | 9.17              | 18.33                | 0.834 | 0.738 | 0.285    |
| 30         | 357.8              | 441.6              | 7.05              | 8.70              | 17.39                | 0.854 | 0.774 | 0.311    |
| 31         | 356.6              | 433.0              | 6.80              | 8.25              | 16.50                | 0.874 | 0.808 | 0.338    |
| 32         | 355.0              | 424.3              | 6.56              | 7.83              | 15.66                | 0.892 | 0.840 | 0.368    |
| 33         | 352.9              | 415.3              | 6.32              | 7.44              | 14.87                | 0.909 | 0.869 | 0.399    |
| 34         | 350.3              | 406.2              | 6.09              | 7.06              | 14.12                | 0.924 | 0.895 | 0.431    |
| 35         | 347.3              | 396.9              | 5.86              | 6.70              | 13.40                | 0.938 | 0.918 | 0.466    |
| 36         | 343.7              | 387.3              | 5.64              | 6.36              | 12.71                | 0.951 | 0.938 | 0.501    |
| 37         | 339.6              | 377.5              | 5.42              | 6.03              | 12.06                | 0.961 | 0.955 | 0.539    |
| 38         | 335.0              | 367.4              | 5.21              | 5.71              | 11.43                | 0.971 | 0.968 | 0.578    |
| 39         | 329.8              | 357.1              | 5.00              | 5.41              | 10.82                | 0.978 | 0.979 | 0.617    |
| 40         | 324.1              | 346.4              | 4.79              | 5.12              | 10.23                | 0.985 | 0.986 | 0.658    |
| 41         | 317.7              | 335.4              | 4.58              | 4.83              | 9.67                 | 0.990 | 0.992 | 0.700    |
| 42         | 310.6              | 324.0              | 4.37              | 4.56              | 9.12                 | 0.993 | 0.996 | 0.742    |
| 43         | 302.9              | 312.2              | 4.16              | 4.29              | 8.58                 | 0.996 | 0.998 | 0.783    |
| 44         | 294.3              | 300.0              | 3.95              | 4.03              | 8.06                 | 0.998 | 0.999 | 0.823    |
| 45         | 285.0              | 287.2              | 3.74              | 3.77              | 7.54                 | 0.999 | 1.000 | 0.861    |
| 46         | 274.7              | 273.9              | 3.53              | 3.52              | 7.04                 | 1.000 | 1.000 | 0.897    |
| 47         | 263.5              | 259.8              | 3.31              | 3.27              | 6.53                 | 1.000 | 1.000 | 0.928    |
| 48         | 251.0              | 244.9              | 3.09              | 3.02              | 6.03                 | 1.000 | 1.000 | 0.955    |
| 49         | 237.2              | 229.1              | 2.86              | 2.76              | 5.53                 | 1.000 | 1.000 | 0.975    |
| 50         | 221.9              | 212.1              | 2.62              | 2.51              | 5.01                 | 1.000 | 1.000 | 0.989    |
| 51         | 204.6              | 193.6              | 2.37              | 2.24              | 4.49                 | 1.000 | 1.000 | 0.996    |
| 52         | 184.7              | 173.2              | 2.10              | 1.97              | 3.94                 | 1.000 | 1.000 | 0.999    |
| 53         | 161.5              | 150.0              | 1.80              | 1.67              | 3.35                 | 1.000 | 1.000 | 1.000    |
| 54         | 133.1              | 122.5              | 1.46              | 1.34              | 2.68                 | 1.000 | 1.000 | 1.000    |
| 55         | 95.0               | 86.6               | 1.02              | 0.93              | 1.86                 | 1.000 | 1.000 | 1.000    |

Continuation of table 2

| 1500 A.MeV |                    |                    |                   |                   |                      |       |       |          |
|------------|--------------------|--------------------|-------------------|-------------------|----------------------|-------|-------|----------|
| A          | $\sigma_G$ [MeV/c] | $\sigma_M$ [MeV/c] | $\theta_G$ [mrad] | $\theta_M$ [mrad] | $\theta_{DM}$ [mrad] | $T_G$ | $T_M$ | $T_{DM}$ |
| 10         | 274.7              | 587.4              | 12.23             | 26.10             | 51.89                | 0.473 | 0.152 | 0.041    |
| 11         | 285.0              | 580.9              | 11.53             | 23.48             | 46.73                | 0.513 | 0.185 | 0.050    |
| 12         | 294.3              | 574.5              | 10.92             | 21.29             | 42.40                | 0.552 | 0.220 | 0.061    |
| 13         | 302.9              | 567.9              | 10.37             | 19.43             | 38.73                | 0.589 | 0.258 | 0.072    |
| 14         | 310.6              | 561.2              | 9.88              | 17.83             | 35.57                | 0.625 | 0.298 | 0.085    |
| 15         | 317.7              | 554.5              | 9.43              | 16.45             | 32.82                | 0.659 | 0.340 | 0.099    |
| 16         | 324.1              | 547.7              | 9.02              | 15.23             | 30.40                | 0.692 | 0.384 | 0.115    |
| 17         | 329.8              | 540.8              | 8.64              | 14.16             | 28.26                | 0.723 | 0.430 | 0.131    |
