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? How to study (loosely bound) 3 body systems (Borromean):

 Preparation of an unbound final state

 e.g. @ GSI:

$$E \geq 100 \text{ A MeV} \Leftrightarrow \beta_{\text{beam}} \gg \beta_{\text{intrinsic}}$$

 Determine and chose reaction mechanism

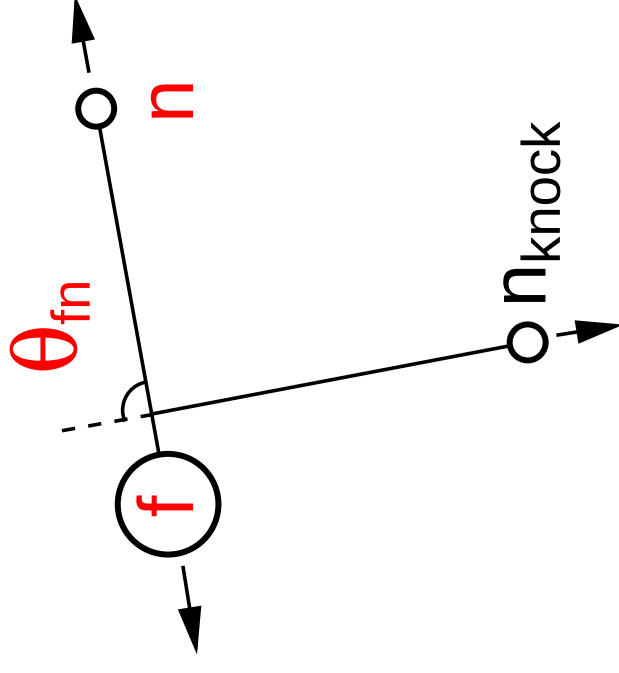
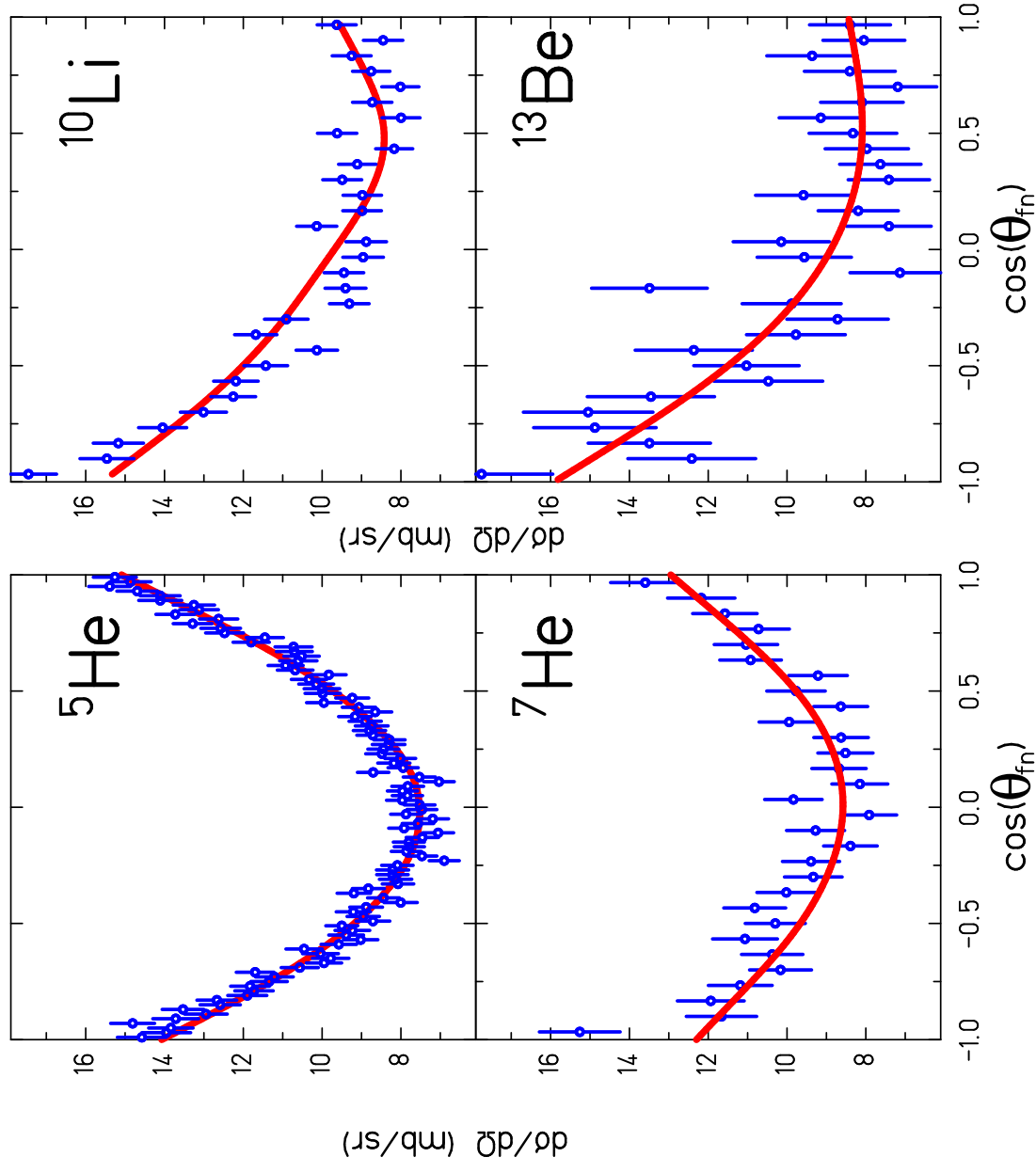
 What is the structure of these nuclei ?
single particle states, core polarisation,
intruder states, shell gaps, ...

