

# Experimental cross sections and velocities of the light nuclides produced in the proton-induced fission of $^{238}\text{U}$ at 1 GeV

**M. VALENTINA RICCIARDI<sup>1</sup>**

K. -H. SCHMIDT<sup>1</sup>, F. REJMUND<sup>1</sup>, T. ENQVIST<sup>1</sup>, P. ARMBRUSTER<sup>1</sup>,  
J. BENLLIURE<sup>2</sup>,  
M. BERNAS<sup>3</sup>, B. MUSTAPHA<sup>3</sup>, L. TASSAN-GOT<sup>3</sup>,  
C. STEPHAN<sup>4</sup>, A. BOUDARD<sup>4</sup>, S. LERAY<sup>4</sup>, C. VOLANT<sup>4</sup>,  
S. CZAJKOWSKI<sup>5</sup>, M. PRAVIKOFF<sup>5</sup>

1 — GSI Darmstadt, Germany

2 — Universidad de Santiago de Compostela, Spain

3 — IPN Orsay, France

4 — DAPNIA / SPhN CEA / Saclay, France

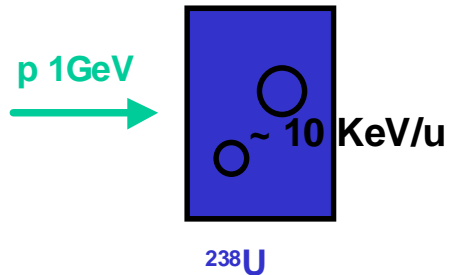
5 — CEN Bordeaux, France

**PART I:**

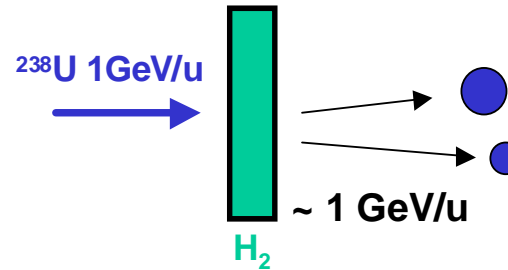
**EXPERIMENT AND RESULTS**

# THE EXPERIMENT: 1 A·GeV $^{238}\text{U} \rightarrow \text{p}$

direct kinematics



inverse kinematics



Advantages of the inverse kinematics:

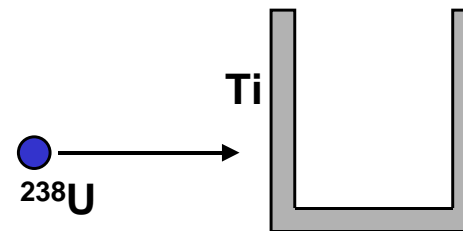
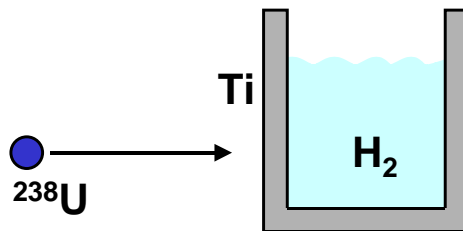
↓ complete identification

↓ knowledge of the kinematics

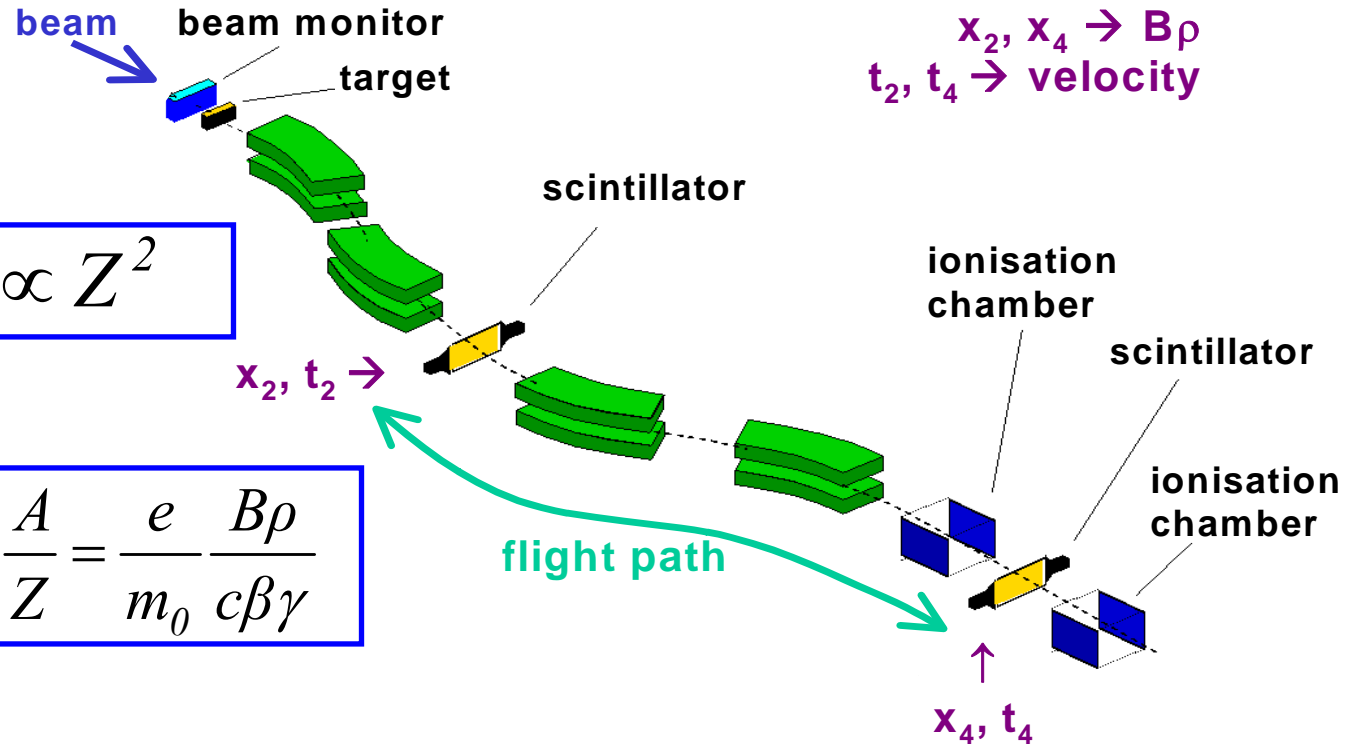
Disadvantage:

↓ I need a  $\text{H}_2$  target

Background experiment  $^{238}\text{U}$  on Ti



# THE FRS AT GSI AND THE EXPERIMENTAL SET-UP for LIGHT RESIDUES



$$Z \text{ from IC: } \Delta E \propto Z^2$$

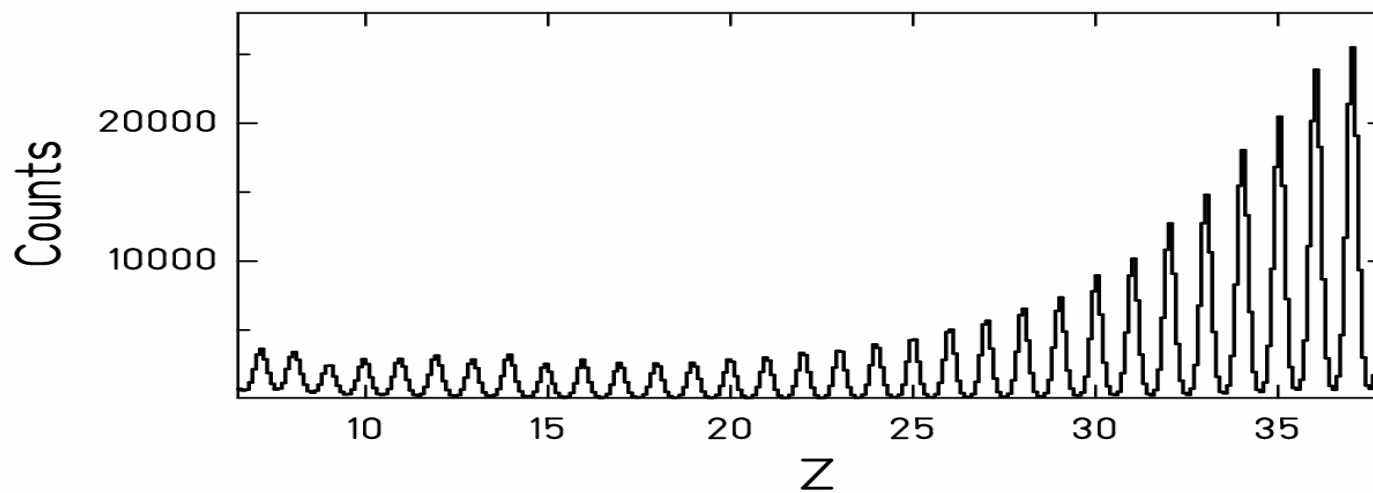
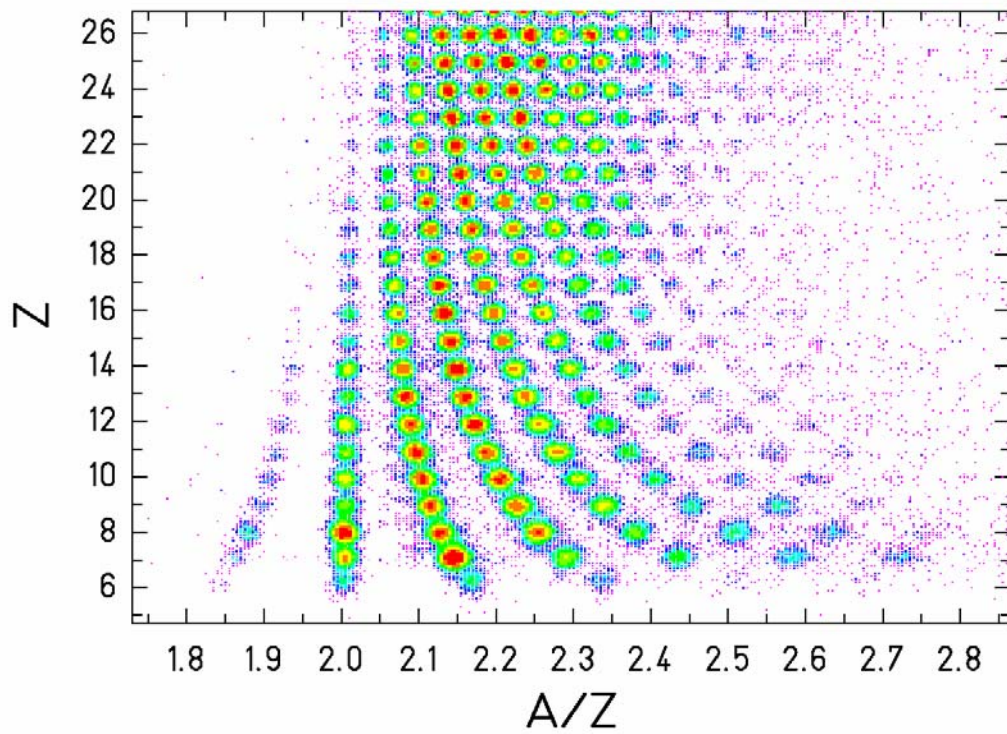
$$A/Z \text{ from time and position: } \frac{A}{Z} = \frac{e}{m_0} \frac{B\rho}{c\beta\gamma}$$

Once mass and charge are identified ( $A, Z$  are integer numbers)  
the **velocity** is calculated from  $B\rho$ :

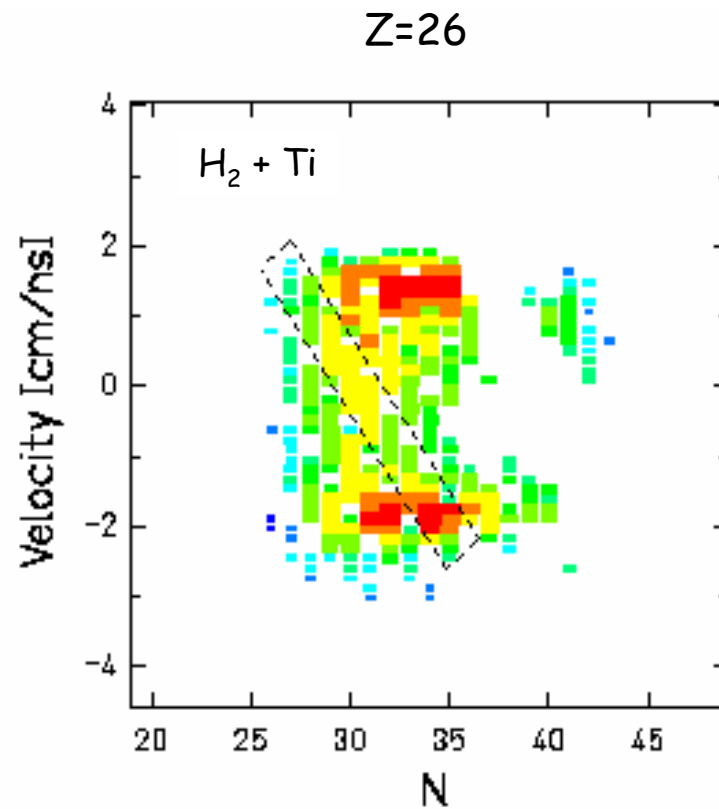
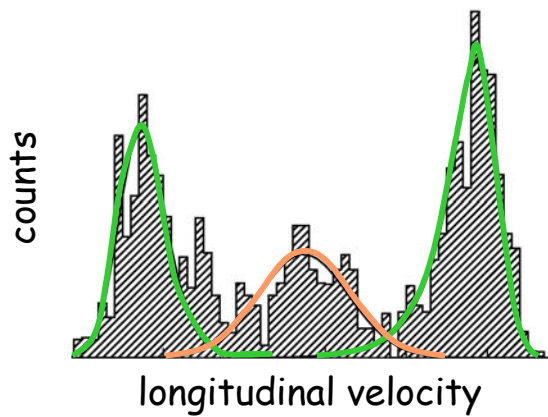
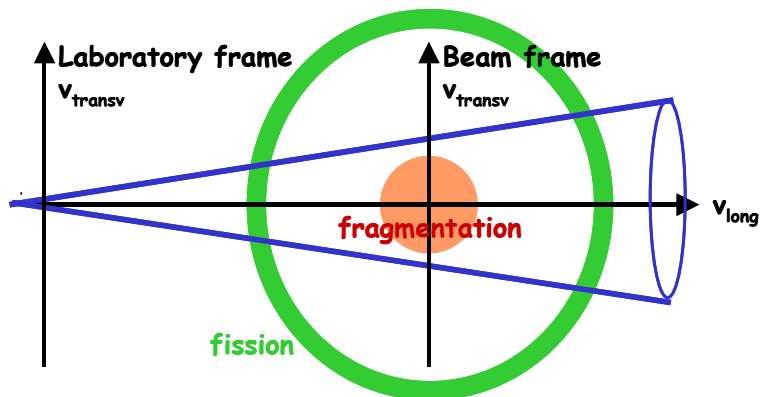
very precise evaluation!