| 18         | 335.0              | 533.9              | 8.29              | 13.20             | 26.36                | 0.752 | 0.476 | 0.150    |
| 19         | 339.6              | 526.8              | 7.96              | 12.34             | 24.65                | 0.779 | 0.522 | 0.169    |
| 20         | 343.7              | 519.6              | 7.65              | 11.56             | 23.10                | 0.805 | 0.569 | 0.190    |
| 21         | 347.3              | 512.3              | 7.36              | 10.86             | 21.70                | 0.829 | 0.615 | 0.213    |
| 22         | 350.3              | 505.0              | 7.09              | 10.22             | 20.41                | 0.851 | 0.660 | 0.237    |
| 23         | 352.9              | 497.5              | 6.83              | 9.63              | 19.24                | 0.871 | 0.703 | 0.262    |
| 24         | 355.0              | 489.9              | 6.58              | 9.09              | 18.16                | 0.890 | 0.744 | 0.289    |
| 25         | 356.6              | 482.2              | 6.35              | 8.59              | 17.16                | 0.907 | 0.783 | 0.318    |
| 26         | 357.8              | 474.3              | 6.13              | 8.12              | 16.23                | 0.922 | 0.818 | 0.347    |
| 27         | 358.4              | 466.4              | 5.91              | 7.69              | 15.37                | 0.935 | 0.851 | 0.379    |
| 28         | 358.7              | 458.3              | 5.70              | 7.29              | 14.56                | 0.947 | 0.880 | 0.412    |
| 29         | 358.4              | 450.0              | 5.50              | 6.91              | 13.81                | 0.958 | 0.905 | 0.446    |
| 30         | 357.8              | 441.6              | 5.31              | 6.55              | 13.10                | 0.966 | 0.927 | 0.481    |
| 31         | 356.6              | 433.0              | 5.12              | 6.22              | 12.43                | 0.974 | 0.945 | 0.517    |
| 32         | 355.0              | 424.3              | 4.94              | 5.90              | 11.80                | 0.980 | 0.960 | 0.554    |
| 33         | 352.9              | 415.3              | 4.76              | 5.60              | 11.20                | 0.985 | 0.972 | 0.592    |
| 34         | 350.3              | 406.2              | 4.59              | 5.32              | 10.64                | 0.989 | 0.981 | 0.630    |
| 35         | 347.3              | 396.9              | 4.42              | 5.05              | 10.09                | 0.993 | 0.988 | 0.669    |
| 36         | 343.7              | 387.3              | 4.25              | 4.79              | 9.58                 | 0.995 | 0.993 | 0.707    |
| 37         | 339.6              | 377.5              | 4.09              | 4.54              | 9.08                 | 0.997 | 0.996 | 0.744    |
| 38         | 335.0              | 367.4              | 3.93              | 4.30              | 8.61                 | 0.998 | 0.998 | 0.781    |
| 39         | 329.8              | 357.1              | 3.77              | 4.08              | 8.15                 | 0.999 | 0.999 | 0.816    |
| 40         | 324.1              | 346.4              | 3.61              | 3.86              | 7.71                 | 0.999 | 0.999 | 0.849    |
| 41         | 317.7              | 335.4              | 3.45              | 3.64              | 7.28                 | 1.000 | 1.000 | 0.880    |
| 42         | 310.6              | 324.0              | 3.29              | 3.43              | 6.87                 | 1.000 | 1.000 | 0.908    |
| 43         | 302.9              | 312.2              | 3.14              | 3.23              | 6.47                 | 1.000 | 1.000 | 0.932    |
| 44         | 294.3              | 300.0              | 2.98              | 3.04              | 6.07                 | 1.000 | 1.000 | 0.953    |
| 45         | 285.0              | 287.2              | 2.82              | 2.84              | 5.68                 | 1.000 | 1.000 | 0.969    |
| 46         | 274.7              | 273.9              | 2.66              | 2.65              | 5.30                 | 1.000 | 1.000 | 0.982    |
| 47         | 263.5              | 259.8              | 2.50              | 2.46              | 4.92                 | 1.000 | 1.000 | 0.990    |
| 48         | 251.0              | 244.9              | 2.33              | 2.27              | 4.54                 | 1.000 | 1.000 | 0.996    |
| 49         | 237.2              | 229.1              | 2.16              | 2.08              | 4.16                 | 1.000 | 1.000 | 0.998    |
| 50         | 221.9              | 212.1              | 1.98              | 1.89              | 3.78                 | 1.000 | 1.000 | 1.000    |
| 51         | 204.6              | 193.6              | 1.79              | 1.69              | 3.38                 | 1.000 | 1.000 | 1.000    |
| 52         | 184.7              | 173.2              | 1.58              | 1.48              | 2.97                 | 1.000 | 1.000 | 1.000    |
| 53         | 161.5              | 150.0              | 1.36              | 1.26              | 2.52                 | 1.000 | 1.000 | 1.000    |
| 54         | 133.1              | 122.5              | 1.10              | 1.01              | 2.02                 | 1.000 | 1.000 | 1.000    |
| 55         | 95.0               | 86.6               | 0.77              | 0.70              | 1.40                 | 1.000 | 1.000 | 1.000    |