 Multiparticle and γ –coincidences:
 β -decay studies, transfer reactions,
coulomb excitation or quasielastic
processes

 Study unbound subsystems (2 body)

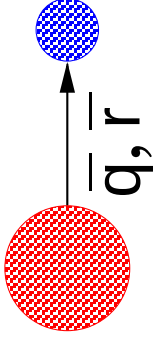
 Study unbound systems (3 body)

Angular correlations



He: p-states
 Li/Be: different parity states

Two-Body



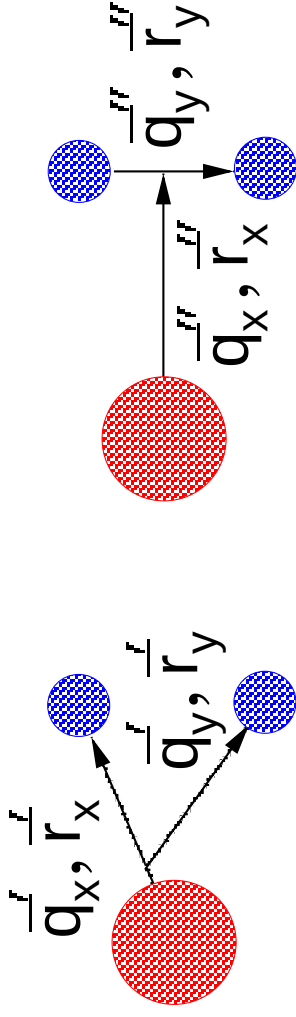
$$\hat{T} \propto \frac{\partial^2}{\partial r^2} + \frac{2}{r} \frac{\partial}{\partial r} - \frac{\ell(\ell+1)}{r^2}$$

$$\hat{L}^2 Y = \ell(\ell+1) Y_m^\ell(\Omega_2)$$

$$d\tau \propto d\Omega$$

Observable $\frac{d\sigma}{d\Omega}$

Three-Body



$$\hat{T} \propto \frac{\partial^2}{\partial \rho^2} + \frac{5}{\rho} \frac{\partial}{\partial \rho} - \frac{\kappa(\kappa+4)}{\rho^2}$$

$$\rho^2 = |\vec{r}_x|^2 + |\vec{r}_y|^2$$

$$\hat{K}^2 \mathcal{Y} = \kappa(\kappa+4) \mathcal{Y}_{m_x m_y}^{\kappa \ell_x \ell_y}(\Omega_5)$$