$$\beta\gamma c = \frac{e}{m_0} \cdot \frac{A}{Z} \cdot B\rho$$

# RESOLUTION

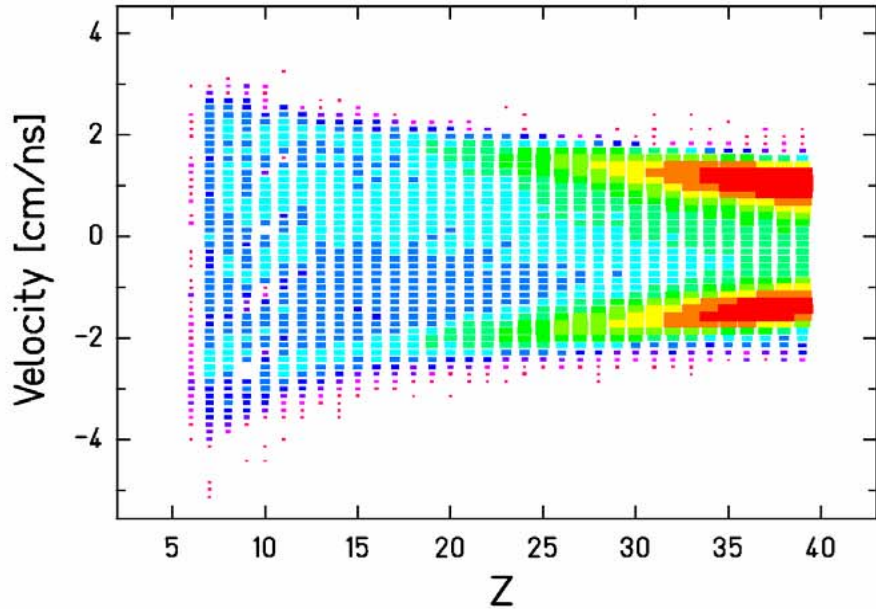


# DISCRIMINATION OF FISSION EVENTS

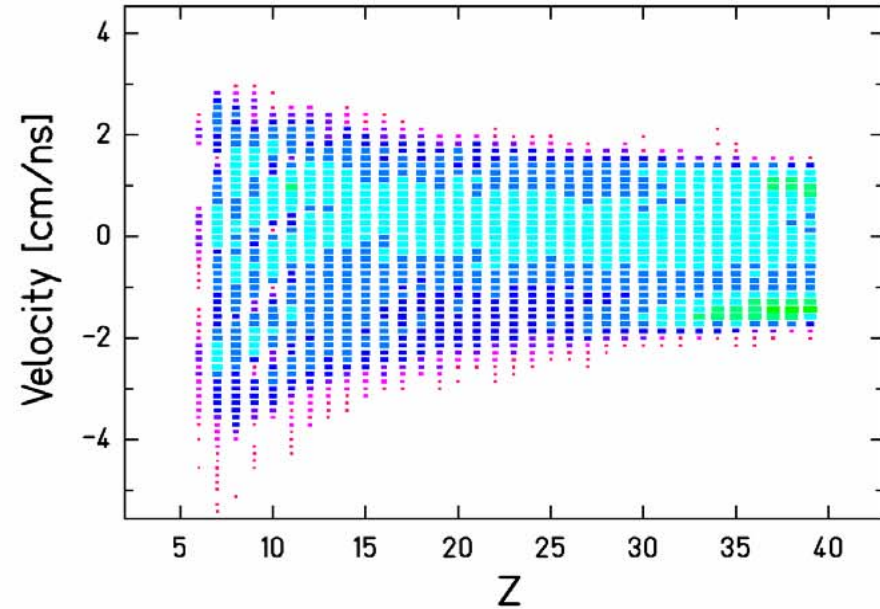


# VELOCITY OF ALL RESIDUES

hydrogen+titanium

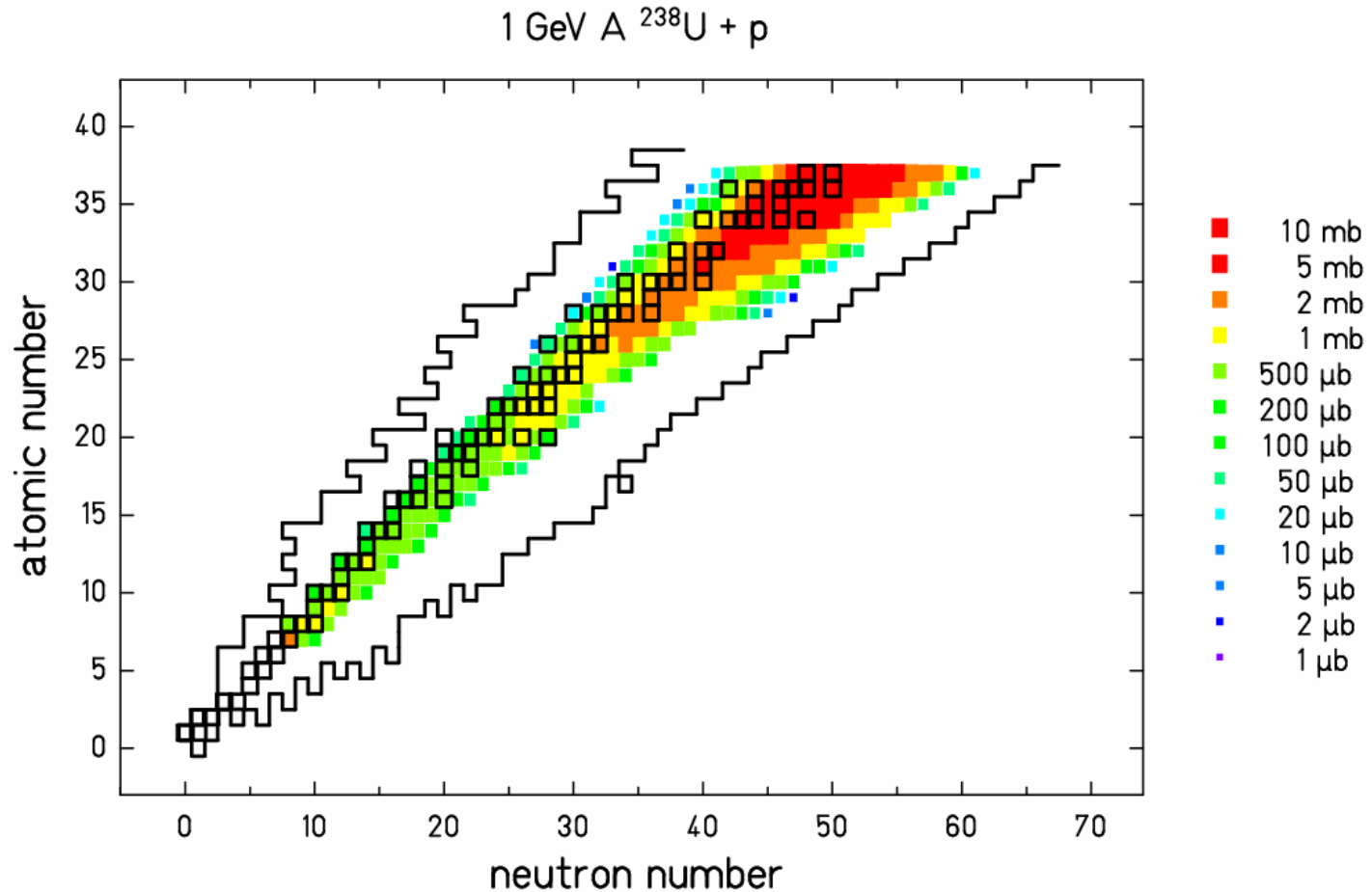


titanium alone



Evidence for a "binary" decay

# CROSS SECTIONS OF THE LIGHT RESIDUES



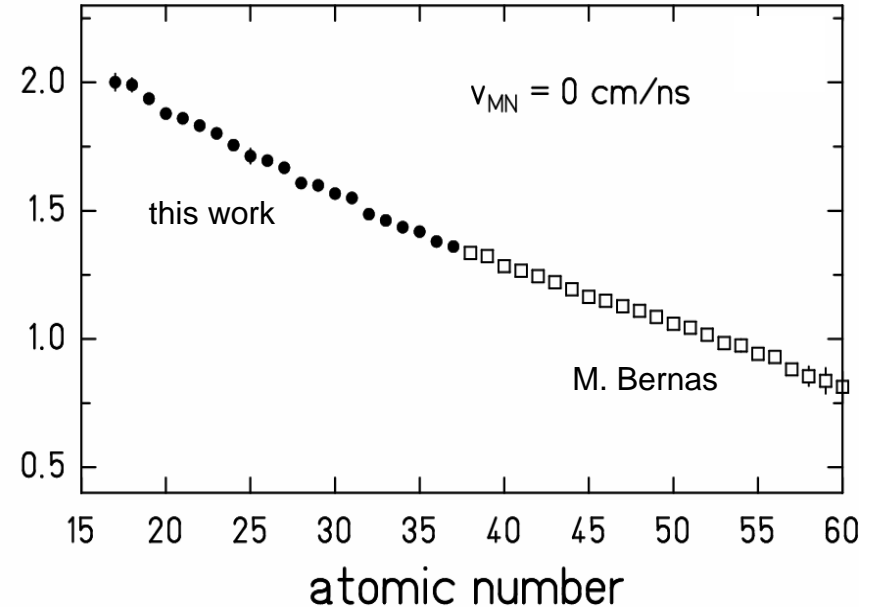
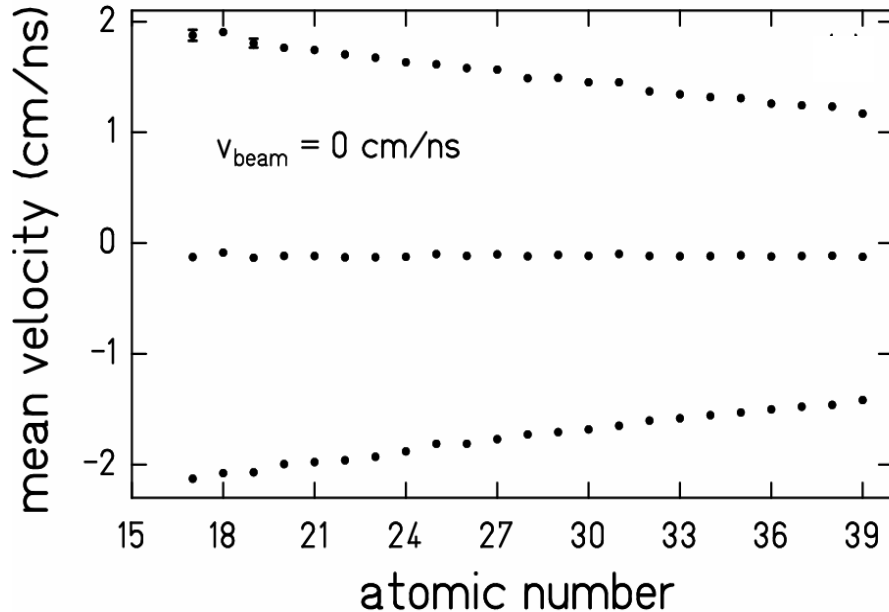
Data available at: <http://www-w2k.gsi.de/charms/data.htm>



**PART II:**

**INTERPRETATION OF THE  
EXPERIMENTAL RESULTS**

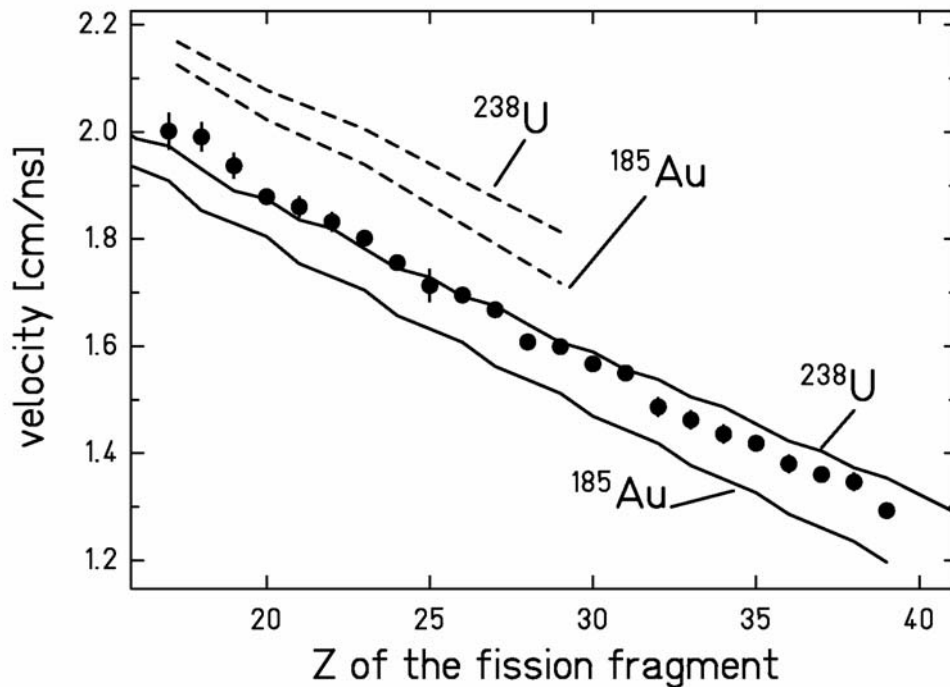
# VELOCITY OF THE RESIDUES



We can interpret the counts in the two wings as very asymmetric fission products in proton-induced reactions on  $^{238}\text{U}$

# TRANSITION FROM FISSION TO EVAPORATION

Velocity: from scission-point model towards  
asymmetric decay from undeformed nucleus



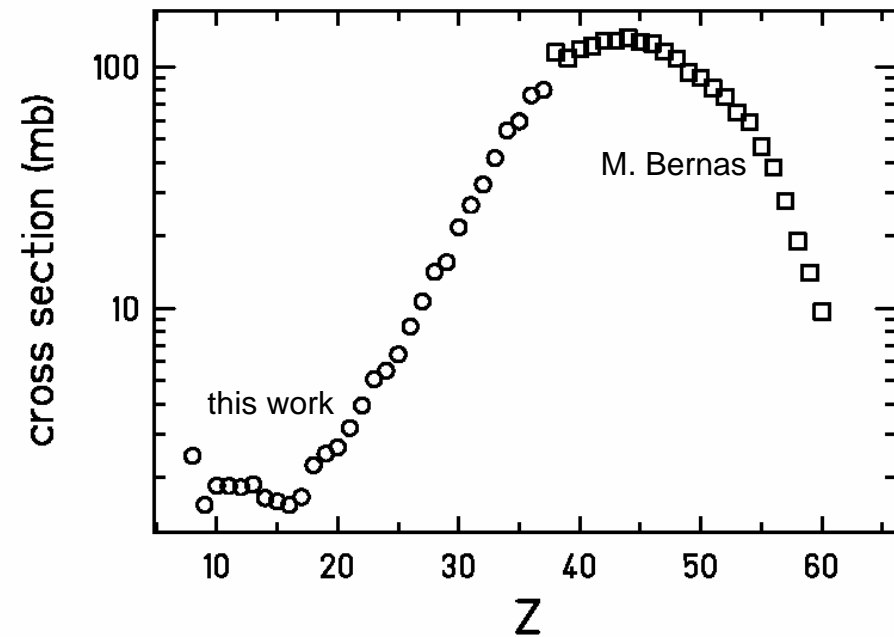
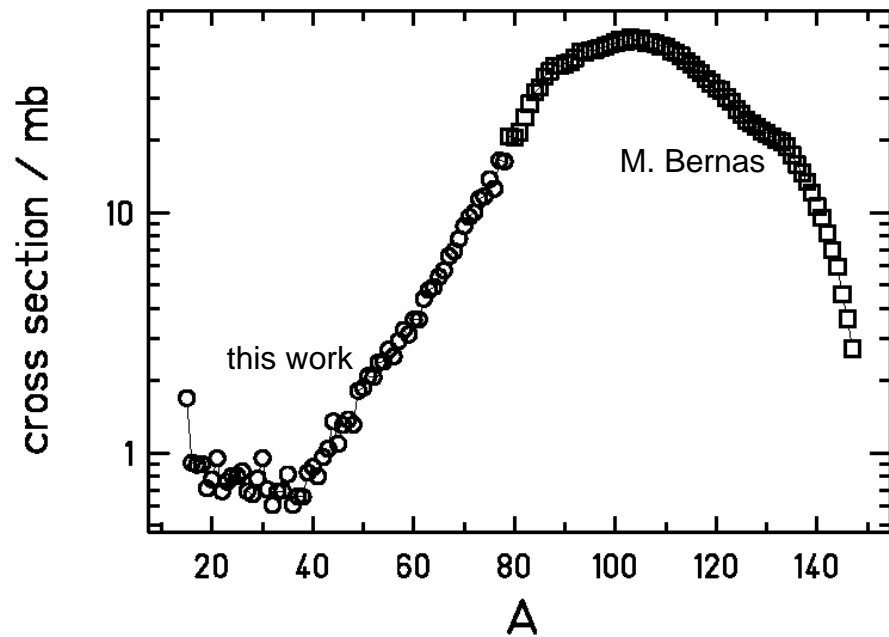
- Mean velocities in the frame of the fissioning nucleus

$^{238}\text{U}$ ,  $^{185}\text{Au}$  = compound nuclei

— scission-point model  
(deformed nuclei)

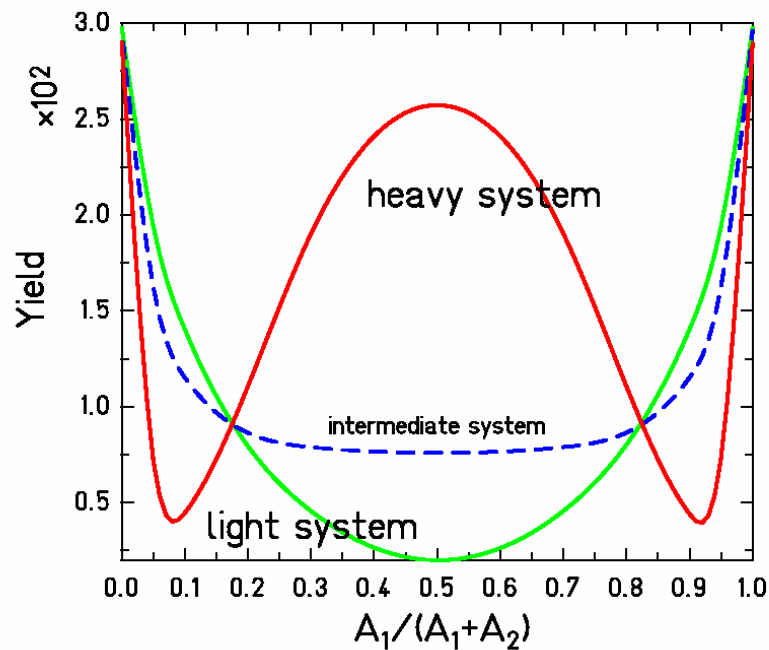
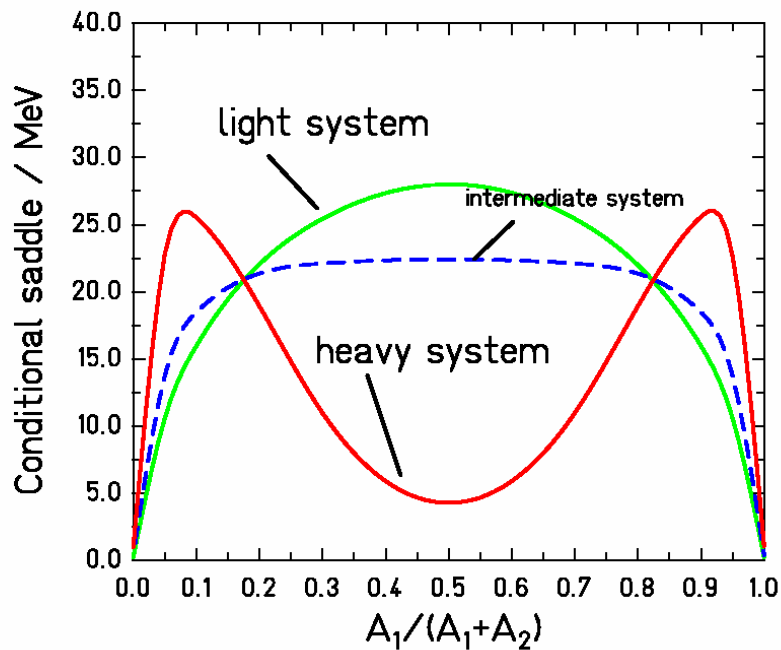
- - - Nucleus-nucleus fusion  
approach (undeformed nuclei)

# CROSS SECTIONS: MASS AND CHARGE DISTRIBUTIONS

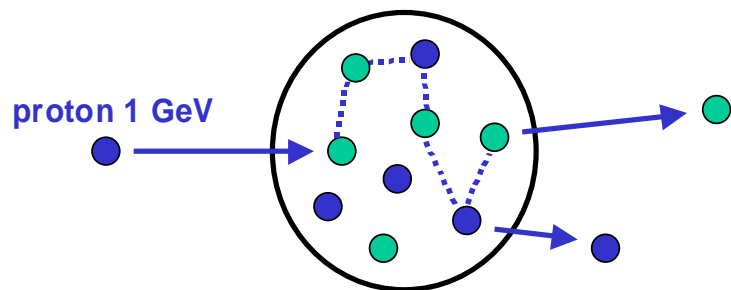


# TRANSITION FROM FISSION TO EVAPORATION

Mass distribution: the statistical transition-state model

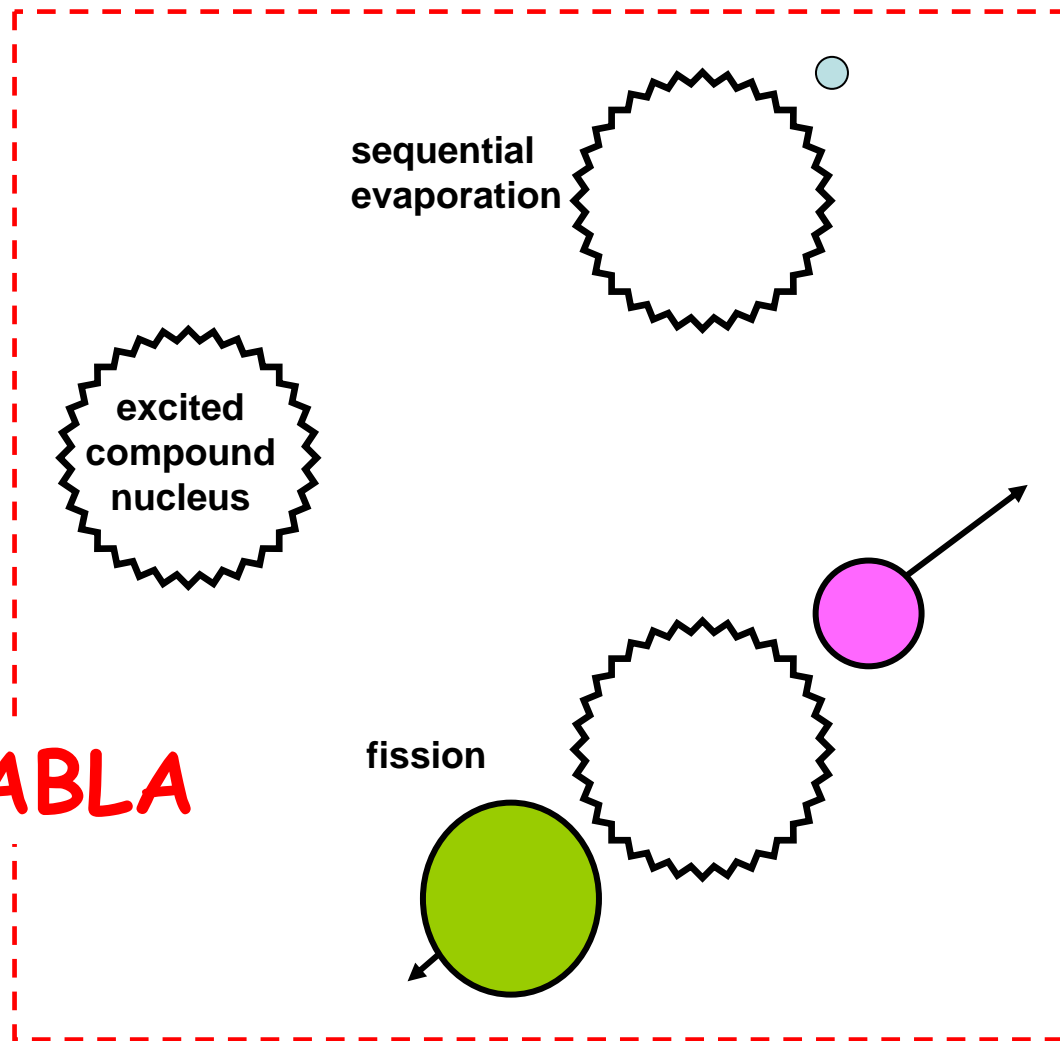


# OUR STATISTICAL MODEL



Intra-nuclear Cascade

**ABLA**



# THE FISSION MODEL: THE FISSION PROBABILITIES

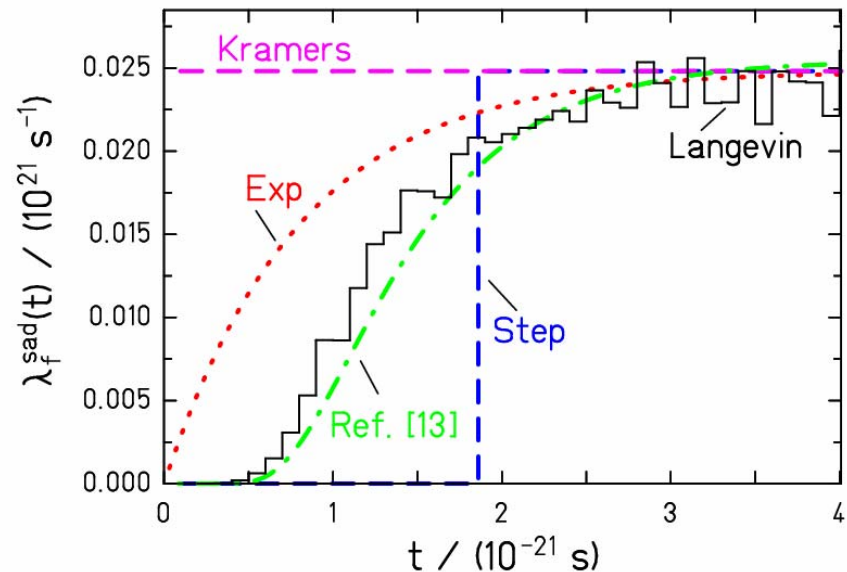
Fission decay  
width: transition-  
state method of  
Bohr and Wheeler

$$\Gamma_f^{BW} \approx T_f \frac{\rho_f(E - B_f)}{\rho_C(E)}$$

level density of the  
compound nucleus

level density of the  
transition states in  
the saddle-point  
configuration

The fission decay  
widths depend  
explicitly on time  
(dynamical evolution of  
the system along its  
path to fission)  
(influence of nuclear  
viscosity)



# THE FISSION MODEL: THE FISSION-FRAGMENT PROPERTIES (SEMIEMPIRICAL)

*J. Benlliure et al. / Nuclear Physics A 628 (1998) 458–478*

The modeling of  
the potential  
for very  
asymmetric  
fission is  
missing

We use another  
approach...

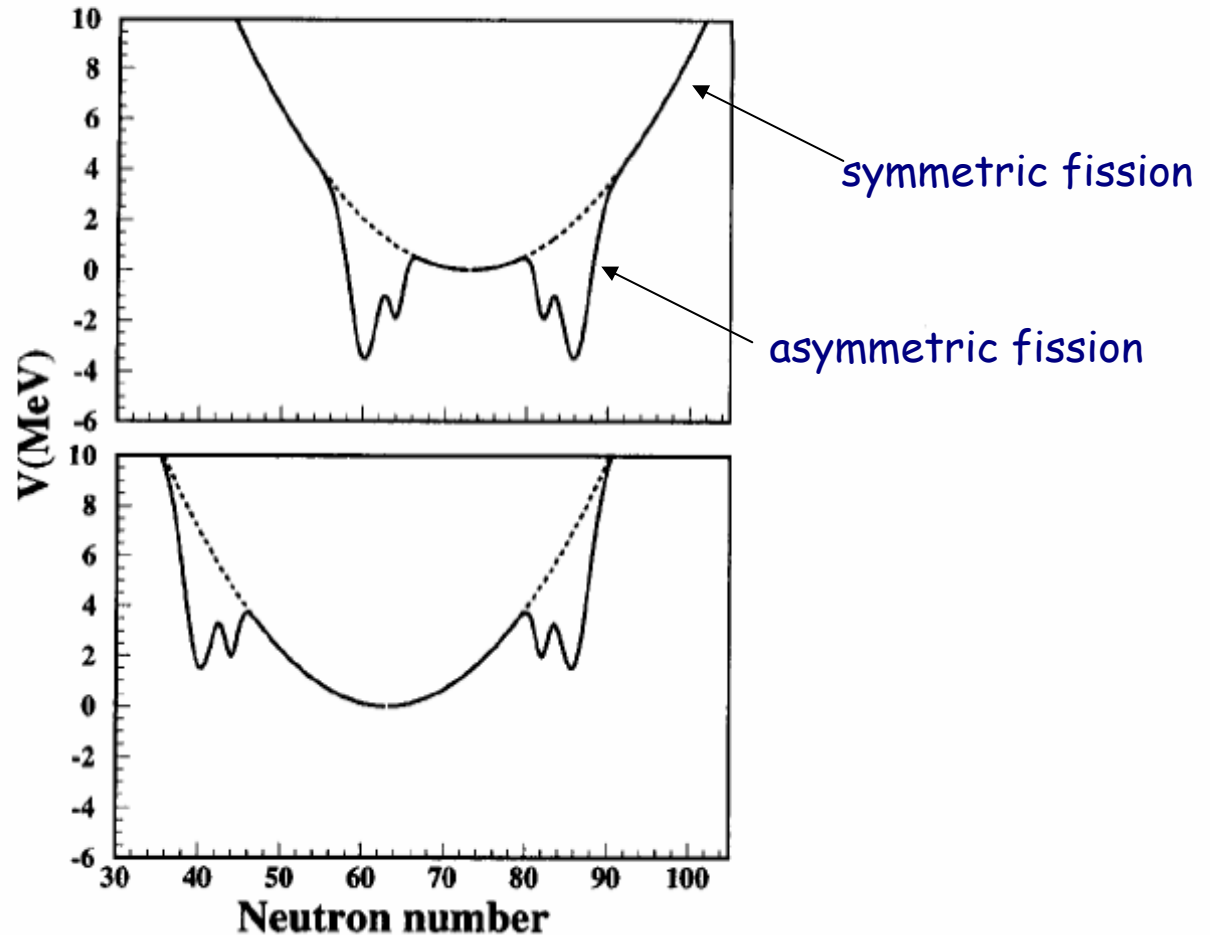


Fig. 1. Potential energy at the fission barrier for  $^{238}\text{U}$  (upper part) and  $^{208}\text{Pb}$  (lower part), as a function of mass asymmetry expressed by the neutron number of one of the preformed fragments.