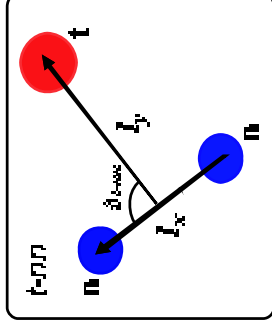
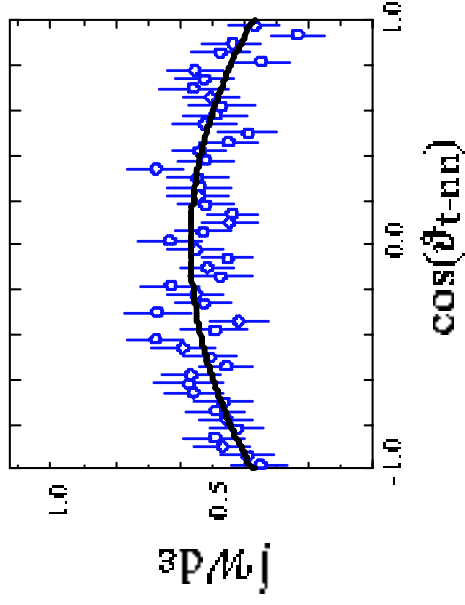
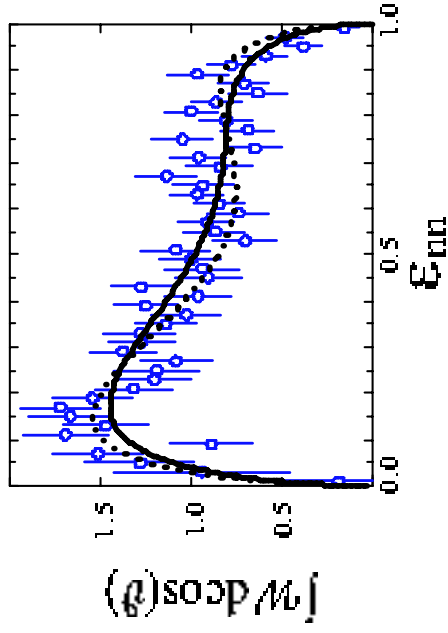
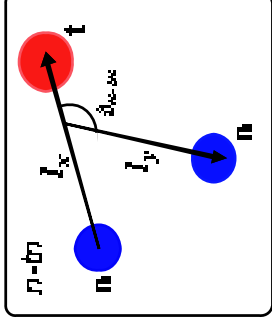
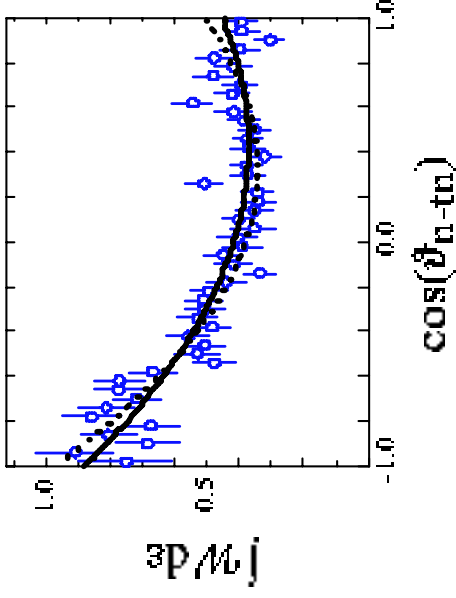
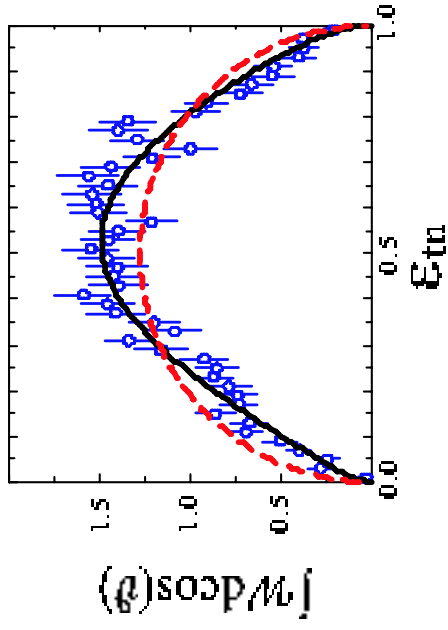
$$\vec{\ell} = \vec{\ell}_x + \vec{\ell}_y, \quad \kappa = 2n + \ell_x + \ell_y$$