# THE VERY ASYMMETRIC FISSION: THE INTERMEDIATE-MASS FRAGMENT EMISSION

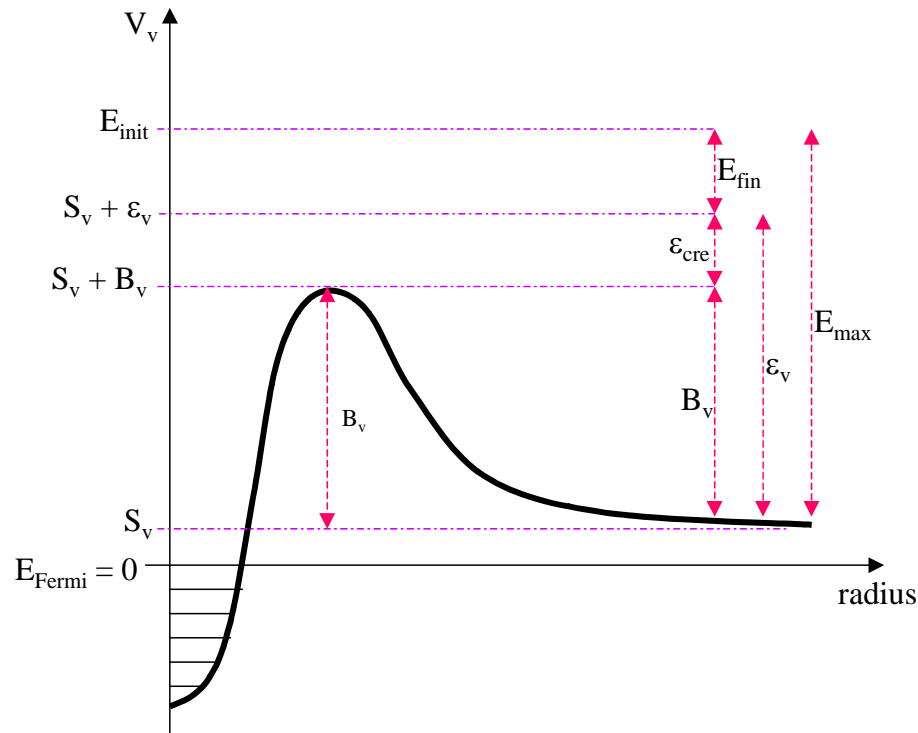
IMF decay width

$$\Gamma_{IMF} \approx \sigma_{inv} T_M^2 \frac{\rho_M(E - B_{IMF})}{\rho_C(E)}$$

level density of the  
compound nucleus

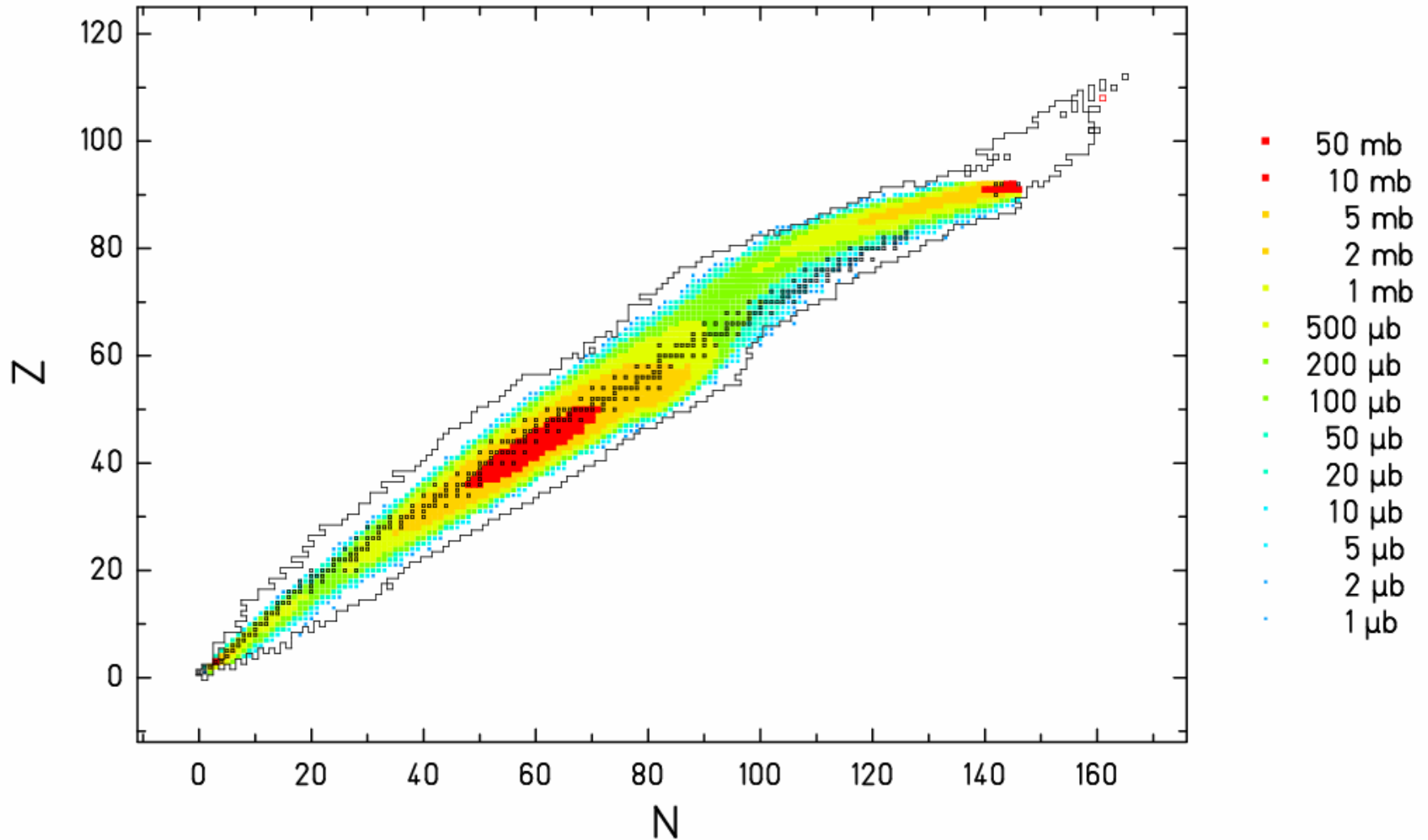
level density of the  
mother  
nucleus at the  
barrier