$$d\tau \propto \sqrt{\varepsilon(1-\varepsilon)} d\varepsilon d\Omega_x d\Omega_y$$

$$\varepsilon = E_x / (E_x + E_y)$$

Observable $\frac{d^3\sigma}{d\Omega_x d\Omega_y d\varepsilon}$

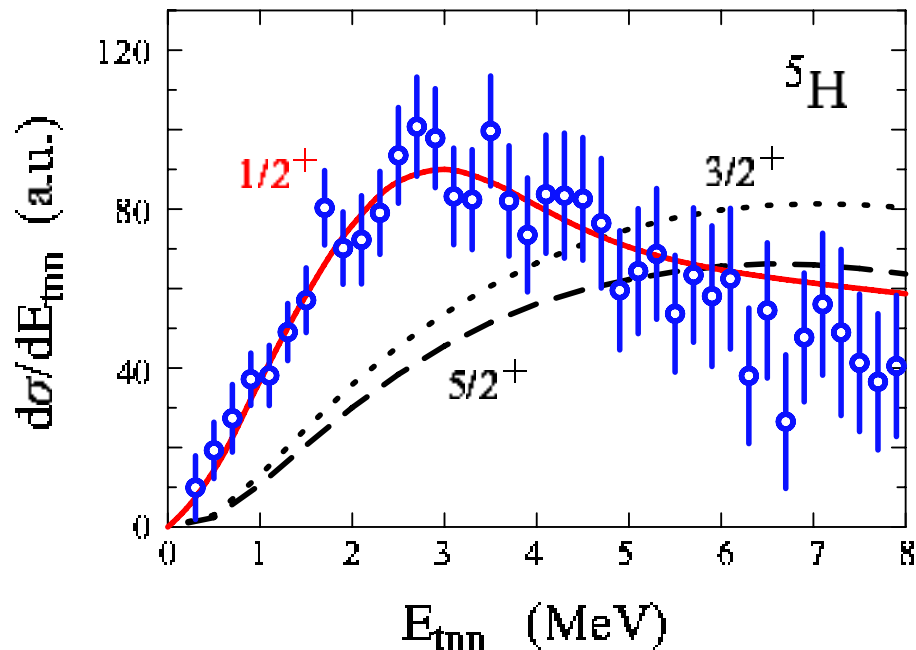
5H: Hyperspherical Harmonics expansion K=0,2



Fits: $\mathcal{W}(\epsilon, \vartheta) \Rightarrow A_{\mathbf{SK}\ell_x\ell_y}$

$$\mathcal{W} = \frac{4}{\pi} \sqrt{\epsilon(1-\epsilon)} \left(8\epsilon(1-\epsilon) \sin^2 \vartheta |A_{1211}|^2 + |A_{0000} - 2(2\epsilon - 1)A_{0200} + 4\sqrt{\epsilon(1-\epsilon)} \cos \vartheta A_{0211}|^2 \right)$$

^5H : Results



SK $\ell_x\ell_y$: t -nn system	0000(%)	0200(%)	1211(%)	Ref.
^6He	4	78	15	[1] th.
^6Be	6(5)	44(12)	50(17)	[2] ex.
^5H	18(3)	45(3)	37(4)	*this

[1] NUP **A632** (1998) 383 / [2] NUP **A505** (1989) 215

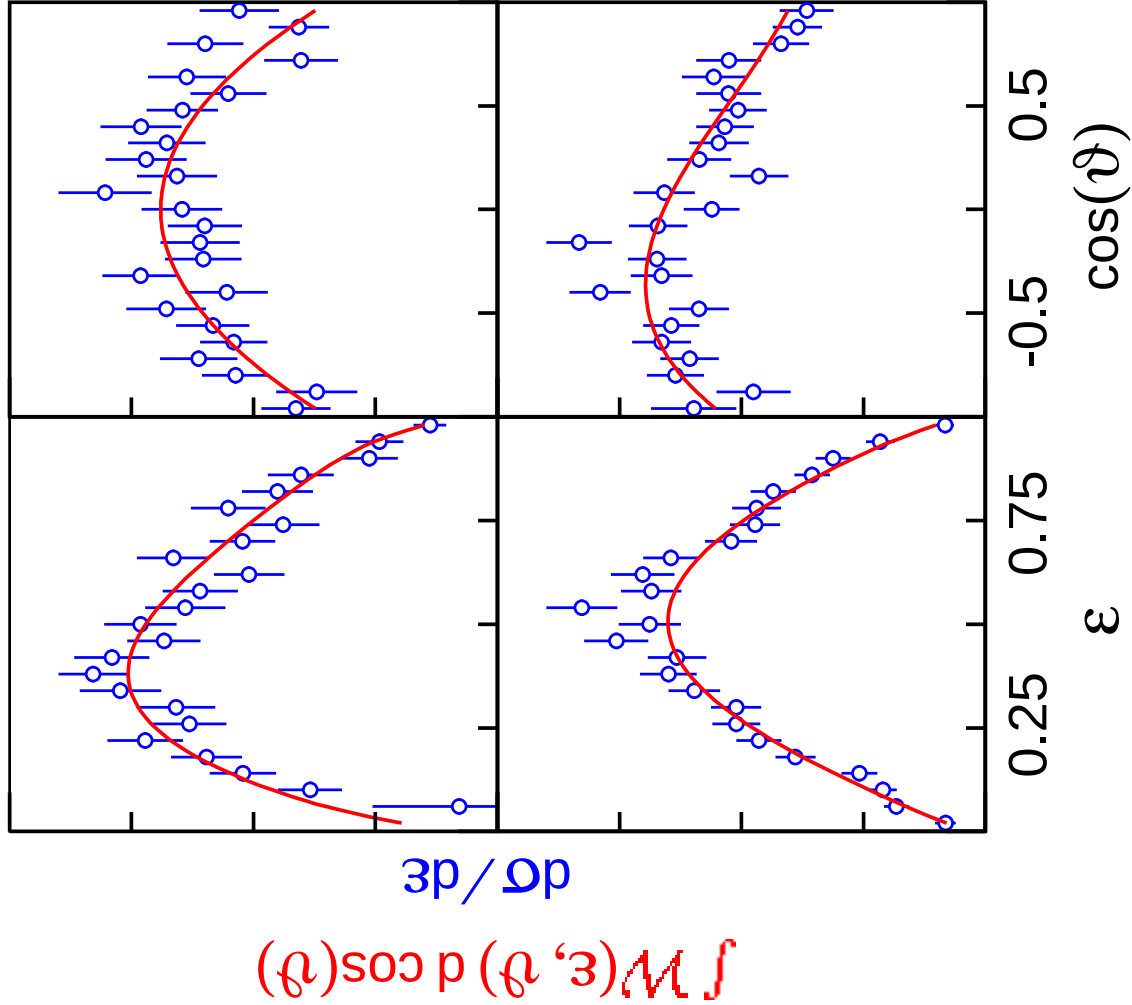
- Pauli forbidden 0211 component: 0.02(9) %
- Consistent description in "T" and "Y" systems (Raynal-Revai coefficients)
- Described by microscopic dynamical calculation assuming a $1/2^+$ state Phys. Rev **C62** (2000) 014312

⇒ Recent GSI work: L.V. Grigorenko et al., in prep.