The barrier is  
calculated using  
the fusion  
nuclear  
potential of  
Bass

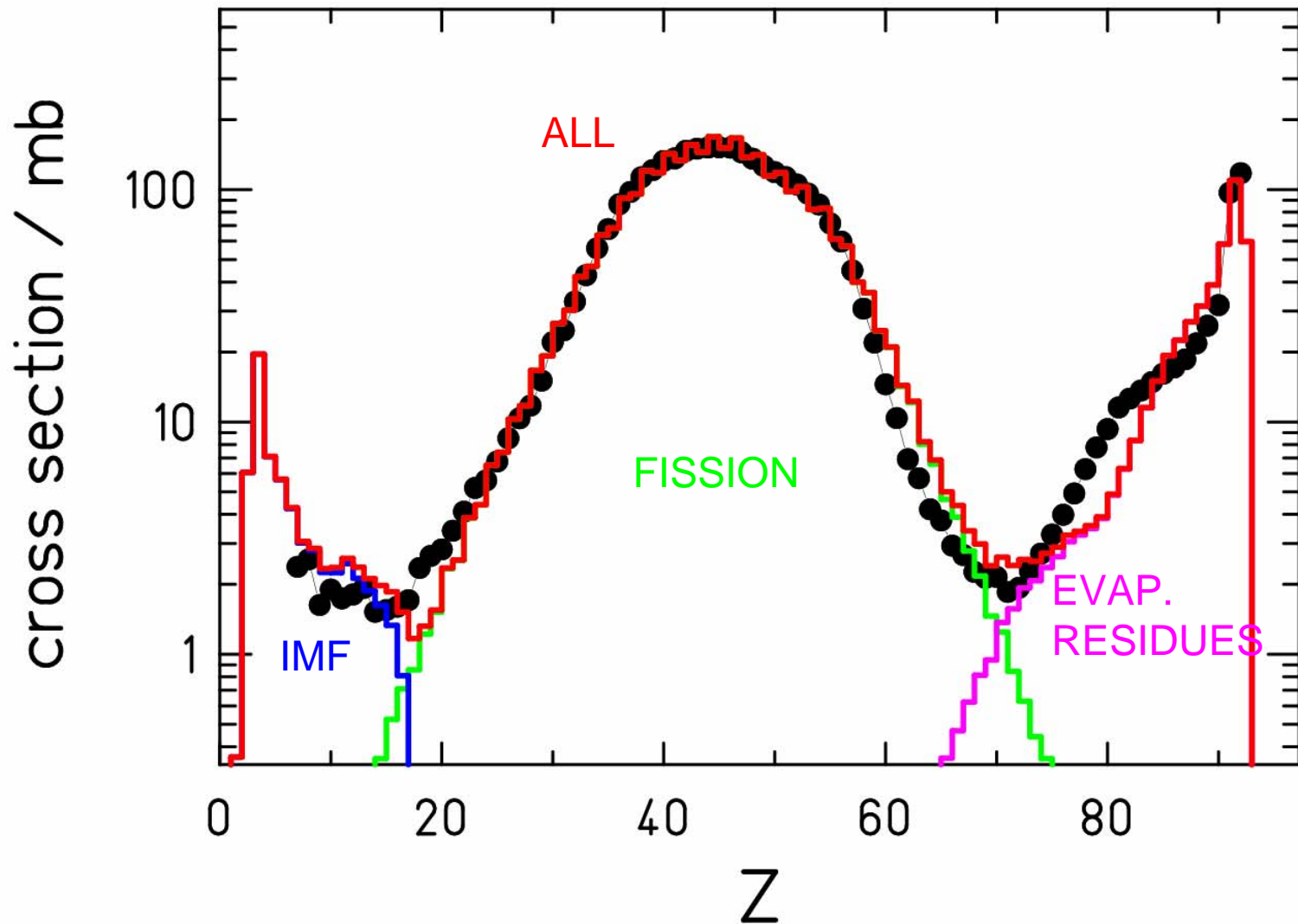


# RESULT FOR 1 GeV p on $^{238}\text{U}$

INCL+ABLA 1 GeV p on  $^{238}\text{U}$

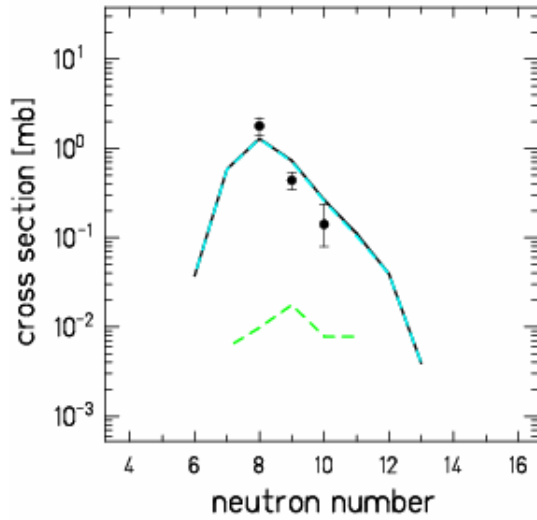


# RESULT FOR 1 GeV p on $^{238}\text{U}$

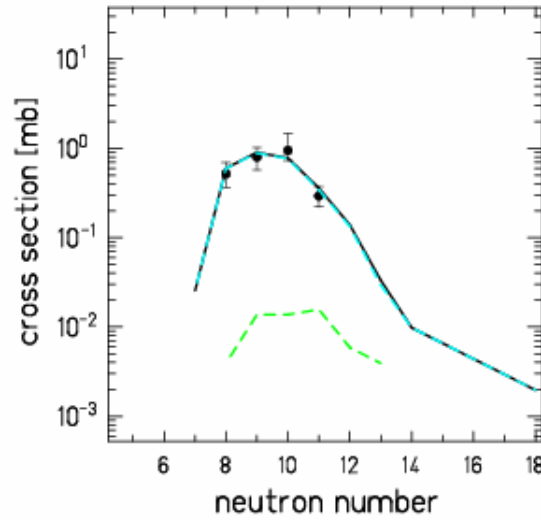


# RESULT FOR 1 GeV p on $^{238}\text{U}$

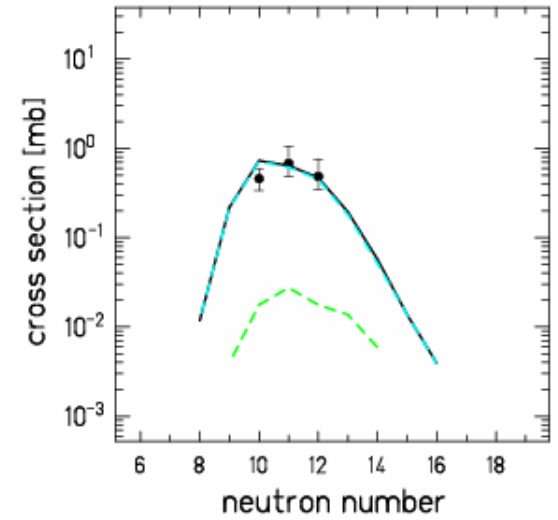
Z = 7



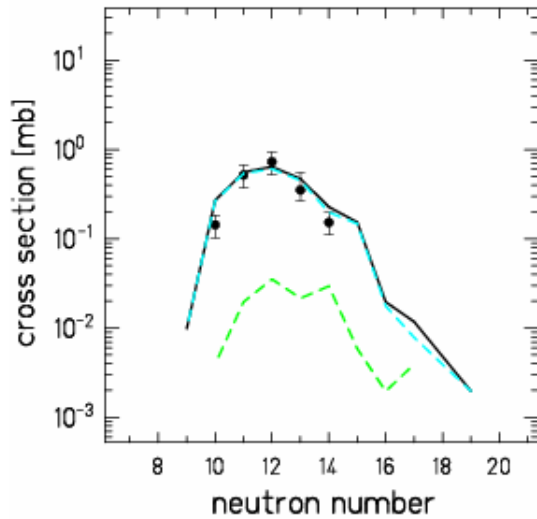
Z = 8



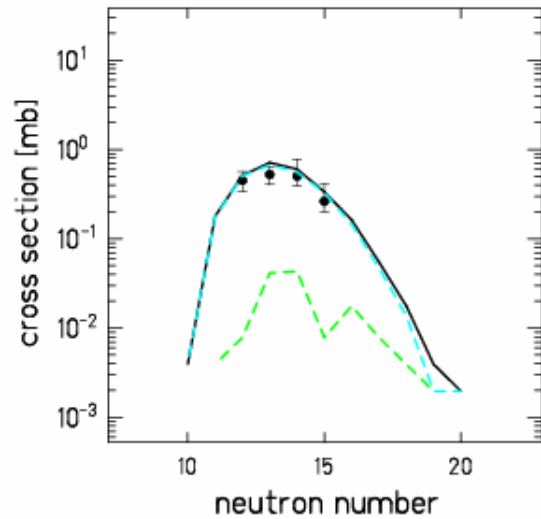
Z = 9



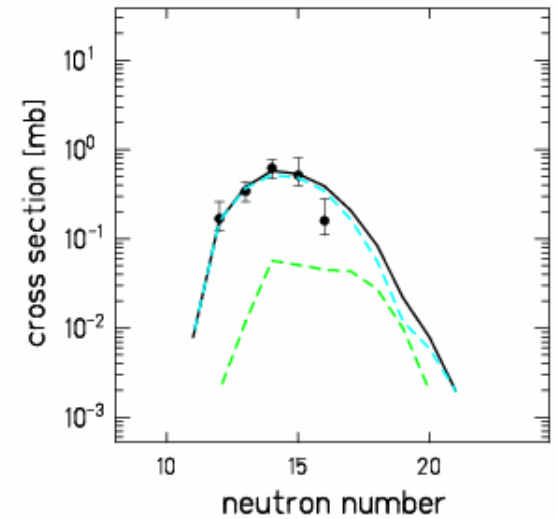
Z = 10



Z = 11

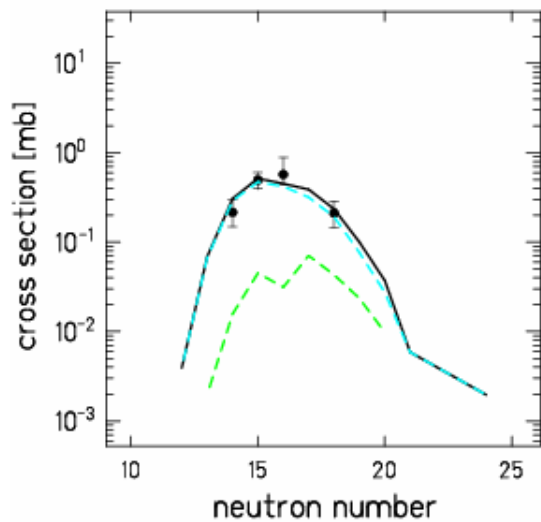


Z = 12

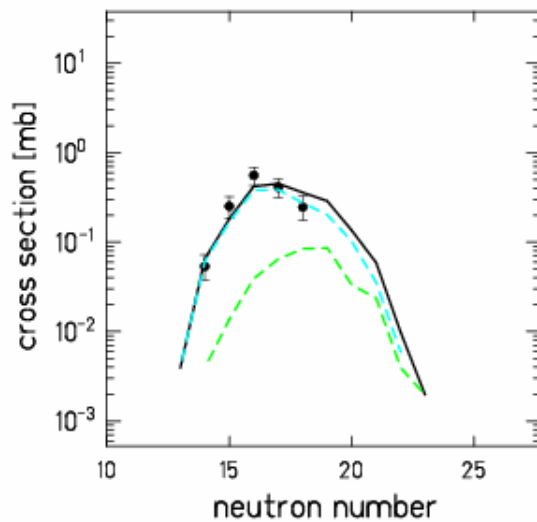


# RESULT FOR 1 GeV p on $^{238}\text{U}$

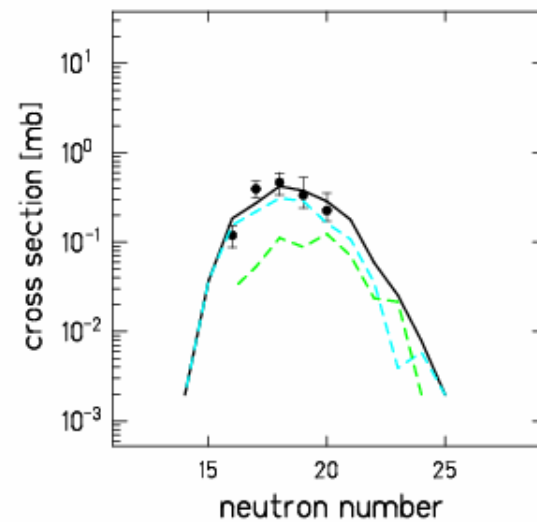
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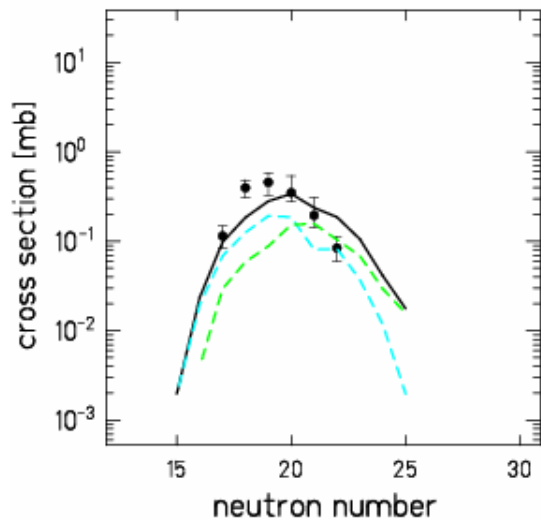
Z = 14



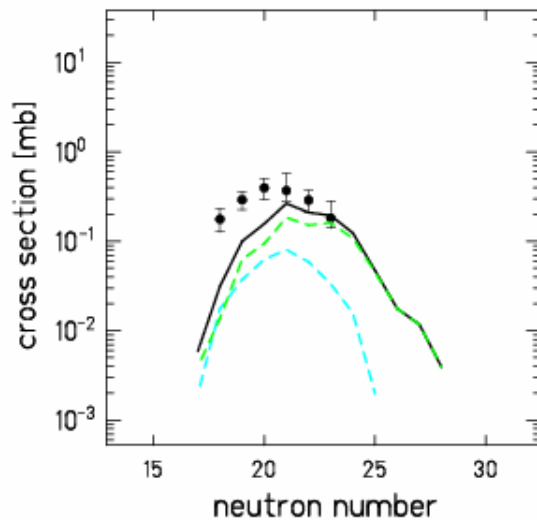
Z = 15



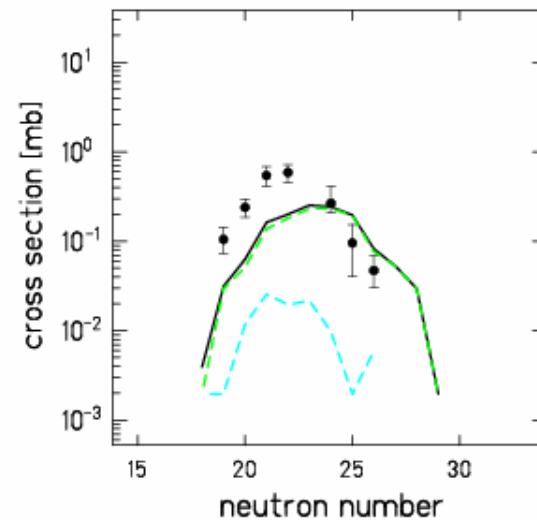
Z = 16



Z = 17

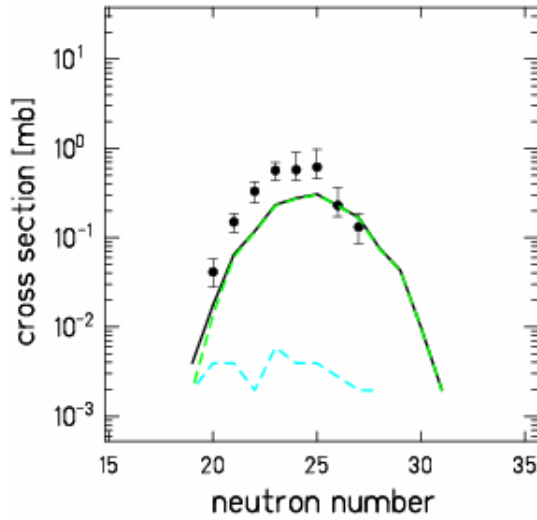


Z = 18

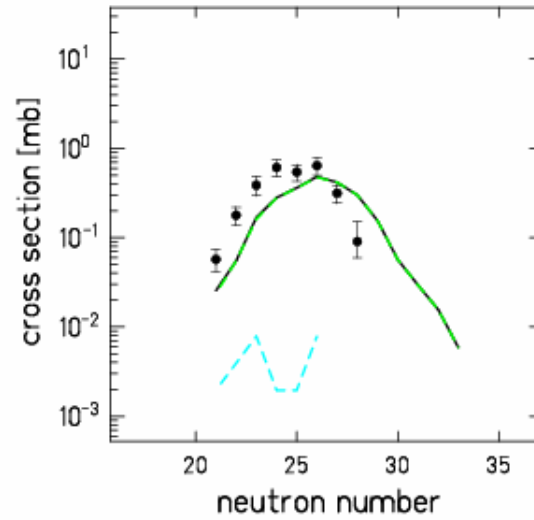


# RESULT FOR 1 GeV p on $^{238}\text{U}$

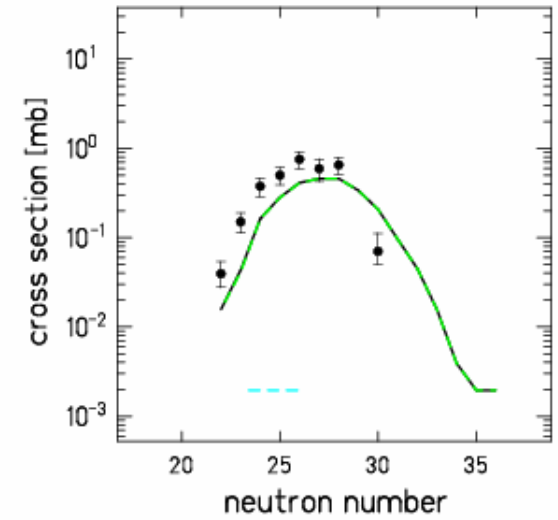
Z = 19



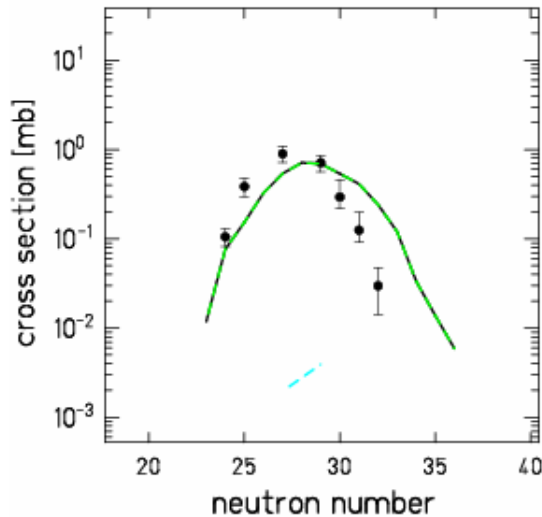
Z = 20



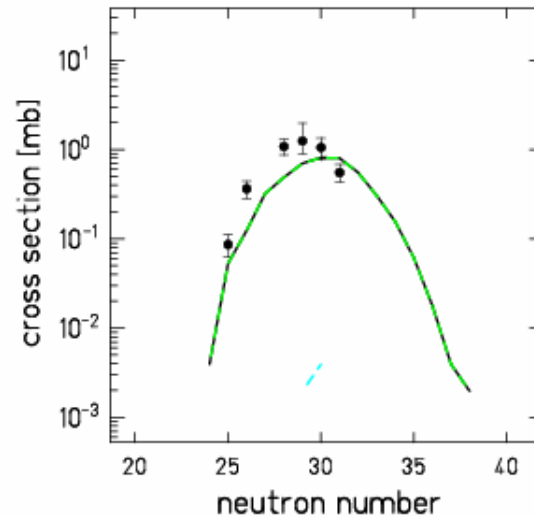
Z = 21



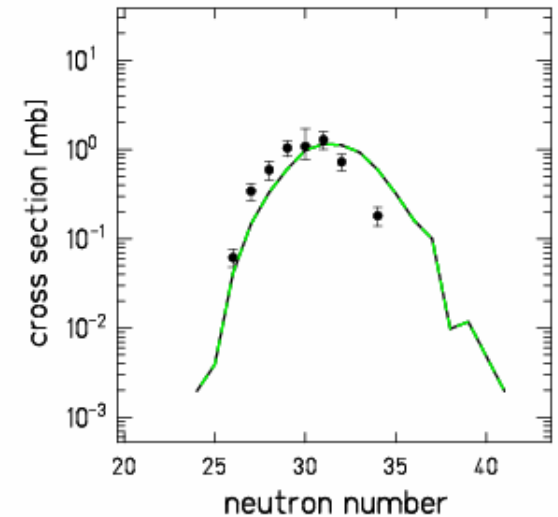
Z = 22



Z = 23

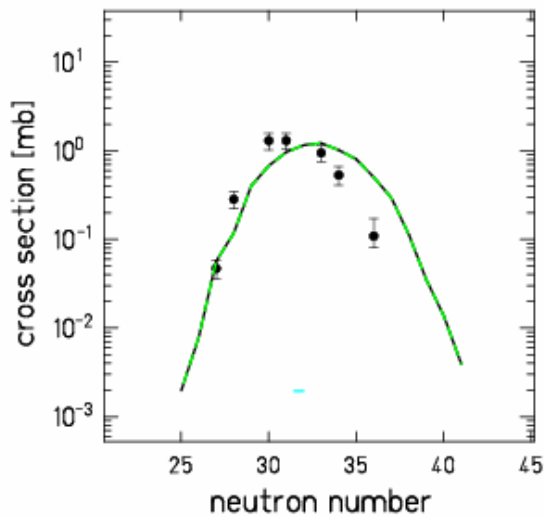


Z = 24

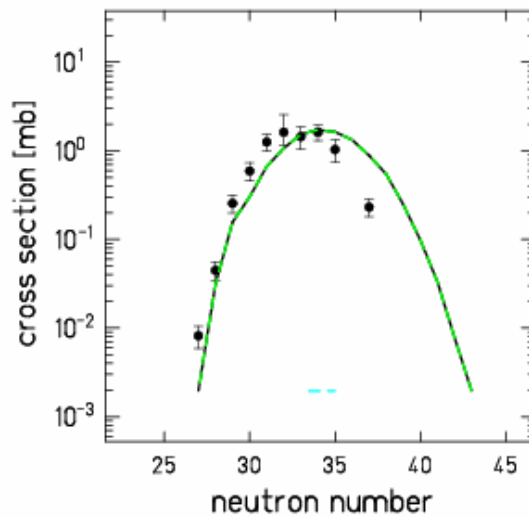


# RESULT FOR 1 GeV p on $^{238}\text{U}$

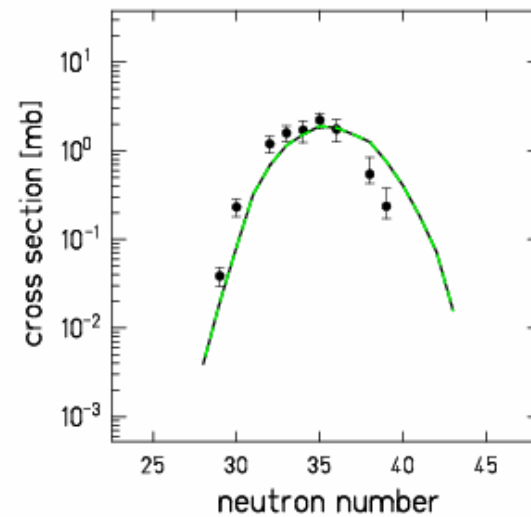
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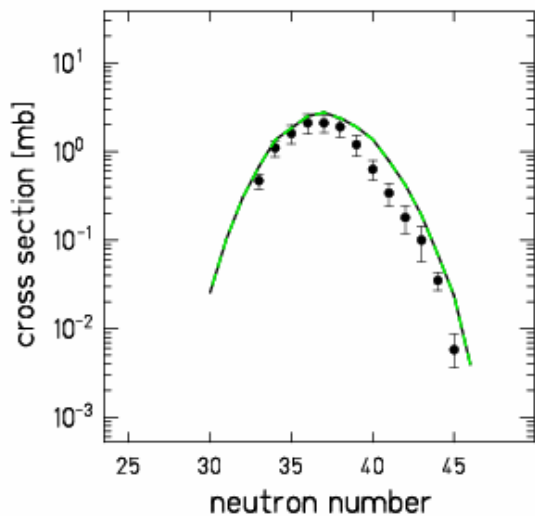
Z = 26



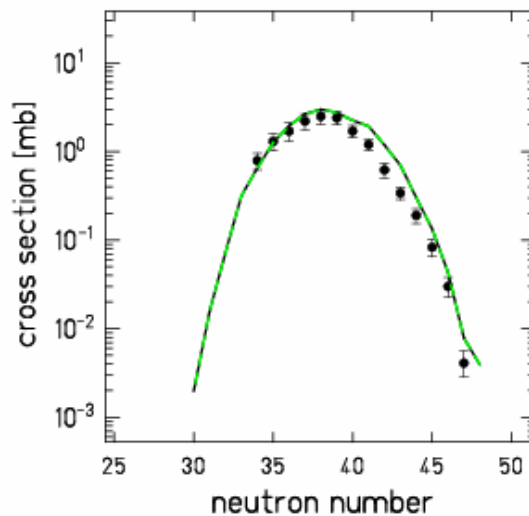
Z = 27



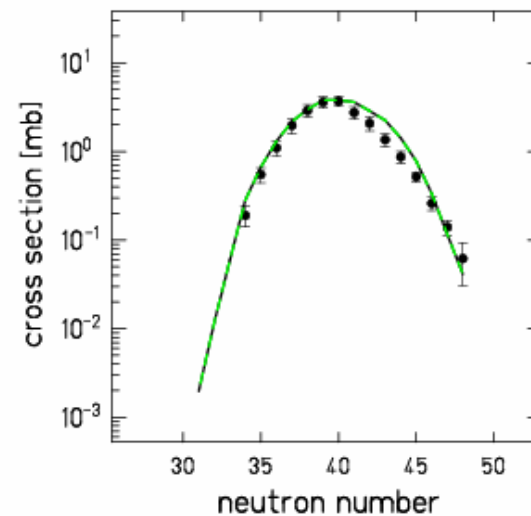
Z = 28



Z = 29

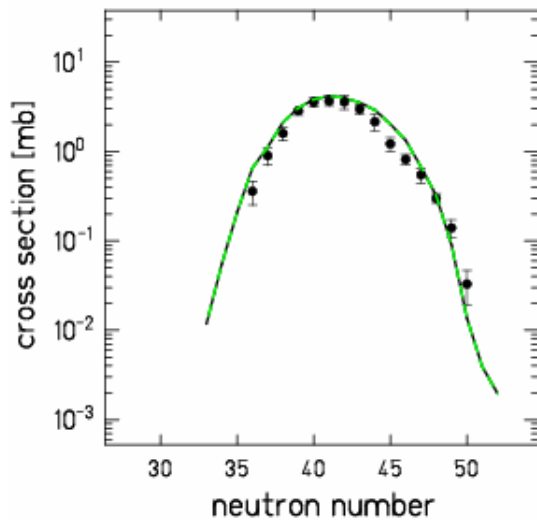


Z = 30

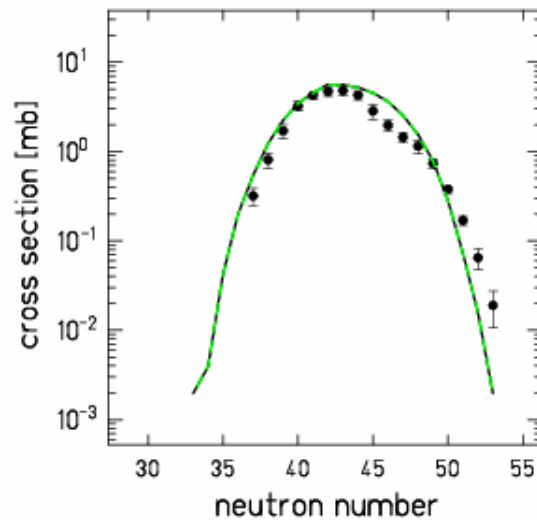


# RESULT FOR 1 GeV p on $^{238}\text{U}$

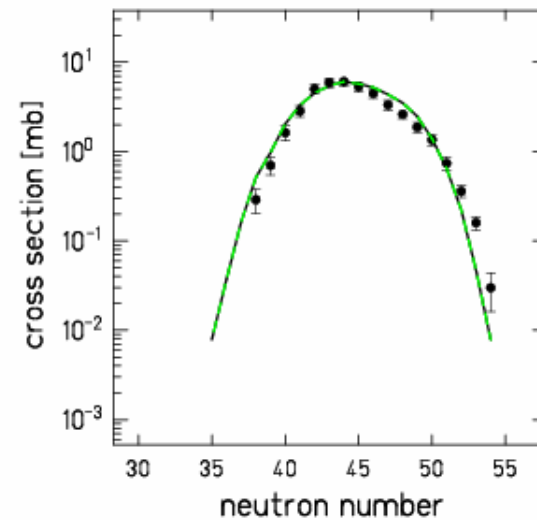
Z = 31



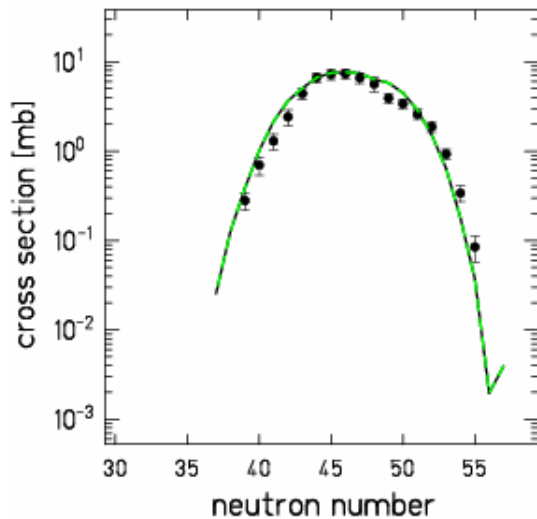
Z = 32



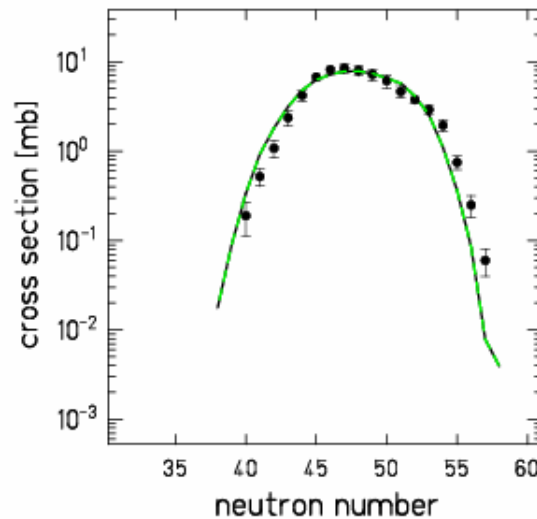
Z = 33



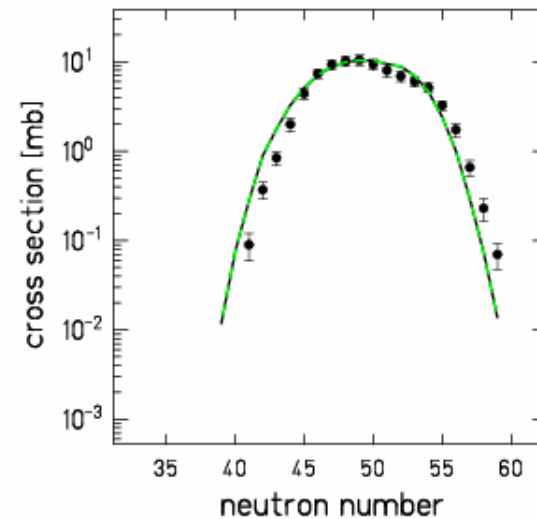
Z = 34



Z = 35



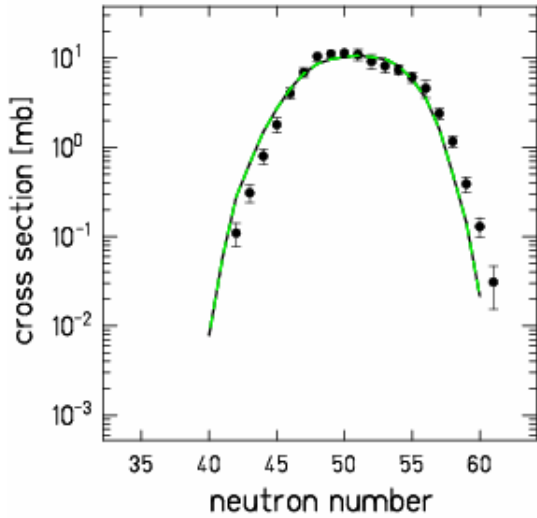
Z = 36



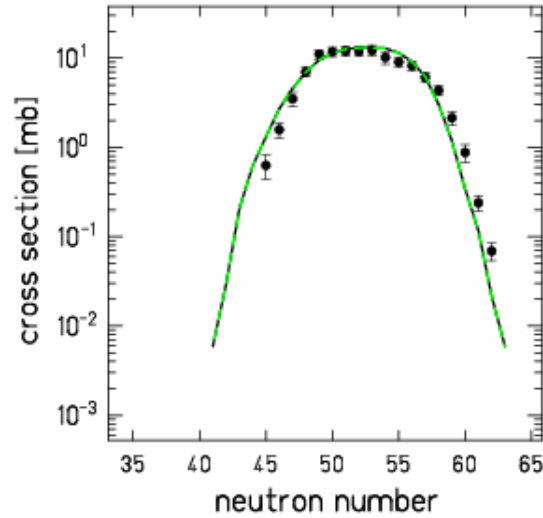


# RESULT FOR 1 GeV p on $^{238}\text{U}$

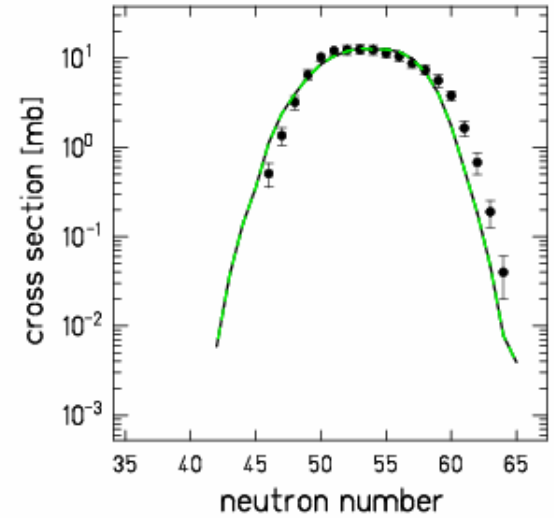
Z = 37



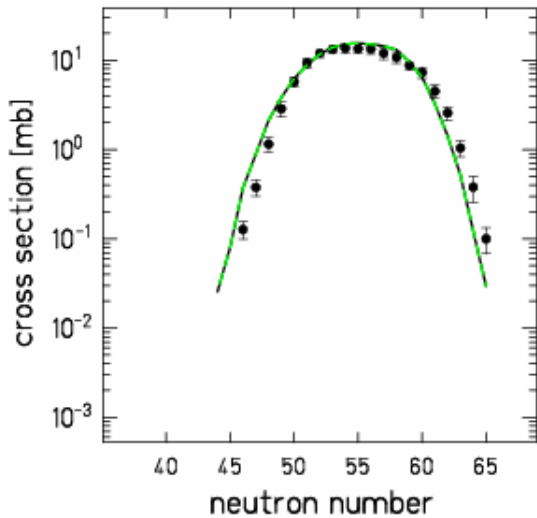
Z = 38



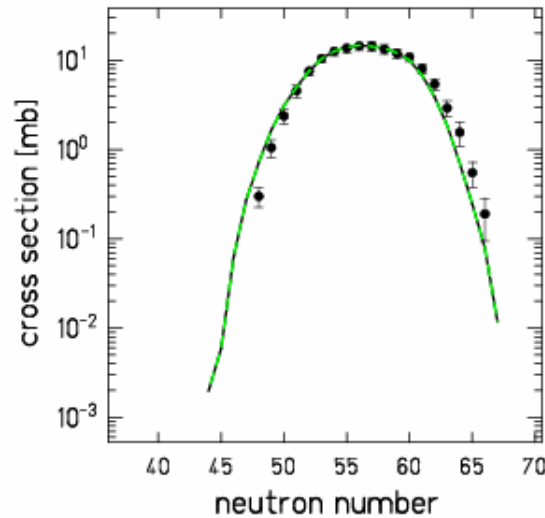
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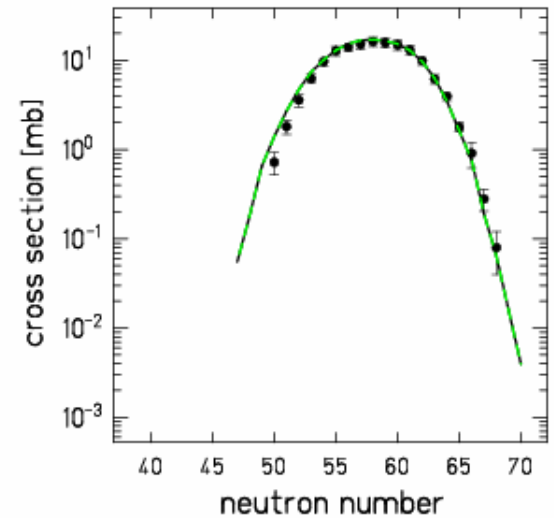
Z = 40