3-body decay: ${}^6\text{He}^* \rightarrow \alpha + n + n$ (1 - 3 MeV)

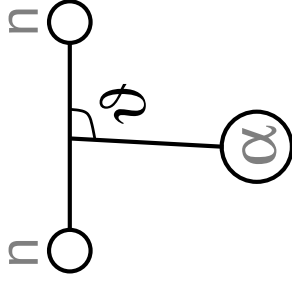
Ansatz for $\mathcal{W}(\varepsilon, \vartheta)$ based on theoretical calculation for $\langle \Psi_{\text{exc}} | \varepsilon_1 | \Psi_{\text{gs}} \rangle$

B.V. Danilin et al., NUPA632 (1998) 383

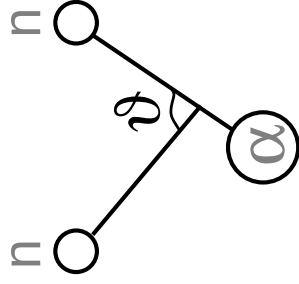


$$\int \mathcal{W}(\varepsilon, \vartheta) d\varepsilon$$

$$d\sigma/d\cos(\vartheta)$$



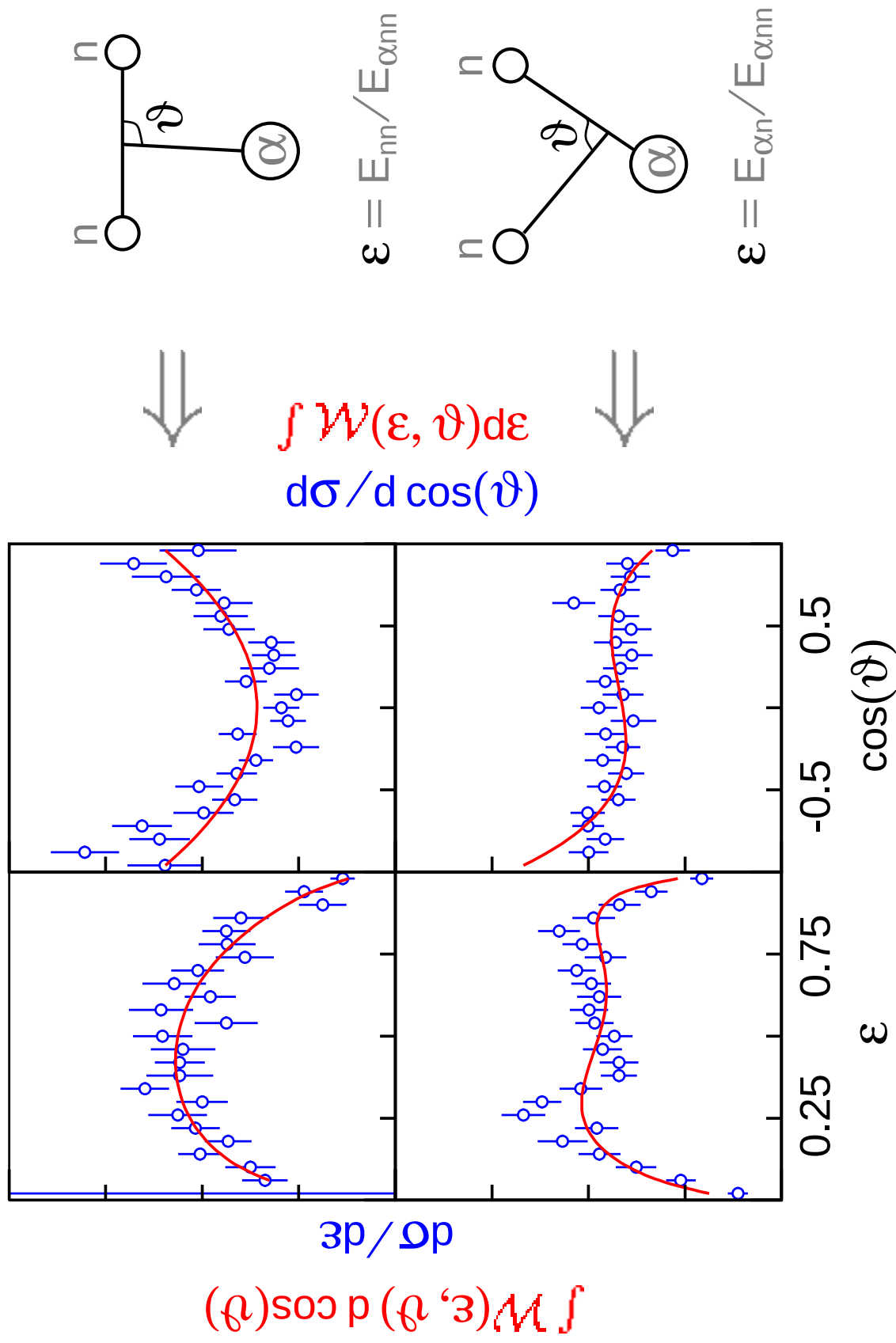
$$\varepsilon = E_{nn}/E_{\alpha nn}$$



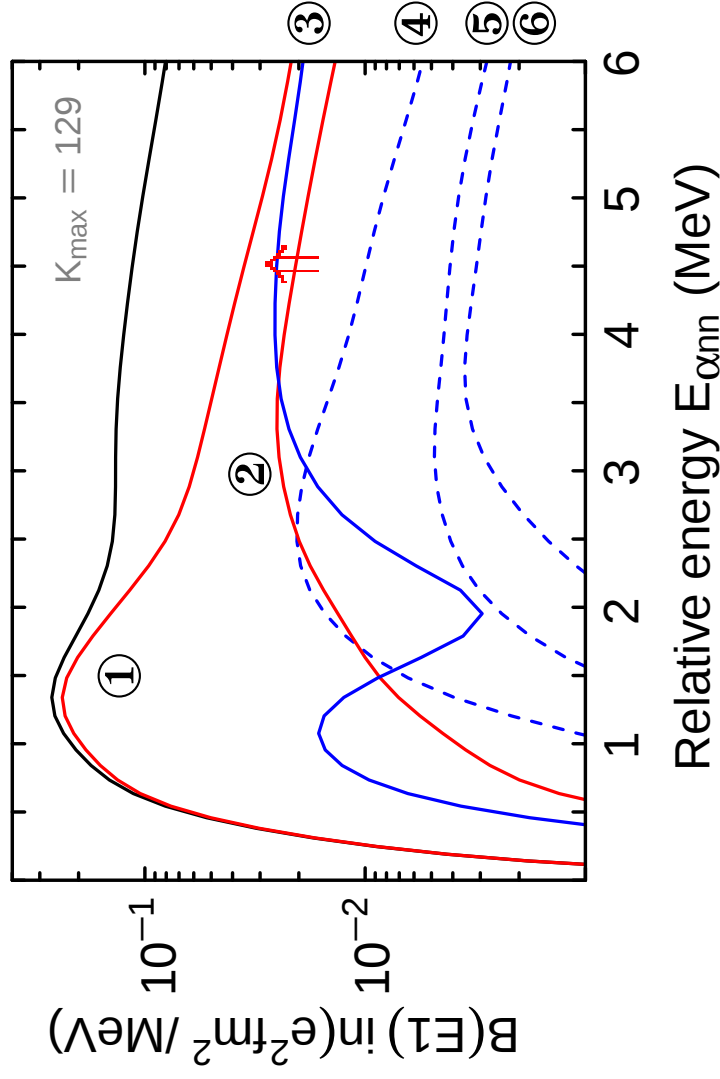
$$\varepsilon = E_{\alpha n}/E_{\alpha nn}$$

3-body decay: ${}^6\text{He}^* \rightarrow \alpha + n + n$ (3 - 6 MeV)

Higher energy, form of $\mathcal{W}(\varepsilon, \vartheta)$ kept $\Rightarrow$ different configuration $\Leftrightarrow$ different amplitudes



3-body decay: ${}^6\text{He}^*$ comparison with theory



B.V. Danilin et al., NUPA**632** (1998) 383

$KL\ell_x\ell_y$

Main components (exp.):

$S = 0: 1101 \text{ ①}, 3121 \text{ ②}$

Additionally Predicted:

$S = 0: 3101 \text{ ③}$

$S = 1: 1110 \text{ ④}, 3112 \text{ ⑤}, 3110 \text{ ⑥}$

${}^6\text{He}$ groundstate:

$S = 0: 2000 / 0000 \text{ \& } S=1$

- Consistent picture ! (preliminary)