Z = 41

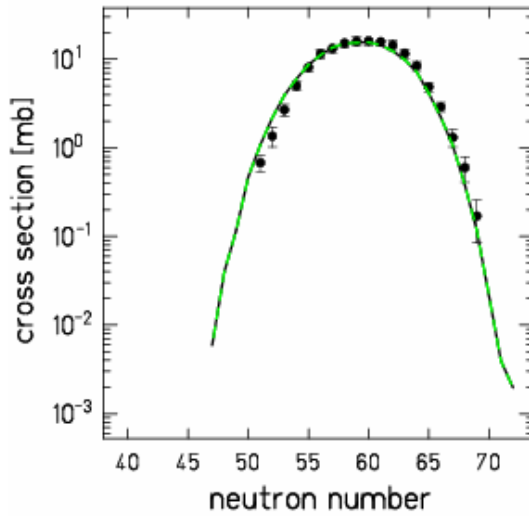


Z = 42

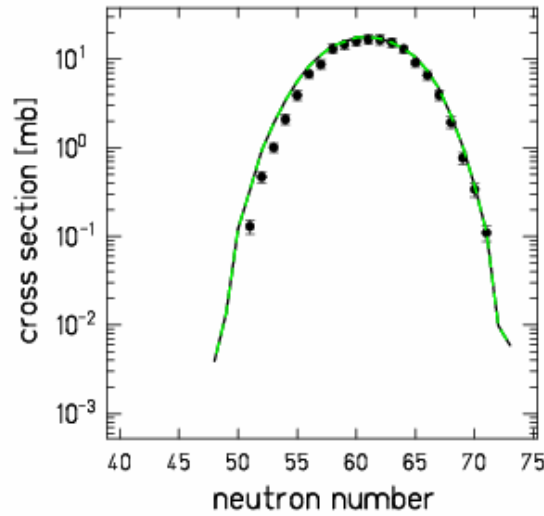


# RESULT FOR 1 GeV p on $^{238}\text{U}$

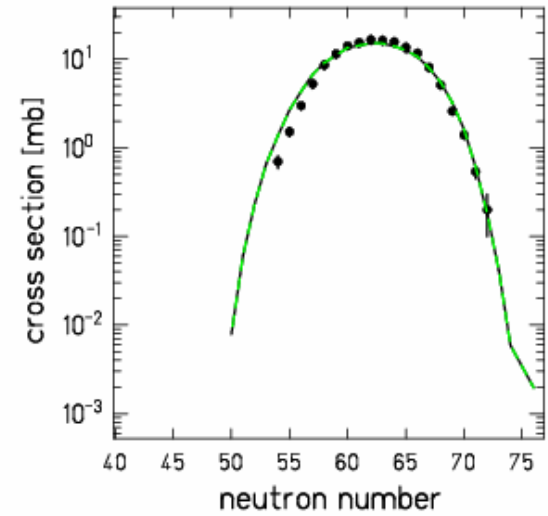
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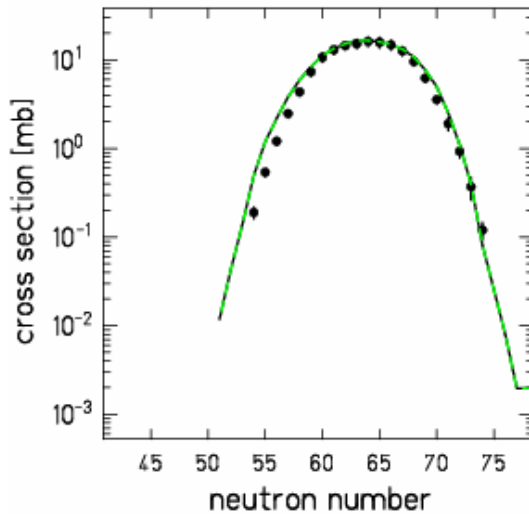
Z = 44



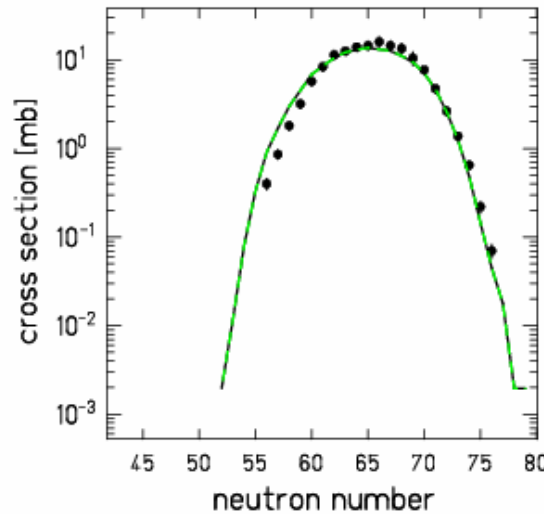
Z = 45



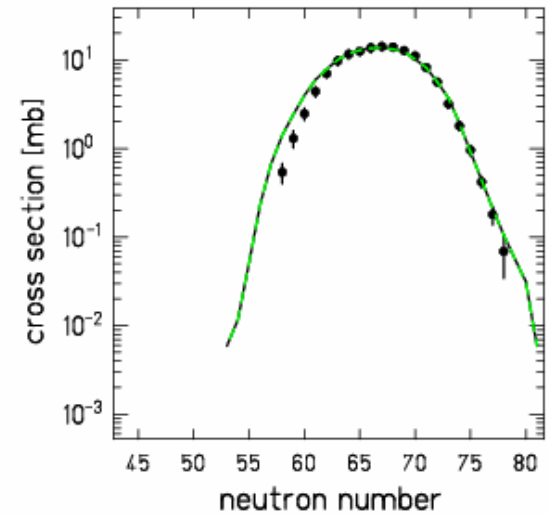
Z = 46



Z = 47

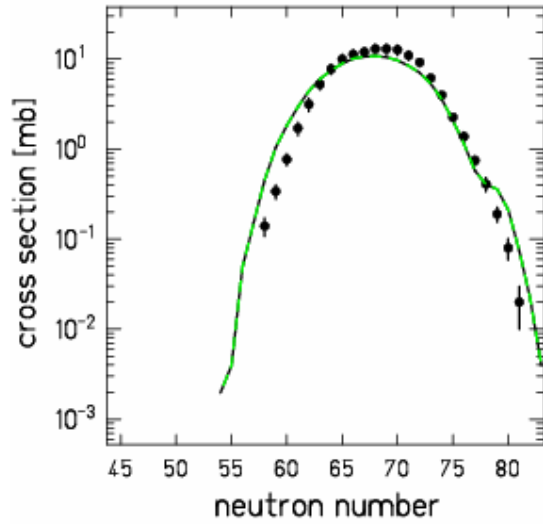


Z = 48

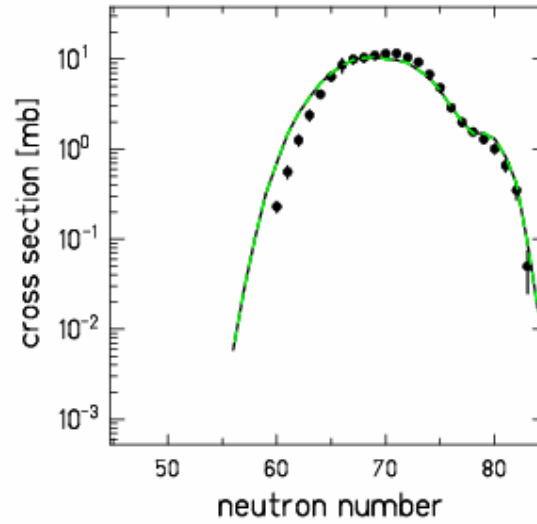


# RESULT FOR 1 GeV p on $^{238}\text{U}$

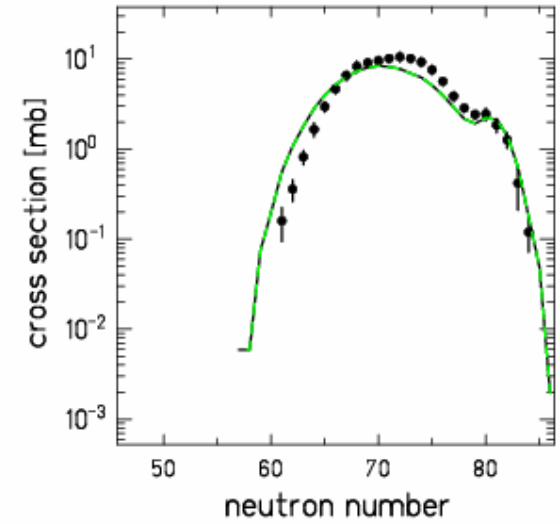
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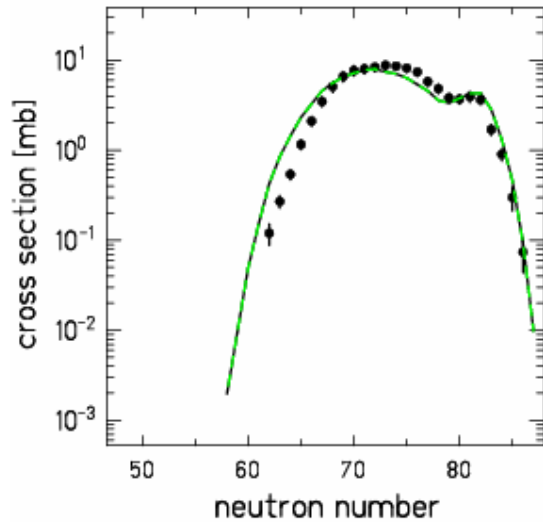
Z = 50



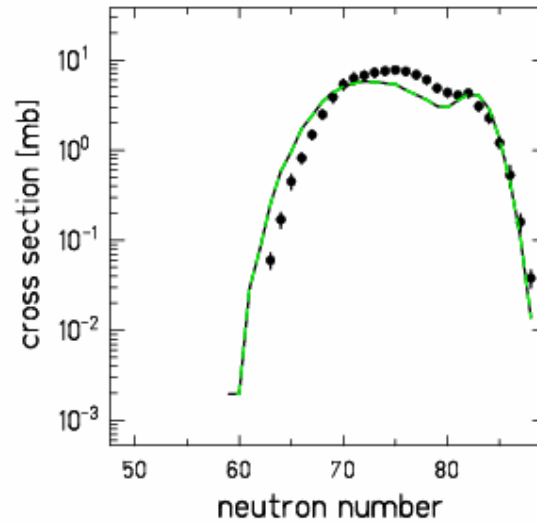
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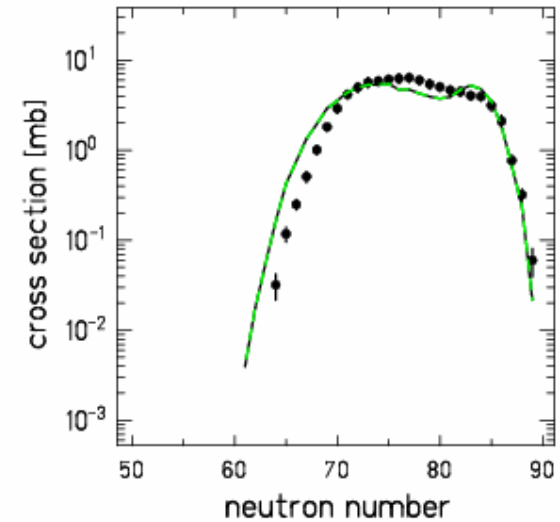
Z = 52



Z = 53

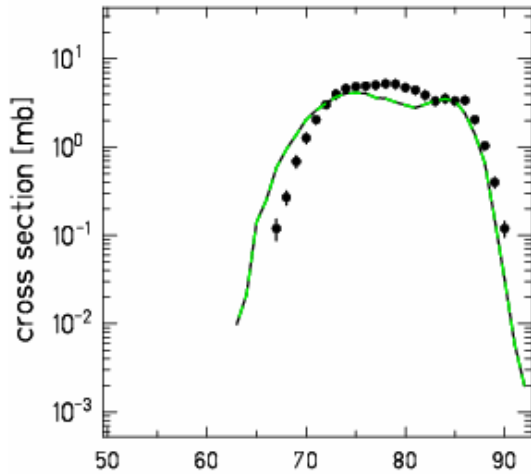


Z = 54



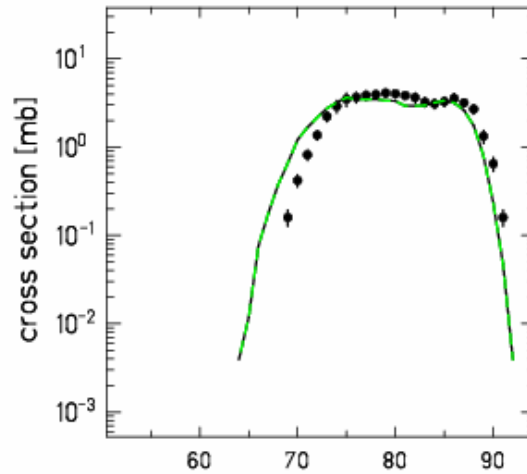
# RESULT FOR 1 GeV p on $^{238}\text{U}$

Z = 55



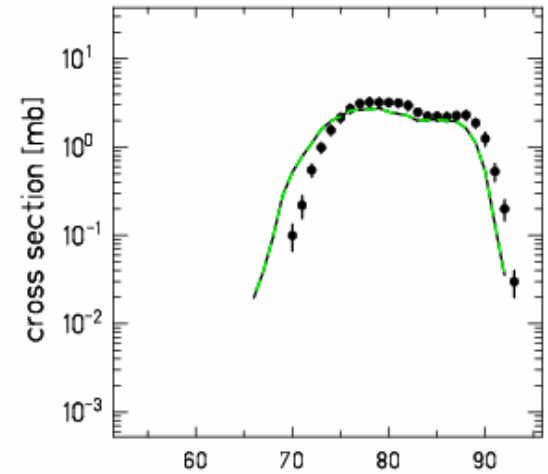
neutron number

Z = 56



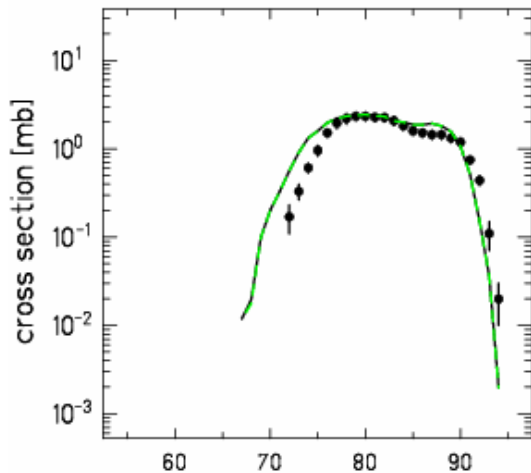
neutron number

Z = 57



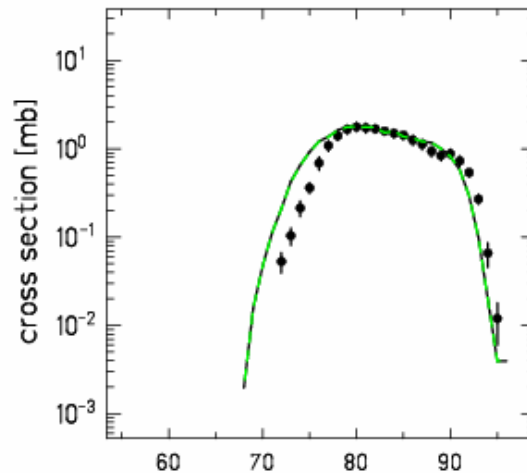
neutron number

Z = 58



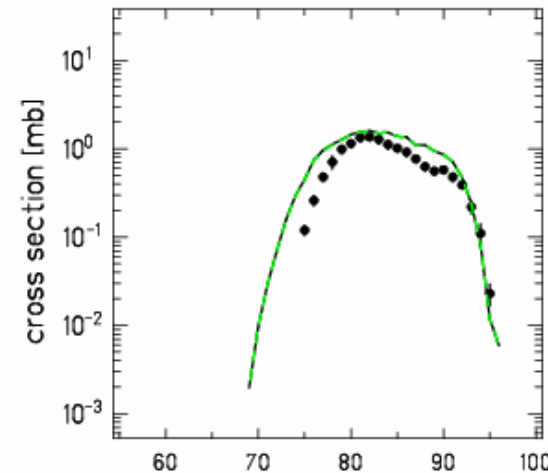
neutron number

Z = 59



neutron number

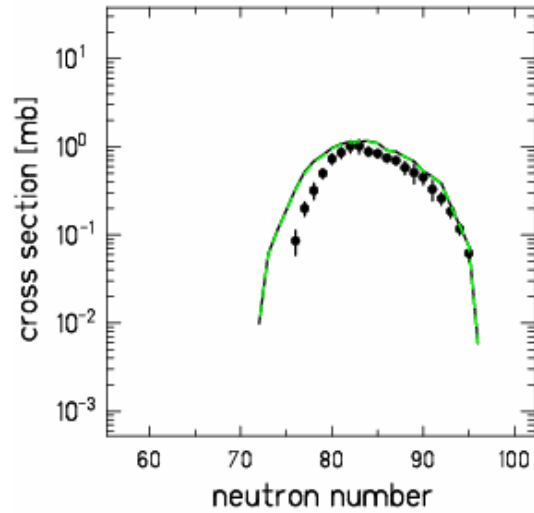
Z = 60



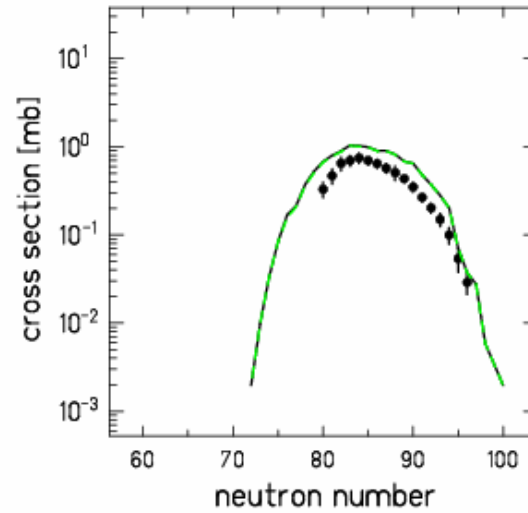
neutron number

# RESULT FOR 1 GeV p on $^{238}\text{U}$

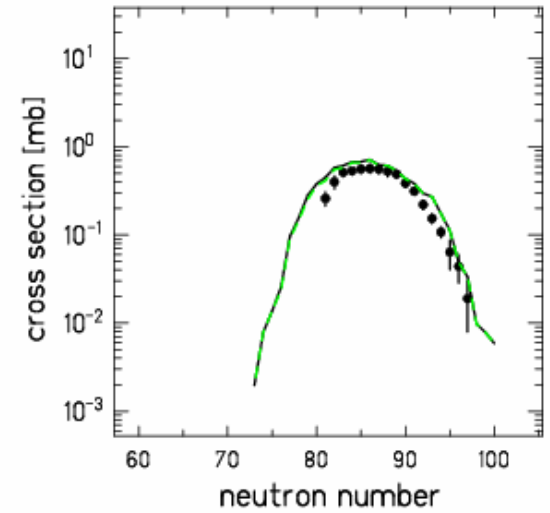
Z = 61



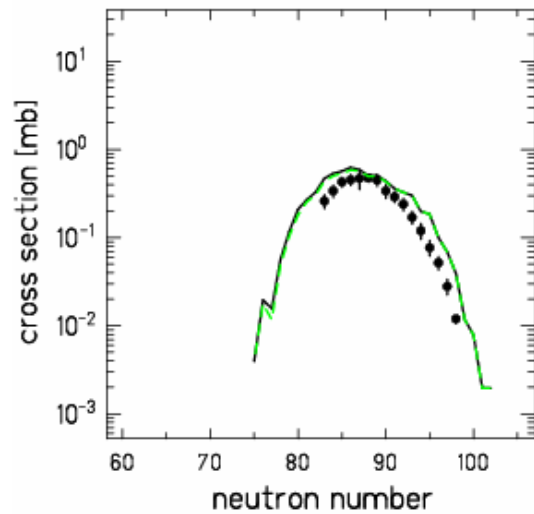
Z = 62



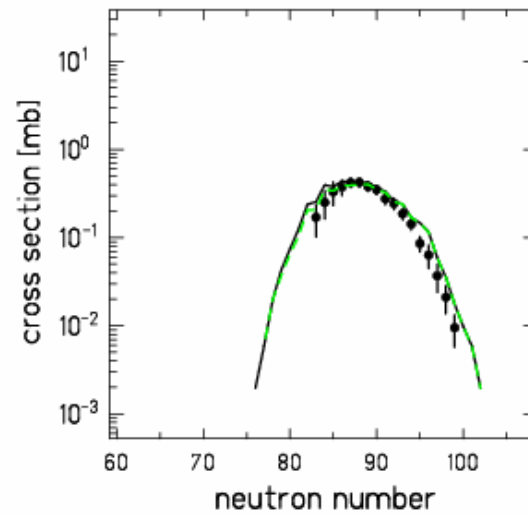
Z = 63



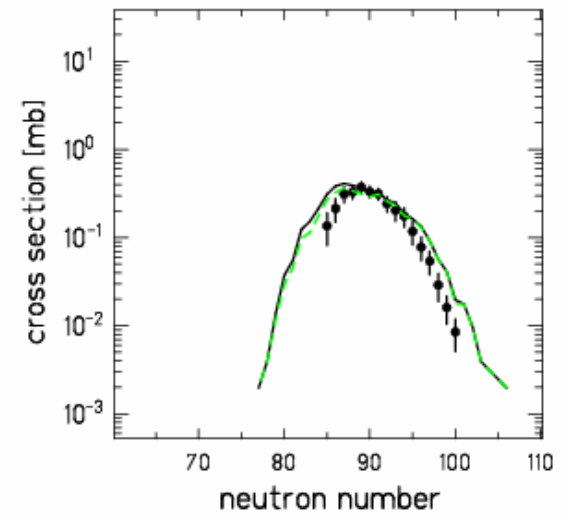
Z = 64



Z = 65

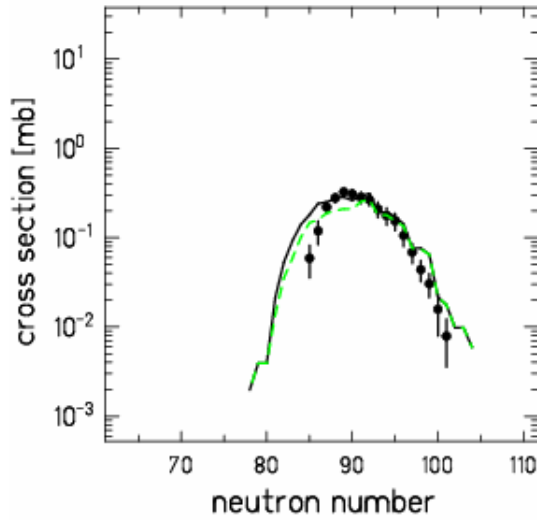


Z = 66

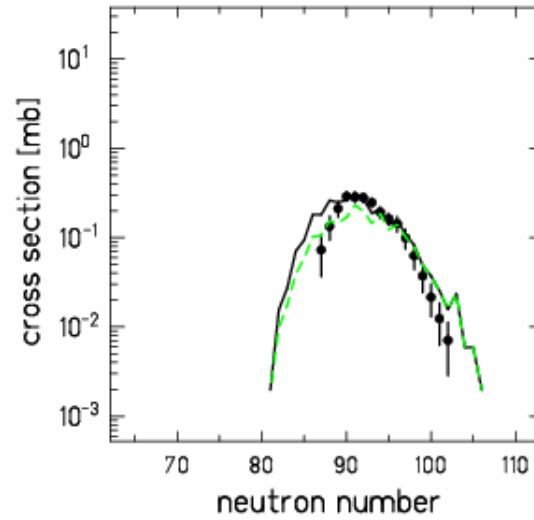


# RESULT FOR 1 GeV p on $^{238}\text{U}$

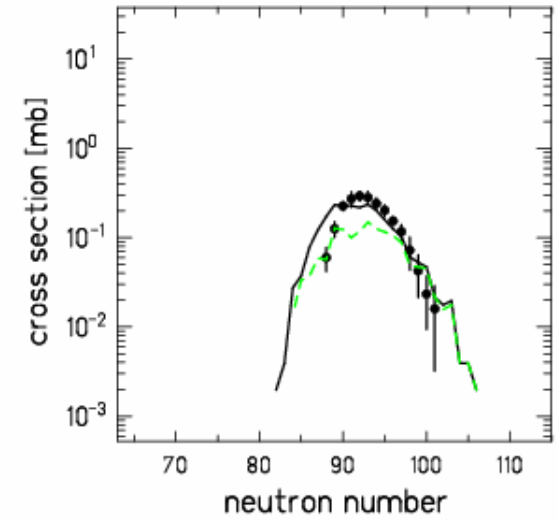
Z = 67



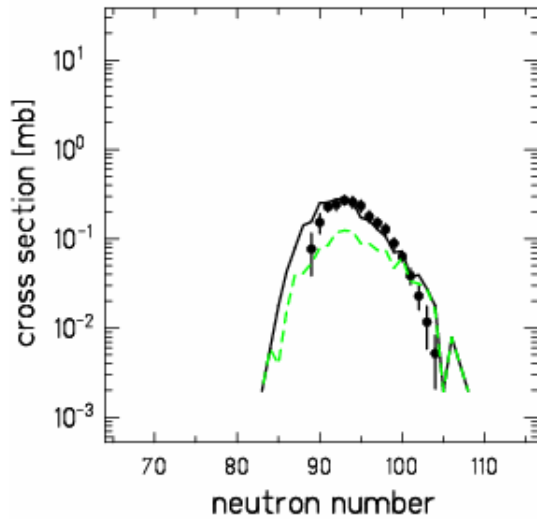
Z = 68



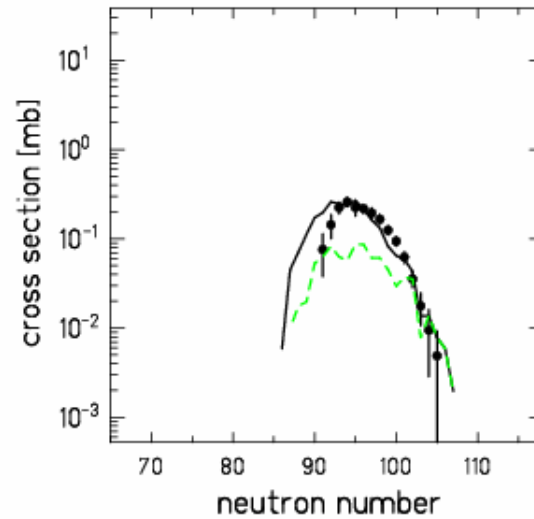
Z = 69



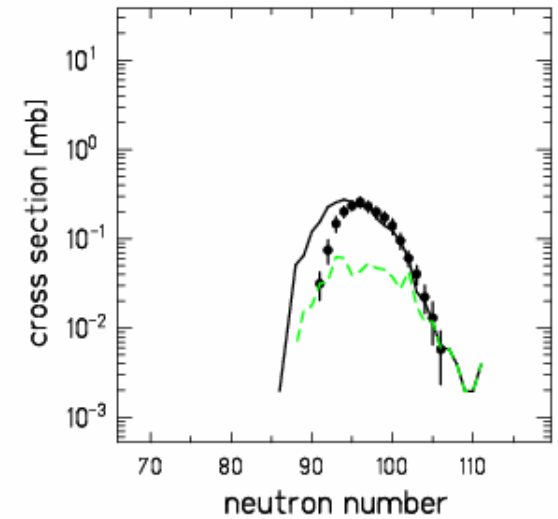
Z = 70



Z = 71



Z = 72



## ADDITIONAL EFFECTS

- 1 — Thermal expansion of the nucleus
- 2 — Pre-formation factor
- 3 — Surface effects on the level density
- 4 — Deformation of the nucleus

For light systems → Thermal instabilities (break-up)

# CONCLUSIONS

## LIGHT NUCLIDES FROM 1 A·GeV $^{238}\text{U} + \text{p}$

### The experimental data:

- Formation cross-section for every isotope, along with its velocity distribution, could be measured at the FRS

### The physics:

- Yields and velocities of light nuclides from 1 A·GeV  $^{238}\text{U} + \text{p}$  indicate a transition from fission to evaporation
- The experimental data could be successfully reproduced by a statistical model, combining a fission approach with the evaporation of intermediate-mass fragments
- No indications for a multifragmentation-type of decay have been observed



**Partial widths  $\Gamma_n$  and  $\Gamma_p$  for emission of neutrons and protons.**

$$\Gamma_n = \frac{2mR^2 g}{2\pi\rho(E - E_r^{gs})} \int_0^{E-B_n} \varepsilon \rho(E - B_n - \varepsilon) d\varepsilon$$

$$\Gamma_p = \frac{2mR^2 g}{2\pi\rho(E - E_r^{gs})} \int_{\varepsilon_c}^{E-B_p} \varepsilon \left(1 - \frac{\varepsilon_c}{\varepsilon}\right) \rho(E - B_p - \varepsilon) d\varepsilon$$

(Approximation without considering tunneling.)

$\Gamma_p$  is reduced by the Coulomb barrier  $\varepsilon_c$ .

# Modelling the Width in A and N/Z of Fission-Product Isotopic Distributions

Approximated parabolic potential

$$U(\eta) = C_{\eta} \cdot (\eta - \eta_o)^2$$

Statistical population:

$$Y(\eta) \propto \exp\{2\sqrt{a(U_o - U(\eta))}\} \rightarrow$$

$$Y(\eta) \propto \exp\left\{-\frac{(\eta - \eta_o)^2}{2\sigma_{\eta}^2}\right\} \quad \text{with}$$

$$2\sigma_{\eta}^2 = \frac{T}{C_{\eta}}$$

$U$  = potential energy,

$\eta$  = either A (mass split) or N/Z (polarisation),

$C_{\eta}$  = stiffness of the potential,

$T$  = nuclear temperature.